Study of the Leaching of A Manganese Mining Residue by $\text{Na}_2\text{SO}_3$ in Sulfuric Acid Solution

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Abstract

This work presents a party results of a study on a method of tailings management manganese mine in operation, the deposit IMINI is the largest manganese deposit in Morocco. These residues from the treatment plant pyrolusite, have a relatively fine particle size (- 710 microns) and Mn content ranging from 31.6% to 39.2%. All these residues are removed and deposited near the mine. The studied parameters were the initial concentration of Na2SO3 and H2SO4, and solid-to-liquid ratio. Statistical techniques were used to determine that pulp density and Na2SO3 concentration were the most significant factors affecting the leaching kinetics and to determine the optimum conditions for dissolution. The kinetic data were analyzed with the shrinking particle and shrinking core models. A new variant of the shrinking core model (SCM) best fitted the kinetic data in which both the interfacial transfer and diffusion across the product layer affect the reaction rate. The orders of reaction with respect to [Na2SO3], [H2SO4] and (S/L) were 1.9, 0.8, and 2.9 respectively. The activation energy for the dissolution was found to be 54.2 kJ/mol and a semi-empirical rate equation was derived to describe the process.

1 Introduction

Manganese is an essential commodity for the steel industry, which plays an important role in industrial and economic development. Beneficiation of low-grade manganese ores is an area of hydrometallurgy that has been extensively studied [1], they could be of strategic international interest, but, owing to their complex nature and the morphology and peculiar surface properties of the mineral, the ore is not amenable to concentration by conventional methods such as flotation, gravity separation, magnetic treatment, etc. [2].

Manganese can be extracted from its dioxide ores either by reduction roasting followed by acid leaching or by aqueous reduction using various reducing agents. The former involves high temperature, whereas the latter can be carried out at room temperature and atmospheric pressure. Leaching experiments have been carried out using various reducing agents and acids [25, 3].

Use of SO2 as reducing agent is encouraged by its rapid rate of reaction, low temperature operation, ease of purifying leach liquors and elimination of barren solution disposal problems [4][7]. Reductive dissolution of manganese dioxide by SO2 is of industrial importance for the treatment of manganese [9] [10] or deep-sea manganese nodules [11][3]. Typical studies on leaching of manganese ores with SO2 or sulfite salts are summarised in (Tab.1).

Das et al.[14, 15] proposed a random nucleation equation for the kinetics of extraction of manganese from low-grade oxidised ores by FeSO4. Many studies have been carried out to leach manganese oxides and sulfide minerals simultaneously in an acid medium, H2SO4 or HCl. In this leaching process, the sulfide minerals function as reductants while the manganese oxides as oxidants. The sulfide minerals include galena (PbS) [16], sphalerite (ZnS) [16, 17, 18] or zinc matt [17], pyrite (FeS2)[19, 20, 21, 16, 22], nickel matte [17], pyriti-ferrous lignite [23].

Many studies have focused on reductive leaching of manganiferous ores containing tetravalent manganese using organic reductants, including sawdust [24], glucose, sucrose [25, 26], lactose [26, 28], glycerine [29], oxalic acid, citric acid, tartaric acid, formic acid [30, 31], molasses in nitric acid solution [32], Molasses Alcohol Wastewater in H2SO4 [33] and triethanolamine and thiosulfate [34].

Aqueous SO2 has proven to be an effective leachant because of rapid rate of dissolution, low temperatures, relative ease of purifying leach liquors and elimination of barren-solution disposal problems [42][46][43].

In the studies using low manganese ores [44, 23, 45], the rate was proposed to be controlled by SO2 diffusion to the reaction surface, evidenced by a low apparent activation energy of 16.6 kJ/mol. Twice the stoichiometric quantity of SO2 was required for dissolution of manganese. The (NH4)2SO3-bisulfite mixture at the bisulfite/H2SO4(w/w) ratio of 1:(0.52–1.55) was also used as the reductant in leaching the Fe–Mn ore concretions [47, 48]. The reaction rate was found to be first order with respect to SO2 concentration and controlled by diffusion of SO2 to the reaction surface [48].

Jan D. Miller and Rong-Yu Wan (1983)[47] proposed that the reduction reaction of MnO2 in aqueous SO2 solution is controlled by an electrochemical surface reaction and that The rate of reaction was significantly dependent on temperature. The apparent activation energy of 71.5 kJ/mol supports the conclusion that the electrochemical reaction is limited by a surface reaction mechanism. To these controversial results, the proposed model [49] seems adequate for the describe mechanism dissolution of MnO2 by sulphite.

This work addresses the most statistically significant factors affecting the dissolution kinetics of a manganese mining residue in Na2SO3/H2SO4 solution. The reaction orders with respect to the process parameters were determined and a semi-
empirical rate equation was developed, a quantitative estimation of the effect of various parameters can be determined by optimization using the statistical design of experiment (DOE) technique. For this purpose, the simultaneous effects of three control factors including Na₂SO₃ and H₂SO₄ concentration and pulp density were studied using response surface methodology (RSM).

2 Materials and methods

2.1 Materials characterization

A representative sample of residue from the the IMINI mine area of Ouarzazate Province (Morrocco) was supplied by the societe Miniere (SACEM). The residu as received was thoroughly blended by rolling. Riffled samples were then collected for size distribution, chemical analysis and mineralogical characterization.

The X-ray diffraction (XRD) determination of the structures present in the product was carried out by an X’Pert Pro powder diffractometer with a vertical configuration using a power of 45 kV and a current of 40 mA. The solid products were dried at 105 °C for 24 h before each analysis. The XRD analysis of the raw product is shown on (Fig:2.1). (Tab.2) gives the chemical composition of the sample. X-ray fluorescence spectrometry has also revealed the presence of a number of trace elements such as K, Na and P. Sieve analysis of the ore is reported on (Fig:2.2). The IMINI manganese ore is characterized by the presence of a colloidal highly hydrated MnO₂ gel, while crystalline phases include silicate gangue minerals (albite, anorthite, quartz, etc.), though a few peaks are attributable to manganese dioxide minerals (pyrolusite, pisolomelane and manganomelane [45].

<table>
<thead>
<tr>
<th>Feed/Regents</th>
<th>Conditions</th>
<th>Key results</th>
<th>Ref</th>
</tr>
</thead>
<tbody>
<tr>
<td>MnO₂ minerals /Aq. SO₂</td>
<td>Studied leaching chemistry</td>
<td>Sulfate/dithionate ratio, depends on pH Eh and Temp.</td>
<td>[56, 57]</td>
</tr>
<tr>
<td>Rich Mn ore (&gt;40% Mn)</td>
<td>Atm. pressure Aq. SO₂ and room temp</td>
<td>&gt;95% Mn in 10 min</td>
<td>[9]</td>
</tr>
<tr>
<td>Low Mn ore (&lt;40% Mn)</td>
<td>Lime for neutralisation</td>
<td>&gt;60% Mn, meeting ferro-manganese</td>
<td>[58]</td>
</tr>
<tr>
<td>Low Mn ore (&lt;40% Mn)</td>
<td>Atm. pressure and room temp.</td>
<td>Rapid leaching rate Aq. SO₄ 95% Mn recovery</td>
<td>[51, 52]</td>
</tr>
<tr>
<td>Low Mn ore (&lt;40% Mn)</td>
<td>&lt;60 °C controlled Eh for adding SO₂</td>
<td>minimised dithionate to lg/L</td>
<td>[59, 60]</td>
</tr>
<tr>
<td>Low Mn slimes Dithionate</td>
<td>90% Mn recovery 55-60% Mn content</td>
<td></td>
<td>[61]</td>
</tr>
<tr>
<td>Fe–Mn concretions (NH₄)₂SO₄–baufite–H₂SO₄</td>
<td>pH 3.5–5.5 50–70 °C</td>
<td>96% Mn recovery</td>
<td>[53]</td>
</tr>
<tr>
<td>Fe–Mn concretions</td>
<td>Kinetic study</td>
<td></td>
<td>[54]</td>
</tr>
<tr>
<td>Low Mn ores (Percolation) Aq. SO₂</td>
<td>Size 1.3–2.5 cm 1.5%-sat. [SO₂] 15–20 days</td>
<td>Rate depends on [SO₂] and pH &gt;90% Mn recovery</td>
<td>[43, 61, 8]</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Component</th>
<th>Grade (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>MnO₂</td>
<td>56.31</td>
</tr>
<tr>
<td>SiO₂</td>
<td>21.16</td>
</tr>
<tr>
<td>Al₂O₃</td>
<td>7.56</td>
</tr>
<tr>
<td>BaO</td>
<td>3.92</td>
</tr>
<tr>
<td>CaO</td>
<td>2.80</td>
</tr>
<tr>
<td>MgO</td>
<td>1.80</td>
</tr>
<tr>
<td>K₂O</td>
<td>1.22</td>
</tr>
<tr>
<td>Fe₂O₃</td>
<td>1.08</td>
</tr>
<tr>
<td>Na₂O</td>
<td>0.16</td>
</tr>
<tr>
<td>P₂O₅</td>
<td>0.04</td>
</tr>
<tr>
<td>Pb</td>
<td>2.04</td>
</tr>
</tbody>
</table>
2.2 Theoretical considerations

The Eh-pH diagrams are shown in (Fig:2:3). The S-H2O system has been plotted without considering the sulfate species in order to be able to take account of the presence of metastable species (under ambient conditions) of importance in the leaching process, such as S2O3, SO3 and HSO3, generated by the oxidation and ionization of SO2·H2O [46].

Figures 2.3 and 2.4 were traced by free Software “ChimGéné v1.3”. Examination of the Eh-pH diagram (Fig:2:3) for the Mn H2O system reveals that MnO2 is very stable both in acid and alkaline solutions. To dissolve it, therefore, the environment must be reducing, so as to attain the region of stability of the manganous ion. Indeed, in the presence of sulphur dioxide, MnO2 is attacked rapidly with the formation of manganese sulphate:

\[
MnO_2(s) + SO_2(aq) \rightarrow Mn^{2+} + SO_4^{2-} \tag{2.1}
\]

\[
MnO_2(s) + HSO_3^- \rightarrow Mn^{2+} + SO_4^{2-} + H_2O \tag{2.2}
\]

By superimposing the Eh-pH diagrams of the SO2-H2O and Mn-H2O systems, the stability region of manganous ion can be readily outlined in the reaction system. Ionization of the hydrogen sulfite is negligible at pH=5 or less. When the concentrations of the species derived from the dissociation of the acid SO2·H2O in water are plotted as a function of pH, for a total predetermined concentration of the acid. The distribution curves for the SO2-H2O system are illustrated in (Fig:2.4).
2.3 Apparatus and procedures

All leaching experiments were carried out in a glass reactor double jacket equipped with a magnetically stirrer, condenser, thermometer, openings for adding the solid sample and a sampling device. This set-up provides stable hermetic conditions and allows heating at constant temperature.

The calculated quantities of H$_2$SO$_4$ and Na$_2$SO$_3$ were added to the glass reactor and heated up to the selected temperature. When the temperature was reached and stirring speed was set, the solid (sample of residue) was added and the reaction commenced. After selected time intervals, the solution samples were taken for chemical analysis, which was carried out by UV-vis spectroscopy (Hach DR-5000) and AAS (Perkin Elmer).

Stirring was provided in 500 rpm, temperatures of 25 to 40 °C, leaching times of 1 to 15 min, while the particle size fraction leached was -630 µm. The H$_2$SO$_4$ and Na$_2$SO$_3$ concentrations were in the range of 1 – 3 M and 0.32 – 1.0 M, respectively. The solid/liquid ratio was 67 -200 g concentrate in 1000 ml of the solution.

3 Results and discussion

3.1 Experimental design

Response surface methodology (RSM) is a collection of statistical and mathematical methods that are useful for the modeling and analyzing engineering problems. In this technique, the main objective is to optimize the response surface that is influenced by various process parameters.

Response surface methodology also quantifies the relationship between the controllable input parameters and the obtained response surfaces [35]. The design procedure of response surface methodology is as follows [36, 37]:

1) Designing a series of experiments for adequate and reliable measurement of the response of interest.

2) Developing a mathematical model of the second order response surface with the best fittings.

3) Finding the optimal set of experimental parameters that produce a maximum or minimum value of response.

4) Representing the direct and interactive effects of process parameters through two and three dimensional plots.

If all variables are assumed to be measurable, the response surface can be expressed as follows:

\[ Y = f(x_1, x_2, x_3, \ldots, x_k) \] (3.1)

where \( Y \) is the answer of the system, and \( x_i \) the variables of action called factors.

The goal is to optimize the response variable \( y \). It is assumed that the independent variables are continuous and controllable by experiments with negligible errors. It is required to find a suitable approximation for the true functional relationship between independent variables and the response surface. Usually a second-order model is utilized in response surface methodology [35, 37]. In this study, the Box–Behnken experimental design was chosen for finding out the relationship between the response function (metal extracted \( Y_{Mn\%} \)) and variables \([H_2SO_4], [Na_2SO_3] \) and S/L).

Box–Behnken design[38, 39] is rotatable second-order designs based on three-level incomplete factorial designs. The special arrangement of the Box–Behnken design levels allows the number of design points to increase at the same rate as the number of polynomial coefficients. For three factors, for example, the design can be constructed as three blocks of four experiments consisting of a full two-factor factorial design with the level of the third factor set at zero [39].

Box–Behnken design requires an experiment number according to \( N = k^2 + k + cp \), where \( k \) is the factor number and \( (cp) \) is the replicate number of the central point [39]. It has been applied for optimization of several chemical and physical processes [40, 41]. For the three-level three-factorial Box–Behnken experimental design, a total of 15 experimental runs, shown in (Tab.3) are needed.
The experimental plan of the leaching experiments by sulphite based on a Box-Behnken design is presented in (Tab:4). In this table, each row indicates the experimental condition of a leaching experiment. The leaching experiments were carried out in random order to avoid noise sources which had not been considered initially and which could occur during an experiment and negatively affect the results.

The responses at any condition in the interval of our experiment design could be calculated from (Eq:3.2). Therefore, the predicted contour plots are given in (Fig:3.1). The graphic analysis (Fig:3.1(S/L.Red)) show that the Na$_2$SO$_3$ concentration and the liquid/solid ratio (S/L) were very meaningful for the dissolution of manganese. However, (Figs. 3.1(S/L.acide); (Red .Acide)) shows the limited effect of the acid in the process of dissolution of MnO$_2$.

3.2 Statistical analysis

ANOVA analysis and the mean response calculation were performed to evaluate the effect of each factor on the optimization criteria. The main objective of ANOVA is to extract from the results how much variation each factor causes relative to the total variation observed in the rate overall manganese extraction.

For statistical analysis of the results, a mathematical function may be needed to apply to the results to meet the assumptions that makes the ANOVA valid. For this purpose, a quadratic function was considered as the best transform to be applied to the results of leaching rate. No transform was needed on the results of overall manganese extraction.
Where $Y$: the percentage of metal extracted, $\beta$: model coefficients, $x$: dimension-less coded factors for Na$_2$SO$_3$ concentration, Solid/Liquid ratio (S/L), sulphuric acid concentration and $\epsilon$ error term. The coefficients, the main effect (bi) and two factors interactions (bij) have been estimated from the experimental results by computer simulation programming applying least square method using software MINITAB.

The results of ANOVA analysis for manganese extraction are presented in (Tab.5). In order to eliminate the zero degree of freedom (DOF) from the error term, the pooled ANOVA was applied. Control factors with the least contribution percent were pooled.

According to this analysis, within the 95% confidence interval, pulp density, Na$_2$SO$_3$ concentration and acid concentration were the most significant factors affecting the manganese dissolution in decreasing order. Their contributions were 49.6%, 47.4% and 3% on manganese extraction, respectively.

![Diagram curves iso-response for $Y_{Mn}$](image)

$$Y = \beta_0 + \sum_{i=1}^{n} \beta_i x_i + \sum_{i=1}^{n} \sum_{j=1}^{n} \beta_{ij} x_i x_j + \epsilon$$  \hspace{1cm} (3.2)
Therefore, all of the factors in the model including pulp density, Na$_2$SO$_3$ and H$_2$SO$_4$ concentration, showed the statistically meaningful effect on manganese extraction (Tab.5). However, the effect of H$_2$SO$_4$ concentration (F = 4.67) on the reaction was not statistically meaningful. From the statistical results obtained, it was shown that the developed models Eq.(3.2) were adequate to predict the desired responses in the range of variables under study. The value of correlation coefficient ($R^2$) between the predicted and observed data were 0.995 for the models of manganese extraction (Fig:3.3). The main and interaction coefficients are evaluated and tested for significance by the Analysis of Variance. The coefficients significant at more than 95% confidence level on extraction of manganese are plotted in (Tab.6).

The chart (a) and the Pareto plots (b) (Fig:3.2) allow to look at both the magnitude and the importance of an effect. This chart displays the absolute value of the effects, and draws a reference line on the chart. Any effect that extends past this reference line is potentially important. The results indicate that S/L and Na$_2$SO$_3$ are significant at the 0.05 $\alpha$-level. The interactions are not significant at the 0.05 $\alpha$-level. The normal and Pareto plots of the effects allow to visually identify the important effects and compare the relative magnitude of the various effects. The plots confirm that S/L and Na$_2$SO$_3$ are significant at the 0.05 $\alpha$-level. The adequation of Eq.(3.2) was tested by ANOVA, to see how it fitted the observations. For $\alpha=0.05$ (95% confidence level), the estimated regression Eq.(3.2) fit the experimental data adequately, see (Fig:3.3).

**Tab. 6: Test of significance of main and interaction coefficients**

<table>
<thead>
<tr>
<th>Term</th>
<th>Coef</th>
<th>SE Coef</th>
<th>T_value</th>
<th>P_value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant</td>
<td>58.00</td>
<td>0.0083</td>
<td>57.523</td>
<td>0.000</td>
</tr>
<tr>
<td>$[H_2SO_4]$</td>
<td>6.75</td>
<td>0.6175</td>
<td>10.932</td>
<td>0.000</td>
</tr>
<tr>
<td>$[Na_2SO_3]$</td>
<td>22.62</td>
<td>0.6175</td>
<td>36.642</td>
<td>0.000</td>
</tr>
<tr>
<td>S/L</td>
<td>-23.12</td>
<td>0.6175</td>
<td>-37.452</td>
<td>0.000</td>
</tr>
<tr>
<td>$[H_2SO_4]^2$</td>
<td>1.50</td>
<td>0.9089</td>
<td>1.650</td>
<td>0.160</td>
</tr>
<tr>
<td>$[Na_2SO_3]^2$</td>
<td>-18.75</td>
<td>0.9089</td>
<td>-20.630</td>
<td>0.000</td>
</tr>
<tr>
<td>(S/L)$^2$</td>
<td>6.25</td>
<td>0.9089</td>
<td>6.877</td>
<td>0.001</td>
</tr>
<tr>
<td>$[H_2SO_4] \times [Na_2SO_3]$</td>
<td>3.75</td>
<td>0.8732</td>
<td>4.294</td>
<td>0.008</td>
</tr>
<tr>
<td>$[H_2SO_4] \times (S/L)$</td>
<td>1.25</td>
<td>0.8732</td>
<td>1.431</td>
<td>0.212</td>
</tr>
<tr>
<td>$[Na_2SO_3] \times (S/L)$</td>
<td>-4.50</td>
<td>0.8732</td>
<td>-5.153</td>
<td>0.004</td>
</tr>
</tbody>
</table>

![Fig. 3.3](image.png)

**Fig. 3.3:** Correlation between $Y_{Meas}$ (measured) vs. $Y_{Calc}$ (calculated): testing the adequacy of Eq.(3.2).
3.3 Effect of parameters reaction

Stirring speed, solid/liquid ratio and particle size of manganese residue is selected as process variables to investigate their effects on the dissolution level of pyrolusite. In the experiments, while the effect of one parameter was studied, the values of other parameters were kept constant.

3.3.1 Effect of stirring speed

The effect of the stirring speed on the dissolution rate of pyrolusite was investigated at 0, 100, 300, 750 and 1000 rpm. The dissolution curve was given in (Fig.3.4). It can be seen from the (Fig.3.4) that the dissolution level of the process increases with increase in the stirring speed rate until about 500 rpm. The dissolution rate of pyrolusite remained almost constant at stirring speed of between 500 and 1000 rpm. Because of this, the stirring speed rate of 500 rpm was as constant value in all experiments to get guaranteed to obtain homogeneity in the batch reactor.

Fig. 3.2: Significant main and interaction terms for manganese extraction. (a) the Pareto chart. (b) the normal and Pareto plots.
3.3.2 Effect of solid/liquid ratio

The effect of solid/liquid ratio on the dissolution rate of pyrolusite was investigated by varying ratio to 80, 100, 120, 130, 160 and 180 g/L. The dissolution curve was given (Fig.3.5). It can be seen from (Fig.3.5) that, the dissolution rate decreases with increasing solid/liquid ratio. This situation can be explained by the decrease in the number of pyrolusite particles per amount of solutions.

3.3.3 Effect of particle size

The effect of particle size was studied by treating four sizes of fractions of this mineral, namely -630, -280, -125 and -63 µm. The dissolution curves are presented in (Fig.3.6). As can be seen from (Fig.3.6), as the particle size decreases the dissolution rates increased because of increasing surface area. it must also be noted that the effect of particle size is remarkably low.

3.4 Kinetic analysis

Kinetic modeling yields comprehensive information regarding leaching mechanisms. In fact, reactions involved in this process are heterogeneous in nature involving mass transport of reactant and product ions. In acidic leaching, the heterogeneous non-catalytic reaction for most manganese ore might be kinetically interpreted by using the shrinking core model (SCM) [47, 48].
In the SCM model, the solid reactant is considered as non-porous particle and is initially surrounded by a fluid film through which mass transfer occurs between the solid particle and the bulk of the fluid. As the reaction proceeding, an ash/inert layer forms around the unreacted core. Detailed derivation of the shrinking core model can be found in [44].

The dissolution of pyrolusite can be expressed as follows:

\[ A(\text{fluid}) + bR(\text{solid}) \rightarrow \text{fluid products} \]  

(3.3)

The rate-limiting step, which decides the form of the rate equation, may be one of the following three steps:

1. diffusion through the liquid film surrounding a solid particle,
2. diffusion through the ash/inert solid layer,
3. chemical reaction on the surface of the unreacted core.

The simplified equations of the shrinking core model when liquid film diffusion, ash/inert solid layer diffusion or the surface chemical reactions is the slowest step can be expressed as follows, respectively [44]:

\[ k'f, kd \text{ and } kr \text{ are calculated from Eq.(3.4), Eq.(3.5) and Eq.(3.6), respectively.} \]

To obtain the leaching kinetic equation, the experimental data in Figs.(3.7),(3.8) and (3.9) were transformed and fitted to Eqs.(3.4),(3.5) and (3.6). The degree of the explanation of these models on the kinetic data was evaluated using correlation coefficient ($R^2$) values. The slopes of these plots were used as the apparent rate constants ($k'f$; kd and kr).

Comparing to the reaction models discussed above, a new variant of the shrinking core model suggested by Dickinson and Heal [49], provided the best fit to the kinetic data.

Based on this model, the interfacial transfer and diffusion across the product layer both affect the reaction rate. Equation of this model is given as follows:
\( \frac{1}{(1-x_B)^{1/3}} - 1 + \frac{1}{3} \ln(1-x_B) = k_m t \)  

(3.7) Where \( x_B \) is the reacted fraction of pyrolusite, \( k_m \) is the apparent rate constant and \( t \) is the reaction time.

**Fig. 3.7: Effect of \( H_2SO_4 \) concentration on leaching rate, \([Na_2SO_4] = 0.5M, S/L = 75, 298^\circ K\)**

**Fig. 3.8: Effect of \( Na_2SO_4 \) concentration on leaching rate, \([H_2SO_4] = 2M, L/S = 13.3, 298^\circ K\)**

**Fig. 3.9: Effect of temperature on leaching rate, \([Na_2SO_4] = 1M, [H_2SO_4] = 1.5M, S/L = 75\)**
As can be seen in (Tab:7), the diffusion-controlled model better fitted the kinetic data in almost all of the leaching experiments compared to the reaction-controlled model. Comparing the results of the diffusion-controlled model, Eq.(3.5), with the model, including both interfacial transfer and diffusion effects, Eq.(3.7), it is clear that the latter model better fitted the kinetic data in all of the leaching experiments.

The variation of Eq.(3.7) with time is plotted for acid concentration, sulphite concentration, solid/liquid ratio and reaction temperature, in Figs.(3.11),(3.12), (3.13),(3.14), respectively. Using the interfacial transfer and diffusion model, the $(km)$ values were plotted versus parameters difference.
Fig. 3.11. Relationship between \([1 - x]^{-1/3} - 1\) and leaching time for various \(H_2SO_4\) concentrations. \([Na_2SO_3] = 0.5M; 298^\circ K; S/L = 75 g/L\).

Fig. 3.12. Relationship between \([1 - x]^{-1/3} - 1\) and leaching time for various \(Na_2SO_3\) concentrations. \([H_2SO_4] = 2M; 298^\circ K; S/L = 75\).

Fig. 3.13. Relationship between \([1 - x]^{-1/3} - 1\) and leaching time for various solid/liquid ratio \([H_2SO_4] = 1M; [Na_2SO_3] = 1M; 298^\circ K\).
The high linearity between \((km)\) and acid concentration, sulphite and temperature is seen in Figs.(3.11), (3.12), (3.14) and (3.5) also shows the regression coefficient \((R^2)\) to be was found as 0.99.

\[
k = A \exp\left(\frac{E_a}{RT}\right)
\]  

(3.8)

The plot of \(\ln(k_m)\) versus \((1/T)\) data for the temperatures is linear (Fig.3.15). The apparent activation energy \((E_a)\) was, hence, determined to be \((54.21 \pm 4.16)\) kJ/mol. The value of the activation energy is high, probably because the dissolution rate of pyrolusite is controlled by the diffusion and by the mass transfer through the product layer, these two mechanisms both to control the reaction kinetics.

To decide the apparent reaction order with respect to reagent concentration, the \((km)\) values for each \(H_2SO_4\) concentration and \([Na_2SO_3]\) and solid/liquid ratio were determined from Figs.(3.16); (3.17); (3.18) and the plots of \(\log(km)\) versus \(\log([H_2SO_4])\), \(\log([Na_2SO_3])\) or \(\log(S/L)\) were obtained. The order of reaction was found be 0.8 with respect to \(H_2SO_4\) concentration and 1.9 with respect to \(Na_2SO_3\) and -2.9 for solid/liquid ratio. It seems that the leaching rate of manganese depends more on the concentration of sulphite and solid/liquid ratio.

According Eq.(3.7), the apparent rate constant \(k_m\) can be expressed as follows:

\[
k_m = k_0[H_2SO_4]^{0.8}[Na_2SO_3]^{1.9}(S/L)\exp\left(-\frac{54210}{RT}\right)
\]  

(3.9)
and 

\[ k_0 = 3.07 \times 10^4 \text{ min}^{-1} \text{ (mol/L)}^{-2.7} \text{ (g/L)}^{2.9} \]

as calculated from the provided data in (Fig:(3.15)).

By the above analysis, the kinetic model of pyrolusite leaching by \( \text{Na}_2\text{SO}_3 \) in sulphuric acid medium is:

\[
(1-x)^{-1/3} - 1 + \frac{1}{3}\ln(1-x) = 3.07 \times 10^4 [\text{H}_2\text{SO}_4]^{0.8}[\text{Na}_2\text{SO}_3]^{1.9} (S/L)^{-2.9} \exp\left(-\frac{54210}{RT}\right) \cdot t 
\]

To test the agreement between the experimental conversion and the values calculated from the semi-empirical model, the graph of \( X_{\text{exp}} \) versus \( X_{\text{cal}} \) was plotted, as shown in (Fig.3.19). It is observed that the agreement between the experimental and the calculated values is very good.

![Graph](image1)

**Fig. 3.16:** Determination of reaction kinetic order for pyrolusite dissolution with respect to \( \text{H}_2\text{SO}_4; [\text{Na}_2\text{SO}_3] = 0.5M; 298^\circ K; S/L=75.\)

![Graph](image2)

**Fig. 3.17:** Determination of reaction kinetic order for pyrolusite dissolution with respect to \( \text{Na}_2\text{SO}_3; [\text{H}_2\text{SO}_4] = 2M; S/L=75.\)
4 Conclusions

The kinetic factors of the dissolution of a low grade manganese ore in H\textsubscript{2}SO\textsubscript{4}/Na\textsubscript{2}SO\textsubscript{3} solutions were evaluated and optimized using a response surface methodology (RSM) and a Box-Behnken design. The statistical analysis performed in this study has enhanced the interpretation of kinetic data collected during the leaching studies. From the results of these studies the following conclusions can be made:

- Pulp density, Na\textsubscript{2}SO\textsubscript{3} concentration and [H\textsubscript{2}SO\textsubscript{4}] were respectively the most significant factors affecting both the pyrolusite reaction rate and the manganese extraction in the confidence interval of 95%. Their contributions were 49%, 47% and ~3% on manganese extraction, respectively.

- The kinetic data best fitted a shrinking core model, in which both the interfacial transfer and diffusion through the product layer affect the reaction rate. Manganese extraction of 95% was obtained after 10 min of leaching. A proper semi-empirical mathematical model expresses the dissolution rate:

\[
\begin{align*}
[(1-x)^{-1/3} - 1] + \frac{1}{3}ln(1-x) &= 3.07 \cdot 10^4 \cdot [H_2SO_4]^{0.8} \cdot [Na_2SO_3]^{-1.9} \cdot (S/L)^{-2.9} \cdot exp\left(\frac{-54210}{RT}\right) \cdot t
\end{align*}
\]

- The activation energy of 54.2 kJ/mol was calculated for pyrolusite dissolution in by Na\textsubscript{2}SO\textsubscript{3} in sulphuric acid medium, the kinetics study also shows strong dependence on acid, sulphite concentration and S/L with a reaction order of 0.8 for total H\textsubscript{2}SO\textsubscript{4} concentration and a reaction order of 1.9 for Na\textsubscript{2}SO\textsubscript{3} and finally -2.9 for solid / liquid ratio.
5 References


