Reliability Analysis of Circuit Breakerin the Nigerian 330-kV Transmission Network.

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Abstract— This paper is concerned with using the fault analysis to establish the requirements for the proper selection of circuit breaker; A Case Study of Power Holding company of Nigeria (PHCN) 330-kV Transmission Grid System. The work is modelled for Fault Analysis and it is written in a flexible MATLAB programs to accommodate addition or reduction in the Transmission Grid System. It aimed at establishing the Circuit Breaker Capacity at any point in the system. The result is then compared with the existing circuit breaker capacity of PHCN 330-kV system. The short-circuit fault is simulated by combining a solution of algebraic equations describing the changes in the network with a numerical solution of the differential equations. Two MATLAB programs were written and simulated; one for Lord Flow study to know the pre-fault bus voltages based on Gauss-Seidel Method; the other for Short Circuit Studies which made use of Thevenin's theorem application. The highest Circuit Breaker Capacity established by the result of this study is relatively lower and the investments needed for this are smaller compared with the normal practice with PHCN system. This reveals that PHCN system can be protected with this low capacity circuit breaker with a reduced cost effectiveness and equal sensitivity which is a break-through in terms of Circuit Breaker Capacity in the field of power system protection.

Keywords— Fault studies, circuit breaker, 330kV transmission grid, MATLAB program, Gauss Seidel load flow solution

I. INTRODUCTION

The current trends of erratic power supply and system collapse in Nigeria have made this study a paramount importance to the nation's power industry. The purpose of an electrical power system is to generate and supply electrical energy to consumers with reliability and economy. The operation of a power system is affected by disturbances that could be due to natural occurrences such as lightning, wind, trees, animals, and human errors or accidents. These disturbances could lead to abnormal system conditions such as short circuits, overloads, and open circuits. Short circuits, which are also referred to as faults, are of the greatest concern because they could lead to damage to equipment or system elements and other operating problems including voltage drops, decrease in frequency, loss of synchronism, and complete system collapse. There is, therefore, a need for a device or a group of devices that is capable of recognizing a disturbance and acting automatically to alleviate any ill effects

on the system element or on the operator. Such capability is provided by the protection system. The protection system is designed to disconnect the faulted system element automatically when the short circuit currents are high enough to present a direct danger to the element or to the system as a whole. The objective of the system will be defeated if adequate provision for fault clearance is not made. The installation of switchgear alone is insufficient, discriminative protective gear, designed according to the characteristics and requirements of the power system must be provided to control the switchgear [1]. Security of supply, therefore, can be better by improving plant design, increasing the spare capacity margin and arranging alternative circuits to supply loads. Majority of the faults are unsymmetrical. However, the circuit breaker rated MVA breaking capacity is based on 3phase fault MVA. Since a 3phase fault inflicts greatest damage to the power system, except in a situation where a single line to ground fault is very close to a solidly grounded generator's terminal. In this instance the severity of single line to ground fault is greater than that of 3phase balance fault.

II. BRIEF REVIEW OF SHORT-CIRCUIT ANALYSIS

Fault studies form an important part of power system analysis. In the context of electrical fault-calculation, a power system fault may be defined as any condition or abnormality of the system which involve the electrical failure of the primary equipment, the primary equipment implying equipment such as generators, transformers, busbars, overhead lines and cables and all other items of plant which operate at power system voltage (330kV for this case).

Faults on power system are divided into three-phase balanced faults and unbalanced faults. The different types of unbalanced faults are single line-to-ground fault (LG), line-to-line fault (LL), and double line-to-ground fault (LLG). The problem consists of determining the voltages and currents during various types of faults. The information gained from fault studies are usedfor proper relay setting and coordination. The three-phase balanced fault (LLL) information is used to select and set phase relays.

Majority of the faults are unsymmetrical and the current which a breaker must interrupt is usually asymmetrical since it still contains some of the decaying dc component [2]. However, the circuit breaker rated MVA breaking capacity is based on three-phase balanced fault MVA. Since a three-phase fault inflicts greatest damage to the power system, except in a situation where LG fault is very close to a solidly grounded generator's terminal. In this instance the severity of single line to ground fault is greater than that of three-phase balanced fault.

The condition of the power system during the fault condition can be explained from the equation for short circuit studies. The equation for the short circuit uses the sequence components theory in the method of calculation.

In an attempt to establish short circuit studies, various forms of faults were simulated to obtain the current which the breaker must interrupt and comparison was made between LLL fault and LG fault either of which is likely to cause greater damage to a power system. This current is properly called the required symmetrical interrupting capacity or simply the rated symmetrical short-circuit current. [3]

III. PROBLEM FORMULATION (LOAD REPRESENTATION)

During sub-transient period, power system loads, other than motors are represented by the equivalent circuit as static impedance or admittance to ground. The symmetrical three phase fault current in per unit is given by

$$I_K(F)pu = \frac{V_K(0)}{X_{KK}}$$
 (1)
Where $V_K(0)$ is the per unit Perfault bus voltage and $X_{KK} =$

the p.u reactance to the point of Fault

The base current
$$I_B = \frac{S_B \times 10^3}{\sqrt{3}V_B}$$
 (2)
Where S_B is the base MVA and V_B is the line to line base

The interrupting rating of a circuit breaker was specified in KVA or MVA.

From (2), it implies that the interrupting KVA equal $\sqrt{3}$ times the kV of the bus to which the breaker is connected times the current which the breaker must be capable of interrupting when its contact part. This current is of course, lowers than the momentary current and depends on the speed of the breaker [2].

Also, for the purpose of short circuit analysis in order to select appropriate circuit breaker to clear a fault instantly before transient condition on a power system, pre-fault condition of the system (i.e, pre-fault voltages and currents) should be known and this can be obtained from the load flow solution for the power system. Detail of the initial value of the current for a constant current representation is obtained from model of fig 1.

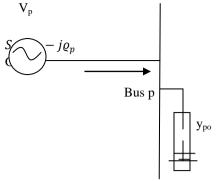


Figure 1: A typical fault model at bus P

$$I_{po} = \frac{P_p - jQ_p}{V_p^*} \tag{3}$$

Where; P_p and Q_p = the scheduled bus load.

 $V_{P}=% \frac{\partial V_{P}}{\partial t}$ the calculated voltage which can only be determined if Q_{ip} is given or known

The injected current Ipo flows from bus P to ground, that is, to

The magnitude and power factor angle of Ipo remain constant.

$$y_{po} = \frac{I_{po}}{V_p}.$$

NETWORK PERFORMANCE EQUATION

The Gauss-Seidel Method of solution used for the load flow equation can be applied to describe the performance of a network during a sub-transient period, using the bus admittance matrix with ground as reference. The voltage equation for bus P is given by:

$$V_{p} = \frac{(P_{p} - jQ_{p})L_{p}}{V_{p}^{*}} - \sum_{q=1}^{p-1} YL_{pq}V_{q}^{k+1} - \sum_{q=p+1}^{n} YL_{pq}V_{q}^{k}...(5)$$

where;
$$YL_{pq} = Y_{pq}L_p; L_p = \frac{1}{Y_{pp}}$$

The term
$$\frac{\left(P_{p}-jQ_{p}\right)}{V_{p}^{*}}$$
 in equation (5) represents the load current at bus P.

for the cons tantload current representation,

$$\frac{P_{p} - jQ_{p}}{(V_{p}^{k})_{p}^{k}} = |I_{po}| < (\omega_{p}^{k} + \varphi_{p})....(6)$$

where; ϕ_n = the power factor angle,

and $\omega_{\scriptscriptstyle p}^{\scriptscriptstyle p}$ = the angle of voltage with respect to the reference.

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When the constant power is used to represent the load, (P_p – jQ_p) L_p will be constant but the bus voltage V_p will change in any iteration [4]. When the load at bus P is represented by a static admittance to ground, the impressed current at the bus is

$$\frac{\left\langle P_{p} - jQ_{p}\right\rangle L_{p}}{V_{p}^{*}} = 0 \tag{7}$$

For a sub-transient analysis in short circuit studies, the parameters of equation (5) must be modified to include the effect of the equivalent element required to represent synchronous, induction and loads. The line parameters YL_{pq} must be modified for the new elements and additional line parameter must be calculated for each new network element.

V. METHOD OF SOLUTION

The methods and concepts employed to implement this work includes:

- Developing an algorithm and hence a programme for fault level calculation at the location of fault in a 330-kV transmission Grid
- Determine the fault current for various types of fault simulation.
- Recommend the appropriate circuit breaker capacity to clear any detected fault.

Note that it is necessary to do a load flow calculation before one can proceed on fault analysis. This is important so as to know the pre-fault voltages and currents necessary for further calculation. The network representation for the short circuit studies includes among other things, the Grid components parameter i.e the generators system buses, transmission lines and transformers. Modification of the admittance matrix to impedance matrix is done on the load flow calculation [4] to reflect fault analysis.

These pre-fault conditions can be obtained from the result of load flow solution by Gauss-Seidel iteration method using Y_{BUS}, the flowchart of which is illustrated in Fig.2.

The pre-fault machine currents are calculated from load flow by Gauss-Seidel iterative method from:

$$I_{ki} = \frac{P_{ki} - jQ_{ki}}{V_{ki}^*}; i = 1, 2, \dots, m.$$
 (8)

where;

 P_{ki} and Q_{ki} = the scheduled or calculated machine real and representational factories at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and representations at the scheduled or calculated machine real and the scheduled at the scheduled machine real and the scheduled machi

 V_{i}^{*} = the last iteration voltage.

m = the number of machines in the system.

The network is then modified to correspond to the desired representation for short circuit studies. Being a linear network of several voltage sources, further calculation can be computed by application of Thevnin's theorem [5].

$$I^{f} = \frac{V^{\circ}}{jX_{TH}^{\circ} + Z^{f}} \dots (9)$$

VI. COMPARISON OF SLG FAULT AND THREE-PHASE FAULT (LLL) CURRENTS

This comparison[5]is necessary because of the earlier statement in this project study that single line-to-ground fault is more severe than that of 3-phase fault if the fault is located very close to the terminal of a solidly grounded generator.

The fault impedance can be assumed to be zero because of the enormous effect of the fault current. In addition, if the impedances Z_1 , Z_2 and Z_0 are assumed to be pure reactances $(X_1, X_2 \text{ and } X_0)$, then for a 3-phase fault.

$$I_a = \frac{E}{jX_1} \tag{10}.$$

and that of $\sin gle line - to - ground$ fault is given as;

$$I_a = \frac{3E}{jX_1 + jX_2 + jX_0}$$
....(11).

The three practical possibilities are as follow;

- Fault at the terminals of neutral solidly grounded generator, (for generator $X_0 << X_1$), and it is assumed that $X_1 = X_2$ for sub-transient condition which is the case for the short circuit studies. At this instance single line -to-ground fault is more severe than a 3-phase fault
- ii. If a generator is grounded through a reactance X_n, this does not have any effect on a 3-phase fault current, but a single line-to-ground fault will have current:

$$I_a = \frac{3E}{j(X_1 + X_2 + X_0 + 3X_n)}$$

to this end the relative severity of 3-phase fault and single line-to-ground fault will depend on the value of X_n.

For a fault on a transmission line (which is the case study) $X_0 >> X_1$ so that for a fault on a line sufficiently far away from the generator

single line-to-ground fault current.

iii.

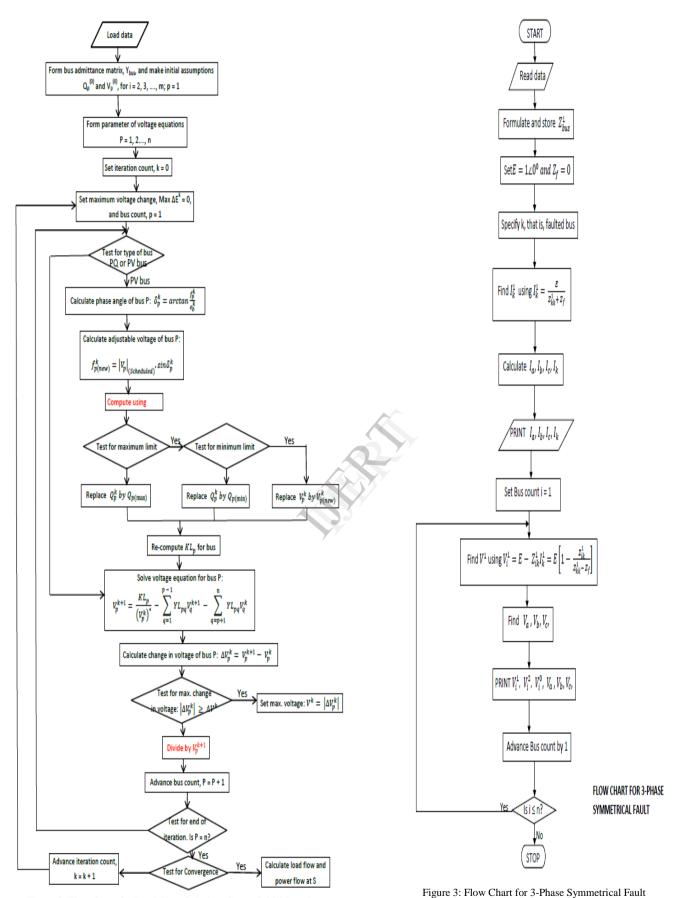


Figure 2: Flow Chart for Load-Flow Solution: Gauss-Seidel Iteration

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VII. RESULT OF SYSTEM MODELING

There is a necessity to have the knowledge of pre-fault voltages and currents in order to proceed with the calculation of the fault currents and hence achieving the aims of the research study. Hereunder are one-line diagram of the existing National 330-kV Network (Fig.4) and the systems data(Table) employed in the load flow calculation:

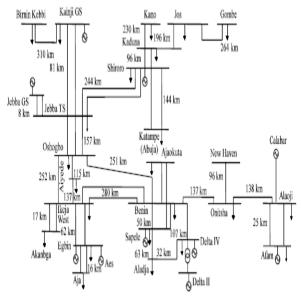


Figure 4: The 28-Bus System of the Nigerian Transmission 330-kV Grid as a Case Study [6]

Table 1: Transmission line data on 33kV, 100MVA base (All values are in per unit) [7]

BU	В	FRO	TO	LENG	R(X(ADMIT
S -	U	M	BUS	TH(km	pu)	pu)	TANCE
NO	S	BUS)			
FR	-						(b/2)
О	N						
M	О						
	T						
	О						
1	2	Alao	Afam	25	0.0	0.0	0.104
		ji			09	07	
1	4	Alao	Onitsha	138	0.0	0.0	0.524
		ji			49	42	
3	4	New	Onitsha	96	0.0	0.0	0.365
		Have			03	29	
		n				2	
4	6	Onits	Okpai	80	0.0	0.0	0.104
		ha			09	07	
5	4	Beni	Onitsha	137	0.0	0.0	0.521
		n			04	41	
					9	6	
5	7	Beni	Ajaokut	195	0.0	0.0	0.745
		n	a		07	56	
5	10	Beni	Sapele	50	0.0	0.0	0.208
		n			01	13	
					8	9	
5	11	Beni	Delta	107	0.0	0.0	0.239
		n			02	19	

5	14	Beni n	Omotos ho	120	0.0	0.0 36	0.228
5	18	Beni	Oshogb	251	0.0	5	0.954
		n	0		08 9	76 3	
10	8	Sape le	Aladja	63	0.0 02 3	0.0 19	0.239
11	8	Delta	Aladja	32	0.0 02 3	0.0 19	0.239
12	5	Ikeja	Benin	280	0.0 10 0	0.0 77 9	1.162
12	9	Ikeja	Aiyede	137	0.0 04 9	0.0 41 6	0.521
12	13	Ikeja	Papanlat o	30	0.0 01 1	0.0 09 1	0.057
12	14	Ikeja	Omotos ho	160	0.0 05 7	0.0 48 6	0.304
12	15	Ikeja	Akangb a	18	0.0 02 2	0.0 17 2	0.257
12	17	Ikeja	Egbin	62	0.0 02 2	0.0 17 2	0.257
12	18	Ikeja	Oshogb o	252	0.0 04 9	0.0 41 6	0.521
13	9	Papa lanto	Aiyede	60	0.0 02 1	0.0 18 2	0.114
17	16	Egbi n	Aja	14	0.0 02 2	0.0 17 2	0.257
18	9	Osho gbo	Aiyede	115	0.0 04 1	0.0 34 9	0.437
18	27	Osho gbo	Jebba(T S)	157	0.0 05 6	0.0 47 7	0.597
20	21	Kadu na	Kano	230	0.0 08 2	0.0 69 9	0.874
20	23	Kadu na	Jos	197	0.0 07 0	0.0 59 9	0.748
20	24	Kadu na	Shiroro	96	0.0 03 4	0.0 29 2	0.364
23	22	Jos	Gombe	265	0.0 09 5	0.0 81	1.01
24	25	Shiro	Katamp	144	0.0	0.0	0.598

	1	ro	e(Abuja		05	40	
		ro	e(Abuja				
)		2	1	
24	27	Shiro	Jebba(T	244	0.0	0.0	0.927
		ro	S)		06	70	
					7	2	
26	28	Beni	Kainji	734	0.0	0.0	1.178
		n			11	94	
		Kebb			1	2	
		i					
27	19	Jebb	Jebba(T	8	0.0	0.0	0.0322
		a(GS	S)		00	02	
)			3	2	
28	27	Kain	Jebba(T	81	0.0	0.0	0.308
		ji	S)		02	24	
					9	6	

		T - 1 - 2 - 2	
16	IKEJA-WEST	-5.1500	-2.2900
17	AJAOKUTA	0.0000	0.0000
18	BENIN	-2.4000	-1.1200
19	ONITSHA	-1.0200	-0.4400
20	ALADJA	-1.5600	-0.8500
21	ALAOJI	-2.1600	-1.0400
22	NEW-HAVEN	-1.1000	-0.1800
23	AKANGBA	-3.0750	-1.5400
24	AJA	0.0000	0.0000
25	KATAMPE	0.0000	0.0000
	(ABUJA)		
26	AIYEDE	0.0000	0.0000
27	PAPALANTO	0.0000	0.0000
28	OMOTOSHO	0.0000	0.0000

Table 2; Voltage-Control Bus Data

QMA v

VSP

QMI N **BUS** NAME

S	NAME			N	X	
NO.						
		SLAC				
		K BUS				
1	KAINJI	0.0000	0.000	-	2.790	1.050
			0	2.790	0	0
				0		
2	JEBBA	0.0000	0.240	-	3.230	1.000
			0	3.230	0	0
				0		
3	SHIROR	0.0000	0.180	-	2.000	1.000
	О		0	2.000	0	0
				0		
4	SAPELE	0.0000	0.000	-	4.670	1.000
			0	4.670	0	0
				0		
5	DELTA	0.0000	0.370	-	3.430	1.000
	(IV)		0	3.430	0	0
				0		
6	AFAM	0.0000	0.000	-	36700	1.000
	(IV)		0	3670		0
				0		
7	EGBIN	0.0000	0.000	-	5.820	1.000
			0	5.820	0	0
				0		

Table 3: Load Bus Data

BUS	BUS NAME	ACTIVE	REACTIVE
NO			
		POWER (PG)	POWER (QG)
8	JEBBA (T.S)	-0.7200	-0.4300
9	BIRNIN-	-0.3900	-0.1800
	KEBBI		
10	KADUNA	-1.6100	-0.8200
11	KANO	-2.0400	-0.8000
12	JOS	-0.9800	-0.3460
13	GOMBE	-1.5300	-1.0800
14	OSOGBO	-1.5600	-0.8800
15	IBADAN	-1.8000	-0.9300

VIII. LOAD FLOW RESULTS

The bus-bar pre-fault voltage, pre-fault current and pre-fault powers, which flow out of the bus bars, are tabulated in Table 4 hereunder

Table 4; Output of Load-Flow Results (in p.u)

BUS				
NO.	VOLTAGE	POWER	POWER	CURRENT
		ANGLE	FLOW	
1	1.0500	0.0000	2.4787	2.3605
2	1.0000	-0.4060	7.2392	7.2394
3	1.0000	-8.1200	3.6954	3.6954
4	1.0000	12.9979	7.0150	7.0150
5	1.0000	13.9877	3.6998	3.6998
6	1.0000	18.2990	4.4075	4.4075
7	1.0000	2.0316	4.3869	4.3869
8	1.1219	-3.8503	0.8403	0.7443
9	1.0081	-0.6090	0.4238	0.4208
10	1.0173	-12.9984	1.8070	1.7760
11	1.0050	-21.0013	2.1898	2.1982
12	1.0601	-21.4268	1.0387	0.9522
13	1.0599	-27.4552	1.8735	1.7563
14	1.0220	-0.5700	1.7934	1.7518
15	1.0042	-2.3010	2.0273	2.0202
16	0.9899	-0.1259	5.6455	5.6960
17	1.0417	10.4510	0.0022	0.0020
18	1.0201	10.6305	1.1065	1.0860
19	1.0340	11.9994	0.4296	0.4068
20	0.9980	13.3385	1.8026	1.8015
21	1.0005	17.3005	2.4028	2.4018
22	1.0350	10.2956	1.1223	1.0764
23	0.9875	-0.5500	3.4326	3.4798
24	1.0002	2.0225	0.0164	0.0168

IX. RESULT OF SHORT CIRCUIT STUDIES

In the short circuit studies, a base current of 174.9546A and a base voltage of 330kV are computed together with the load flow output result of the pre-fault condition in the input data for the various fault current calculations using the Power System Matlab Programming.[9].

Simulations were made for different types of short circuit faults i.e, 3-phase fault; single line-to-ground fault, line-to-line fault and double line-to-ground fault. The summary of is shown in Table 5.

Fault Current Result (IN ACTUAL

VALUE)

BASE CURRENT = 1,749.546kA BASE MVA = 100MVA BASE VOLTAGE = 330kV

TABLE 5: TYPE OF FAULT (SUMMARY)

BUS				
NO.	3-	SLG.	LL.	DLG
	PHASE			
1	21878	11296	19335	19684
2	11688	4321	9897	10369
3	12082	6345	9879	9802
4	15568	8442	12680	12582
5	9157	4913	7723	7675
6	2312	1382	2255	2196
7	24989	13021	21958	22013
8	2228	1180	2012	2032
9	10012	5014	9146	8887
10	5826	2798	4988	5102
11	1895	894	1687	1698
12	1768	852	1485	1551
13	1062	598	986	993
14	8896	4140	7734	7984
15	28984	13982	24968	25437
16	21787	9603	18475	19004
17	5719	2870	4970	5042
18	20593	10143	18042	18275
19	3678	1830	3234	3290
20	9006	4367	7911	7960
21	2218	1150	2019	2050
22	2462	1146	2203	2239
23	25432	11951	22204	22597
24	20998	10246	18269	18804

From the summarized result in Table 5 above, it can be inferred that 3-phase fault causes greatest magnitude of fault current to the system and hence, should be a point of reference upon which the circuit breaker to clear faults on 330kV transmission line is based.

X. CONCLUSION AND RECOMMENDATION

To select the most appropriate size of Circuit Breaker for the Grid System, it has to be borne in mind that rated momentary current and rated symmetrical interrupting currents are required for the computation of circuit breaker ratings. Symmetrical current to be interrupted is computed by using sub-transient reactance for synchronous generators. Momentary current (rms) is then calculated by multiplying the symmetrical momentary current by a factor of 1.6 to account for the presence of D.C. offset current.

The 3-phase short circuit MVA to be interrupted can be computed as in the following equation [8]

$$MVA_{sc}(3-phase) = \sqrt{3} \times V_{pf1} \times I_{sc}$$
.

where:

 $MVA_{sc}(3-phase) = 3-phase short circuit MVA.$

 $V_{pf1} = \Pr e - fault \ line \ voltage \ in \ kV.$

 $I_{so} = Short circuit current in kA$.

If voltages and currents are in per unit values on a 3-phase basis, then.

 MVA_{sc} (3-phase) = $|V|_{pre-fault} \times |I|_{sc} \times MVA_{base}$

For example: The Short Circuit Current from the output result of the program for the short circuit studies is 29036A with a pre-fault voltage of 331.4520kV.

$$MVA_{sc}(3 - phase) = \sqrt{3} \times V_{pf1} \times I_{sc}.$$
$$= \sqrt{3} \times 330kV \times 28,971kA$$
$$= 16,559MVA$$

XI. CONCLUSION

From the above, and as a result of the research study, it can be concluded that the Circuit Breaker capacity for PHCN 330kV Transmission Grid should be 20,000MVA. The research result is a break-through in terms of Circuit Breaker Capacity in the field of Power System Protection.

The Birnin-Kebbi bus (B8) on which the receiving end voltage is higher than the sending end voltage, it is agreed upon and confirmed that the line is an open-ended one. This is what causes the abnormality. The solution to it is to connect a reactor to the line.

XII. RECOMMENDATIONS

From the Nameplate of a Sf_6 Gas Circuit Breaker (manufactured by GEC ALSTHOM T & D) on 330kV Transmission Line at the Area Transmission station in Osogbo:

Line Voltage $V_L = 362kV$,

Frequency f = 50Hz,

Short Circuit Current $I_{sc} = 40kA$

Line Current $I_L = 400A$,

Current Interruption Capacity = 3,150A.

From the above data, the capacity of the Circuit Breaker is calculated to be 25,080.09569MVA. This is too high compared with the result of this project (i.e, 20,000MVA capacity) and it will be expensive in term of cost. The higher value of 25,080.09569MVA apart from cost, it will be more insensitive to any fault detected.

It is therefore recommended that the result of this paper should be of value to PHCN in the daily operation of the National Grid.

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