# Thickness Sensitivities for the Surface Course of Pavement based on the Variation of the Poisson Coefficient of Bituminous Concrete

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Abstract—The laboratory tests that allow to evaluate the Poisson coefficient of the pavement materials are costly in tropical countries. In the absence of these tests, a finite number of Poisson coefficient is often prescribed to design the pavements. This paper consists of studying the influence of these prescribed values in the structural design of the pavement, especially, on the thickness of the surface course. For this, we show that the values of Poisson coefficient taken between 0.25 and 0.45 are adapted for the flexible pavements because they do not affect the thickness of the surface course. The usefulness of the variation of the Poisson coefficient is illustrated with local data and the results show that the thickness of the bituminous and semi-rigid pavements can change when the prescribed values change.

Keywords—Pavement structures; French method; Poisson coefficient; Bituminous concrete

## I. INTRODUCTION

Several techniques ([1], [3], [5]) have been used to estimate the thickness of the road pavement and some relationship have been established between mechanical parameters and the quality of pavement layer material ([6], [7], [9]). Among these parameters, the Poisson coefficient has been characterized for the lateritic natural grave detailed in [13]. In this work, the behavior of the pavement was studied in laboratory to evaluate the influence of the Poisson coefficient in pavement design. But, this procedure is costly and not always practicable in tropical countries due to the absence of the appropriate infrastructures and the change of material properties.

In Cameroon, the values 0.25 and 0.35 are recommended in ([14], [15], [16], [17], [18]) and another work [26] had prescribed the value 0.45 while guaranteed values to be used for bituminous concrete has been determined by Messi et al. in [1]. It means that the Poisson coefficient can change for the same type of pavement and this paper consists of studying the thickness sensitivities of the surface course under the change of the prescribed Poisson coefficient of bituminous concrete.

In this work, we first present the approach which analyzes the thickness sensitivities by applying the French method ([9], [20], [26]) on the local data. By changing the prescribed Poisson coefficient, we then examine this sensitivity, in order to show that the thickness of the surface course remains Koumbe Mbock., Okpwe Mbarga R. African Center of Excellence in Information and Communication Technologies University of Yaounde I Cameroon

constant for the flexible pavements while it varies for semirigid and bituminous pavements. We conclude our study with a short summary and discussion.

## II. OUR APPROACH

#### A. Input parameters

TABLE I.

For this study, we use the materials to achieve our goal, namely 6 prescribed values of the Poisson coefficient ( $v_{BC}$ ) of the bituminous concrete :

- 3 recommended values : 0.25, 0.35 and 0.45 ([14], [15], [16], [17], [18], [26]);
- 3 calculated values : 0.36, 0.42 and 0.43 [1].

In addition, 3 types of pavement structures are analyzed :

YOUNG MODULUS AND POISSON COEFFICIENT

- Type 1 : flexible pavement (table I) ;
- Type 2 : bituminous pavement (table I) ;
- Type 3 : semi-rigid pavement (table I).

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	Type of Pavement	Surface course	Base course	Subbase
	1 avenuent	Material	Material	Material
	1	BC <sup>a</sup>	CG/ Ci <sup>d</sup>	NLG <sup>e</sup>
	2	BC <sup>a</sup>	BG <sup>b</sup>	-
	3	BC <sup>a</sup>	CeG <sup>c</sup>	-

<sup>a.</sup> BC.: Bituminous concrete.

<sup>b.</sup> BG : Bitumen gravel

<sup>c.</sup> CeG : Cement grave

 $^{d.}$  CG : Crushed grave 0/31.5 – Ci : Cinder

e. NLG : Natural laterite gravel.

The design of these pavements is done with the help of the software ALIZE 3 [19] taking into account the recommended values E and v of [26] as it is showed in the table II.

 TABLE II.
 YOUNG MODULUS AND POISSON COEFFICIENT

Materials					
Materials	BC	BG	CeG	CG/Ci	NLG
E (MPa)	2 450	3 500	23 000	400	150
v	$v_{BC}$	0.35	0.25	0.35	0.35

Other parameters used in the French method are important in the pavement design, namely, the traffic and the subgrade parameter. Having the materials defined in the table II above, the additional parameters are showed in the tables III and IV below.

TABLE III. MECHANICAL CHARACTERISTIC OF THE SUBGRADE [5]

T			
Layer	Category	E (MPa)	v
	S2	50	0.35
Subgrade	S3	75	0.35
-	S4	150	0.35

In this table, we denote by S2, S3, S4 the subgrade material with given E and v.

TABLE IV. TRAFFIC CLASSES DEFINED IN TROPICAL COUNTRIES [5]

EN <sup>a</sup>	Traffic class	Equivalent number of vehicle per day		
$< 5 \times 10^{5}$	T1	< 300		
From 5x10 <sup>5</sup> to 1.5x10 <sup>6</sup>	T2	300 to 1 000		
From 1.5x10 <sup>6</sup> to 4x10 <sup>6</sup>	T3	1 000 to 3 000		
From 4x10 <sup>6</sup> to 10 <sup>7</sup>	T4	3 000 to 6 000		

EN: Equivalent number of axles.

## B. States of stress and strain

In continuum mechanics, the states of stress and strain at a point in cylindrical coordinates are determined by :

- $\sigma_r$ ,  $\sigma_t$ ,  $\sigma_z$ : normal stresses ;
- $\tau_{tz}$ ,  $\tau_{rz}$ ,  $\tau_{rt}$  : shear stresses ;
- $\varepsilon_r, \varepsilon_t, \varepsilon_z$ : linear strains;
- $\delta_{tz}$ ,  $\delta_{rz}$ ,  $\delta_{rt}$ : angular strains.

With known Young modulus and Poisson coefficient given by the formulas:

$$E_i = \mu_i (3.\lambda_i + \mu_i) / (\lambda_i + \mu_i)$$
(1)

And

$$v_i = \lambda_i / (2.(\lambda_i + \mu_i)) \tag{2}$$

We determine the Lame coefficients  $\mu$  and  $\lambda$ . According to the model prescribed by Burmister [19], we have the following graphic :

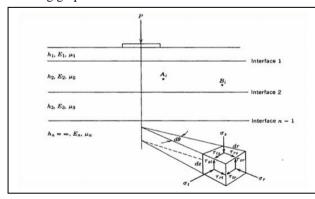


Fig. 1. State of stress at a point in cylindric coordinates

The calculus made with the software ALIZE 3 provides all the information related to the stress and strain tensors for each pavement structure. From these informations, the following values are chosen and compared to admissible values in order to design the pavement structure.

TABLE V.	MAXIMUM STRESS OR STRAIN TO
	CONSIDERATE [5]

Material	Stress or strain (max)
Hydrocarbon materials	ε <sub>t</sub>
Concrete and hydraulic binder treated materials	$\sigma_t$
Untreated soil and materials	ε <sub>z</sub>

We note that the admissible values are found in [5].

TABLE VI. ADMISSIBLE DEFLECTION IN FUNCTION OF TRAFFIC CLASS
[5]

[0]				
Traffic class	Admissible deflections (in 1/100 mm)			
T1	125			
T2	90			
T3	65			
T4	40			

### C. Description of the procedure

To study the thickness sensitivities of the surface course under the change of the Poisson coefficient of the bituminous concrete, we follow the steps below :

- The pavement is designed firstly with the recommended values E and v;
- The Poisson coefficient of the bituminous concrete is modified subject to keep the thicknesses of the base course and subbase constant.

## III. PRESENTATION OF THE RESULTS

A. Case study of the pavement  $n^{\circ}1$ 

In this case, we have the input data :

- Traffic class T1;
- Pavement materials and parameters (*E* and *v*) (Table VII);
- Subgrade (soil) mechanical characteristics (*E* and *v*) (Table VII).

TABLE VII. MECHANICAL CHARACTERISTICS OF THE PAVEMENT N°1

Layer	Material/ Category	E (MPa)	v		
Surface course	BC	2 450	U BC		
Base course	CG/Ci	400	0.35		
Subgrade	S2	50	0.35		

With these entries, the software ALIZE 3 gives us different thicknesses of the surface course as shown in the table VIII and the figure 2.

TABLE VIII. THICKNESS OF THE SURFACE COURSE IN FUNCTION OF THE POISSON COEFFICIENT OF THE BITUMINOUS CONCRETE

CONCILLE			
v <sub>BC</sub> Thickness (cm)			
0.25	3		
0.35	3		
0.36	3		
0.42	3		
0.43	3		
0.45	3		

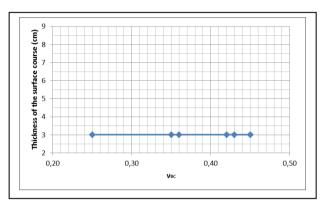


Fig. 2. Thickness of the surface course in function of the Poisson coefficient of the bituminous concrete for the pavement  $n^\circ l$ 

In the figure 2, we can see that the thickness of the surface course remains constant under the change of the prescribed Poisson coefficient of the bituminous concrete.

## B. Application on a finite number of pavement structures

We applied the procedure described in the previous section to determine the thickness of the surface course under the change of the Poisson coefficient of the bituminous concrete for 36 pavement structures.

These pavement structures are presented in the table IX.

TABLE IX.	DESCRIPTION OF THE PAVEMENT STRUCTURES

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Type of Pavement pavement		Surface course	Base course
		Material	Material
	1	BC	CG/ Ci
	2	BC	CG/Ci
	3	BC	CG/ Ci
	4	BC	CG/ Ci
	5	BC	CG/Ci
1	6	BC	CG/ Ci
1	7	BC	CG/Ci
	8	BC	CG/Ci
	9	BC	CG/ Ci
	10	BC	CG/Ci
	11	BC	CG/Ci
	12	BC	CG/ Ci
2	13	BC	BG
2	14	BC	BG

	15	BC	BG
	16	BC	BG
	17	BC	BG
	18	BC	BG
	19	BC	BG
	20	BC	BG
	21	BC	BG
	22	BC	BG
	23	BC	BG
	24	BC	BG
	25	BC	CeG
	26	BC	CeG
	27	BC	CeG
	28	BC	CeG
	29	BC	CeG
2	30	BC	CeG
3	31	BC	CeG
	32	BC	CeG
	33	BC	CeG
	34	BC	CeG
	35	BC	CeG
	36	BC	CeG

Type of Pavement	Numbered pavement	Subbase	Subgrade	Traffic	
	1	Material	Category	class	
	1	NLG	S2	T1	
	2	NLG	S3	T1	
	3	NLG	S4	T1	
	4	NLG	S2	T2	
	5	NLG	S3	T2	
1	6	NLG	S4	T2	
1	7	NLG	S2	T3	
	8	NLG	S3	T3	
	9	NLG	S4	T3	
	10	NLG	S2	T4	
	11	NLG	S3	T4	
	12	NLG	S4	T4	
	13	-	S2	T1	
	14	-	S3	T1	
	15	-	S4	T1	
	16	-	S2	T2	
	17	-	S3	T2	
2	18	-	S4	T2	
2	19	-	S2	T3	
	20	-	S3	T3	
	21	-	S4	T3	
	22	-	S2	T4	
	23	-	S3	T4	
	24	-	S4	T4	
	25	-	S2	T1	
	26	-	S3	T1	
	27	-	S4	T1	
	28	-	S2	T2	
	29	-	S3	T2	
2	30	-	S4	T2	
3	31	-	S2	T3	
	32	-	S3	T3	
	33	-	S4	T3	
	34	-	S2	T4	
	35	-	S3	T4	
	36	-	S4	T4	

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The next tables and figures show that the thickness of surface course can vary when the prescribed Poisson coefficient of the bituminous concrete changes.

TABLE X.	THICKNESS OF THE SURFACE COURSE IN
FUNCTION OF T	HE POISSON COEFFICIENT OF THE BITUMINOUS
CONCI	RETE FOR THE FLEXIBLE PAVEMENTS

Numbered	Thickness of the surface course (cm)						
pavement	$v_{BC} = 0.25$	$v_{BC} = 0.35$	$v_{BC} = 0.36$	$v_{BC} = 0.42$	$v_{BC} = 0.43$	$v_{BC} = 0.45$	
1	3	3	3	3	3	3	
2	3	3	3	3	3	3	
3	3	3	3	3	3	3	
4	3	3	3	3	3	3	
5	3	3	3	3	3	3	
6	3	3	3	3	3	3	
7	4	4	4	4	4	4	
8	4	4	4	4	4	4	
9	4	4	4	4	4	4	
10	4	4	4	4	4	4	
11	4	4	4	4	4	4	
12	4	4	4	4	4	4	

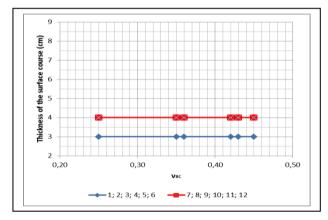


Fig. 3. Thickness of the surface course in function of the Poisson coefficient of the bituminous concrete for flexible pavements

In the figure 3, we can see that the thickness of the surface course of the bituminous pavement does not change under the prescribed Poisson coefficient of the bituminous concrete.

TABLE XI.	THICKNESS OF THE SURFACE COURSE IN
FUNCTION OF	THE POISSON COEFFICIENT OF THE BITUMINOUS
CONCH	RETE FOR THE BITUMINOUS PAVEMENTS

Numbered	Thickness of the surface course (cm)						
pavement	$v_{BC} = 0.25$	$v_{BC} = 0.35$	$v_{BC} = 0.36$	$v_{BC} = 0.42$	$v_{BC} = 0.43$	$v_{BC} = 0.45$	
13	3	3	3	3	3	3	
14	3	3	3	3	3	3	
15	3	3	3	3	3	3	
16	4	4	4	4	4	4	
17	4	4	4	4	4	4	
18	5	5	5	4	4	4	
19	7	7	7	6	6	6	

ĺ	20	7	6	6	6	6	5
	21	7	7	6	6	6	6
	22	8	7	7	6	6	6
	23	8	7	7	7	7	6
	24	8	7	7	6	6	6

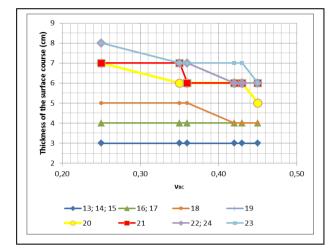


Fig. 4. Thickness of the surface course in function of the Poisson coefficient of the bituminous concrete for bituminous pavements

In the figure 4, the thickness of the surface course of the bituminous pavement changes under the prescribed Poisson coefficient of the bituminous concrete for the pavements numbered from 18 to 23 in contrary to those numbered from 13 to 17.

TABLE XII. THICKNESS OF THE SURFACE COURSE IN FUNCTION OF THE POISSON COEFFICIENT OF THE BITUMINOUS CONCRETE FOR THE SEMI-RIGID PAVEMENTS

Numbered	Thickness of the surface course (cm)						
pavement	$v_{BC} = 0.25$	$v_{BC} = 0.35$	$v_{BC} = 0.36$	$v_{BC} = 0.42$	$v_{BC} = 0.43$	$v_{BC} = 0.45$	
25	4	3	3	3	3	3	
26	6	5	5	4	4	4	
27	4	3	3	3	3	3	
28	6	5	5	4	4	4	
29	5	4	4	3	3	3	
30	8	7	7	6	6	6	
31	7	6	6	5	5	5	
32	6	5	5	4	4	4	
33	9	8	7	7	6	6	
34	8	7	7	6	6	6	
35	7	6	6	5	5	5	
36	7	6	6	5	5	5	

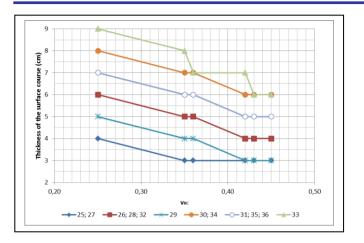


Fig. 5. Thickness of the surface course in function of the Poisson coefficient of the bituminous concrete for semi-rigid pavements

In the figure 5, we observe that the thickness of the surface course of the semi-rigid pavement changes under the prescribed Poisson coefficient of the bituminous concrete for the corresponding pavements.

#### IV. CONCLUSION

In this paper, the French method has been applied to study the thickness sensitivities of the surface course under the variation of the Poisson coefficient of the bituminous concrete. The case study of flexible pavements has shown that the prescribed values taken between 0.25 and 0.45 do not change the thickness of the surface course. In opposition, the analysis of the semi-rigid and bituminous pavements has shown that the change in Poisson coefficient can modify the thickness of the surface course considerably. We conclude that this second case study is sensitive under the variation of the Poisson coefficient than the flexible pavements. It is important to take into account the influence of the variation of the Poisson coefficient before recommending the mechanical values for these pavements design in tropical countries.

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#### REFERENCES

- A. F. Messi, F. Sikali, B. C. Toh, "Proposal of minimum and maximum values for the poisson's ratio of asphaltic concrete", International Journal of Lastest Research in Science and Technology, 2014, pp 25-29.
- [2] A. F. Messi, K. Mbock, R. P. M. Okpwe, J. Madjadoumbaye, T. F. Miyo, "New approach for determining Young modulus and Poisson coefficient in the structural design of the pavement", International Journal of Engineering Research & Technology, 2016, pp. 616-621.
- [3] Association of State Highway, Official AASHTO guide for design of pavement structures. Association of State Highway, American, Washington, D. C., 1993.
- [4] Austroads, Pavement design. Sydney, 2004.
- [5] CEBTP, Guide pratique de dimensionnement des chaussées pour les pays tropicaux. Ministère des relations extérieures, Coopération et Développement, République Française, 1984.

- [6] Department of the Environment, RN-29, A guide to the structural design for new roads. Department of the Environment, HMSO, London, 1970.
- [7] E. E. Putri, N. S. V. K. Rao, M. A. Mannan, "Evaluation of the modulus of elasticity and resilient modulus for hightway subgrades," EJGE, University of Malaysia Sabah, Kota Kinabaly, Malaysia, 2010.
- [8] F. A. Miyo Tchatchouang, Influence de l'inexactitude des valeurs des paramètres mécaniques (E et v) des matériaux constitutifs des chaussées sur le dimensionnement de celles-ci, simulation par le logiciel Alizé 3. Master in Engineering thesis, National Advanced School of Engineering, Cameroon, 2015.
- [9] H. Goacolu et Al. "La méthode française de dimensionnement," LCPC, p. 15, 2003.
- [10] H. L. Theyse, M. Beer, F. C. Rust, "Overview of the South African mechanistic pavement design analysis method", Transportation Research Record, 1539, TRB, National Research Council, Washington, D.C., 1996, pp.6-17.
- [11] IRC, Guidelines for the design of flexible pavements, 2nd revision. IRC, 2001.
- [12] Japan Road Association, Manual for asphalt pavement. Japan Road Association, Japan, 1989.
- [13] J. Madjadoumbaye, S. M. Lezin, P. Mangoua, S. F. Takoukam, T. T. Tamo, "Poisson's ratio in the choice of thicknesses of layers of pavement structure in lateritic natural grave", International Journal of Latest Research in Science and Technology, 2012.
- [14] LABOGENIE, Etudes géotechniques routières en vue de la construction de certaines routes du réseau national-lot 9 : Tronçon (RP19) Dschang-Fontem-Bakebe, Cameroon, 2012.
- [15] LABOGENIE, Etudes géotechniques routières en vue de la construction de certaines routes du réseau national-lot 9 : Road Ring Carrefour Nyos-Weh. LABOGENIE, Cameroon, 2012.
- [16] LABOGENIE, Etudes géotechniques routières en vue de la construction de certaines routes du réseau national-lot 9 : Road Ring (RN11) Kumbo-Nkambe-Misaje-Mungong-Kimbi-Nyos-Weh-Wum. LABOGENIE, Cameroon, 2012.
- [17] LABOGENIE, Recommandation pour l'utilisation des assises de chaussées en graveleux latéritiques. LABOGENIE, Cameroon, 1983.
- [18] LABOGENIE, Recommandation pour l'utilisation des assises de chaussées en graves concassées. LABOGENIE, Cameroon, 1983.
- [19] LCPC, Manuel d'utilisation du logiciel ALIZE- LCPC version 1.3. LCPC, 2010.
- [20] LCPC and SETRA, French design manual for pavement structures. Guide Technique, Union Des Synducates, De L'industrie Routiere, 1997.
- [21] M. Kassogue, G. Hebert, M. Massiera, Contrôle de la qualité sur les matériaux des couches de chaussée (revêtement exclu). Faculté d'Ingénierie (Génie Civil), Université de Moncton, Canada, 2002.
- [22] M. Karray, G. Lefebre, "Significance and evaluation of Poisson's ratio in Rayleigh wave testing", Canadian Geotechnical Journal, 2008.
- [23] NCHRP, Mechanistic-empirical design of new & rehabilitated pavement structures, 2011.
- [24] N. T. TRAN, Valorisation de sédiments marins et fluviaux en technique routière. PhD Thesis, Université d'Artois, France, 2009.
- [25] RstO 2000, Richtlinien f
  ür die Standardisierung des Oberbaues von Verkehrsfl
  ächen, Entwurf, September 1999.
- [26] SETRA-LCPC. Conception et dimensionnement des structures de chaussées. Guide technique, LCPC, 1994.
- [27] Shell International Petroleum Company Limited, Shell pavement design manual – asphalt pavements and overlays for road traffic, Shell International Petroleum Company Limited, London, 1978.
- [28] S. Triaw, Dimensionnement mécaniste-empirique des structures de chaussées: application au tronçon Séo-Diourbel. Master in Engineering thesis. Ecole Supérieure Polytechnique Centre, Senegal, 2006.