

Overall Image Enhancement Through Discrete Wavelet Transform

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Abstract - In this paper, we defeat the issue of reproducing the high resolution image in view of the alteration of the image in both low and high resolution mode from a solitary input image. In order to establish the mapping relation between low and high resolution images most of the methods collect the different features in both the high and low resolution image. In order to make mapping more practicable we are implementing discrete wavelet transform in the training phase. To preserve singularity and edge we are implementing Lipschitz regularity and structure keeping constraints compared with the state of arts on standard image. Our strategy gets improvements in PSNR, SSIM and visuality.

Key words— Image super-resolution, wavelet domain, Lipschitz regularization, structure-keeping constraint

1. INTRODUCTION

Single image super resolution (SR) goes for producing a high resolution (HR) image from a low resolution (LR) image. The center piece of the SR method is to keep up the high recurrence information of the edge territory of the image to make the recreated image more honed outwardly and better in execution. As of now SR method can be generally subdivided into three classes. Interpolation based techniques utilize the linear mix of close-by known pixels to get the obscure pixels like bicubic addition, or non-linear interpolation like NEDI (new edge coordinated insertion) [1]. Reconstruction based method delineate LR images to HR images utilizing the known earlier. Neighbor embedded strategy in [2] that executes the earlier that the manifolds of LR and HR images are locally in comparative geometries and LR/HR images can be directly consolidated by the LR/HR neighbors. Learning-based method utilize machine learning systems that endeavor to take in the mapping capacity or some connection between the LR images and HR images. Edge insights are found out in [3] from normal images as angle profile earlier. A profound convolutional neural system is actualized in [4] to take in a conclusion to-end mapping between the LR and HR images. Sparse representation based techniques [5] learned coupled LR and HR word dictionaries to speak to the mapping capacity in light of sparse representation signal earlier. K-SVD/OMP is actualized in the sparse representation process which got bring down computational unpredictability and enhanced quality in [6]. The sparse representation techniques and neighborhood embedded method are joined in [7, 8]. Timofte et al [7] discover the neighbors in the inadequate sparse representation to speak to LR/HR images and utilize Ridge Regression [9] to reformulate the issue as a minimum squares relapse. Timofte et al [8] utilize the sparse

representation dictionary to discover neighbors in the preparation input rather to speak to the LR/HR images.

As of now, most SR method [5, 6, 7, 8] utilized the first and second arrangement angles of patches as the highlights for LR images and subtracted the bicubically introduced LR image from the HR image to make the highlights for HR images. We can see that the highlights for LR/HR images removed from various ways with the goal that we can't ensure the structures of these highlights in high-dimensional complex co-ordinating admirably. To tackle this issue, we actualize the wavelet change to extricate the high-recurrence parts both in LR and HR image.

Numerous single image SR method [5, 6, 10, 11] execute back projection loyalty term to enhance the underlying outcomes that are acquired from their crude techniques. Wang et al [12] and Dong et al [13] actualize nonlocal self similarity which is demonstrated without a doubt existing in characteristic images [14] to regularize the advancement issue in SR. Other than the back projection devotion term and nonlocal self-similarity limitation term, in this paper we actualize nearby Lipschitz regularity imperative and structure-keeping constraint to protect the neighborhood peculiarity and edge in our technique. We join these four terms to a general improvement strategy that fundamentally enhances the outcome contrasted and other SR method in edge-full images.

In the accompanying areas, we will first present the model of our proposed method in Section 2. At that point we clarify subtle elements of our proposed technique in Section 3, and depict our analyses in Section 4 where we contrast the execution of our strategy with other condition of-state of art method. At long last in Section 5 we conclude the paper.

2. MODEL OF WAVELET-BASED SINGLE IMAGESR METHODS

Our proposed technique expands on hypotheses from learning-based super-resolution method. So in this segment we quickly exhibit the model of our technique. What's more, the preparation and testing stages is appeared in 1.

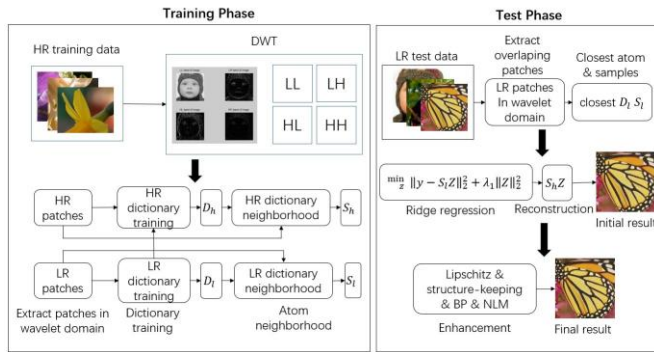


Fig. 1. Training Phase of our method

Right off the bat our technique gathers patches from the 91 training images[5] in 4 wavelet areas. At that point it utilizes a sparsity limitation to mutually prepare the LR/HR word dictionary to speak to the LR/HR patches[6] in every wavelet domains.

At that point we utilize the nearby neighborhood samples S_l of every LR word dictionary atom in every wavelet area to speak to patches with Ridge Regression. Defined underneath:

$$\min_{\alpha} \|S_l \alpha - p_l\|_2^2 + \lambda \|\alpha\|_2 \quad (1)$$

where S_l contains the K training samples that lie nearest to the dictionary atom to which the input patch p_l is coordinated, and K is a steady we have to set. The distance measure utilized for neighbor search in our strategy is the Euclidean distance.

After we get the reconstructed coefficient α , we utilize relating HR neighbor samples S_h and after that reproduce the underlying HR image patch in wavelet area. At that point we averagely include these covering HR patches and actualize reverse wavelet change to get an underlying HR image. At that point we execute back-projection fidelity term with Lipschitz regularity limitation, structure-keeping constraint and nonlocal self-similarity imperative to improve the outcome.

3. DETAILS OF PROPOSED METHOD

In this area, we show the points of interest of the preparation stage and the enhancement stage.

3.1. Training

Right now numerous techniques [5, 6, 7, 8] utilized the first and second order slopes of patches as the component for LR images. In any case, we see that every one of these highlights are restricted. These highlights can not speak to the entire high frequencies points of interest. In the mean time wavelet change is an ideal method to separate the entire nearby high frequencies points of interest and our exploratory outcomes will represent it. We actualize discrete wavelet change to the preparation LR/HR images and we can get four wavelet domains(LL,LH,HL,HH) LR/HR images, at that point gather covering patches from them. Sparse distribution are found out autonomously in every wavelet area for LR/HR images. Particularly we utilize K-SVD for the LR word dictionary in every

wavelet space and pseudo-inverse for the HR dictionary in every wavelet area, much the same as [6].

3.2. Enhancement

3.2.1. Lipschitz regularization

The neighborhood maxima of wavelet change modulus catch the sharp variety pixels of a image and their development crosswise over scales portrays the nearby Lipschitz consistency of the image. For instance, left piece of Fig.2 demonstrates a two-dimensional image and its wavelet change at a few scales. Furthermore, right piece of Fig.2 demonstrates the propagation of extrema focuses over the scales in the tenth section of the image.

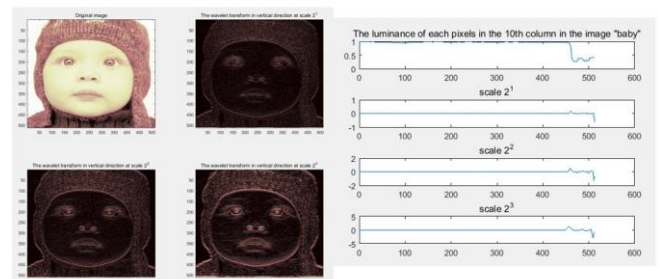


Fig. 2. Left: Pseudocolor image of Baby and its LH components of 2-D wavelet transform in three scales. Right: Propagation of extrema points across the scales for 2-D waveform in the 10th column of the image Baby

The singularities in the flag instigate crests in the wavelet change spread crosswise over scales, and the estimations of the pinnacles relating to a similar peculiarity change over the scales as indicated by an exponential capacity. Specifically, a capacity f is consistently Lipschitz α (characterized in [15]) over an interim (a,b) if and just if there exists a steady $K > 0$ to such an extent that for all $x \in (a,b)$, the wavelet change of $f(x)$ fulfills

$$|W_s f(x)| \leq K s^\alpha \quad (2)$$

The wavelet change of f at scale s and position x , signified by $W_s f(x)$. In the event that $f(x)$ is differentiable yet not consistently differentiable at x_0 , at that point it is Lipschitz $\alpha = 1$ at x_0 and the comparing wavelet change maxima carry on as $O(s)$ around x_0 . On the off chance that f is intermittent however limited in the area of x_0 , at that point $\alpha = 0$ at x_0 , and the comparing maxima stay steady over the scales. What's more, for Dirac work, $\alpha = -1$ at x_0 and the relating wavelet change maxima carry on as $O(1/s)$ around x_0 . For the neighborhood extremum in the wavelet space of signs, we can change (Equation2) in discrete detailing

$$W_{2^j} f[x_m^{(j)}] = K_m (2^j)^{\alpha_m}, j = 1, \dots, J, \quad (3)$$

(j)

and all the extremum focuses in HR image signified by E_0 can (0) be evaluated by $E_0 = W_{2^0} f[x_m] = K_m$

$$\log_2(W_{2^j} f[x_m^{(j)}]) = \log_2(K_m) + j\alpha_m, j = 1, \dots, J, \quad (4)$$

For the image that we need to improve, we execute a 2-D discrete wavelet change to the LR image. By scaling the LR image a few times, we can acquire the extremum focuses in the wavelet area of the HR images that we need to remake. We anticipate

$$\min_X \|E(X) - E_0\|_2^2, \quad (5)$$

to be little, where $E()$ is the activity to get the all extremum focuses in wavelet space of current HR image. As the $E()$ task is an unlinear activity, it can not be detailed into a framework shape. Rather, we change the misfortune work in (Equation5) to

$$\min_X \|X - IWA(E_0 + E^r)\|_2^2, \quad (6)$$

where X remains for the present HR image, and IWA is a converse wavelet change, E_0 is the extremum focuses that we got from the comparing LR image previously and E^r is the other piece of the wavelet area of HR image X . More

points of interest can be found in [15]. At that point we can execute an iterative slope descent technique to solve this regularization term as underneath

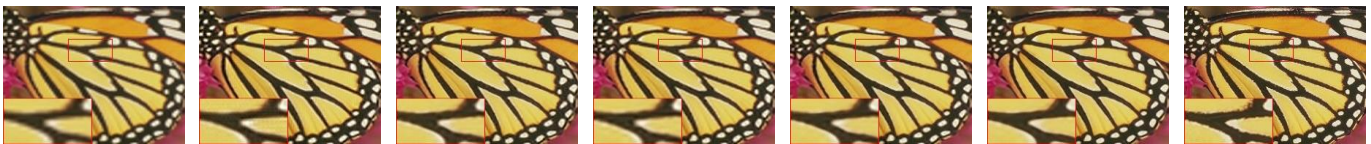
$$X_{t+1} = X_t - \rho(X_t - IWA(E_0 + E_t^r)), \quad (7)$$

where X_t is the gauge of the remaking result after t th emphasis, ρ is the progression of the inclination plunge.

3.2.2. Structure-Keeping Constraint

Regularly, a LR image protects the structure of the relating HR image great. Normal super resolution method like addition as a rule obscure the structure. To upgrade the structures in our reproduction comes about, we can utilize a generally structure regularization to compel our reconstructed comes about. Xu et al [16] proposed a relative aggregate variation(RTV) to separate significant structure

(a)Bicubic (b) ScSR[5] (c) ANR[7] (d) A+[8] (e) CSC[10] (f) Proposed (g) Ground truth Fig. 3. Results by $3\times$ on *Butterfly* image. The red box with its corresponding magnification on the left-bottom of each image



under middle surface examples. The relative aggregate variety is

$$RTV = D_x(p_i)/(L_x(p_i) + \epsilon) + D_y(p_i)/(L_y(p_i) + \epsilon), \quad (8)$$

where $D_x/y(p_i)$ remains for the windowed add up to variety in x/y course in the pixel p_i , $L_x/y(p_i)$ remains for the windowed intrinsic variety in x/y bearing in the pixel p_i , and is a little positive number to maintain a strategic distance from division by zero. more subtle elements in [16].

In a image, pixels with surfaces and strutures yield vast D . In any case, pixels with just surfaces are by and large littler than the pixels with surfaces and structures on the measure of L . It is demonstrated that relative aggregate variation(RTV) is linear forward but then powerful to make fundamental strutures in a image emerge, which implies that it can hone the structures region in an obscured image.

To protect this structure in a reproduced HR image,we include a structurekeeping term $\min_X \|X - X_s\|_2$ to our misfortune work, where X_s is the structure image of the X acquired from [16].

3.2.3. Enhancement procedure

Most importantly, the entire upgrade system is detailed as beneath

$$\begin{aligned} X^* = \min_X & SHX - Yk^2 + ak(I - W)Xk^2 \\ & + bkX - IWA(E_0 + E^r)k^2 + ckX - X^sk^2. \end{aligned} \quad (9)$$

The primary term signifies the back-projection devotion term, Y means the relating LR image, S indicates a downsampling administrator and H indicates an obscuring channel. The second term indicates the nonlocal self-comparability regularization, W signifies nonlocal implies comparable weight network characterized in [13] and I means personality lattice. The third term indicates the Lipschitz regularization, the fourth term signifies the structure-keeping imperative. In the mean time a, b , c signify the regularization parameters. The answer for (Equation9) can be effectively figured in view of iterative improvement, as in Yang et al [5] and utilized as a part of the back-projection, as detailed beneath.

$$\begin{aligned} X_{t+1} = X_t + \nu H^T S^T (Y - SHX_t) - a(I - W)^T (I - W)X_t \\ - b(X_t - IWA(E_0 + E_t^r)) + c(X_t^s - X_t) \end{aligned} \quad (10)$$

4. EXPERIMENTAL RESULT

In this area, we examine the execution of our strategy through the remaking exactness amount and visual quality contrasted and other condition of-workmanship method: SCSR by Yang et al [5], ANR by Timofe et al [7], A+ by Timofe et al [8], CSC by Gu et al [10]. We utilize Set5 that contains 5 images gave in [17] and Set14 that contains 14 images gave in [6] as test images. In our examinations, the patch measure is 9×9 . We separate patches from bicubically added LR in wavelet spaces to create LR patches. In the interim we extricate patches from these HR images in wavelet spaces. We utilize 1024 dictionary and neighborhood estimate is 2048. We set v to 1.8, a to 0.09, b to 1, c to 0.025. Table. 1 indicates PSNR(Peak motion-to-clamor proportion) comparison and table.2 demonstrates SSIM(Structural SIMilarity) comparison, in the interim illustrations are appeared in Fig. 3. We can see that our proposed technique outflanks the condition of-expressions in these 19 testing images, and its PSNR is in normal 0.15dB higher than CSC[10], which is the best among alternate method. In particular. in Fig. 3, we can see that our proposed strategy can safeguard edges superior to the next condition of-state of art method in visual quality. What's more, Table.2 additionally outlines the viability of our strategy.

5. CONCLUSION

In this paper, we proposed a new wavelet-based single image super-resolution method. Our contributions are: We extract high-frequency components separately in four wavelet domains for both LR/HR images, which guarantee the features for LR/HR images forming the same structure in the high-dimensional manifold; We constraint the enhancement with local Lipschitz regularity, which is bonus for us to extract the features in wavelet domains; And we also constraint the enhancement with structure image, which can preserve the edge quite well. With above all, our proposed method achieves better results in both reconstruction precision and visual quality.

However our proposed method is not that fast as other state-of-art methods because regularizing with nonlocal selfsimilarity and structure images significantly increases the complexity of our proposed method. The major of our future investigation is to reduce the computing complexity.

Table 1. PSNR results on image super-resolution with other methods in Set5 and Set14 (scaling factor = 3)

imges	Bicubic	ScSR[5]	ANR[7]	A+[8]	CSC[10]	Proposed
Baby	33.9	34.3	35.1	35.2	35.3	35.3
Bird	32.6	34.1	34.6	35.5	35.8	35.6
Butterfly	24.0	25.6	25.9	27.2	27.1	28.2
Head	32.9	33.2	33.6	33.8	33.8	33.8
Woman	28.6	29.9	30.3	31.2	31.2	31.5
Baboon	23.2	23.5	23.6	23.6	23.6	23.6
Barbara	26.2	26.4	26.7	26.5	26.7	26.4
Bridge	24.4	24.8	25.0	25.2	25.2	25.3
Coastguard	26.6	27.0	27.1	27.3	27.3	27.3
Comic	23.1	23.9	24.0	24.4	24.4	24.6
Face	32.8	33.1	33.6	33.8	33.8	33.7
Flowers	27.2	28.2	28.5	29.0	29.0	29.2

Foreman	31.2	32.0	33.2	34.3	34.2	34.4
Lenna	31.7	32.6	33.1	33.5	33.6	33.7
Man	27.0	27.8	27.9	28.3	28.3	28.4
Monarch	29.4	30.7	31.1	32.1	32.1	32.9
Pepper	32.4	33.3	33.8	34.7	34.7	34.5
Ppt3	23.7	25.0	25.0	26.1	25.9	26.2
Zebra	26.6	28.0	28.4	29.0	29.2	29.3
Average	28.29	29.13	29.5	30.04	30.06	30.21

Table 2. SSIM results on image super-resolution with other methods in Set5 and Set14 (scaling factor = 3)

Images	Bicubic	ScSR[5]	ANR[7]	A+[8]	CSC[10]	Proposed
Baby	0.9039	0.9046	0.9225	0.9233	0.9245	0.9239
Bird	0.9256	0.9398	0.949	0.956	0.958	0.9562
Butterfly	0.8215	0.8622	0.872	0.9091	0.9064	0.9188
Head	0.8007	0.8036	0.8249	0.8281	0.8298	0.8264
Woman	0.8896	0.9044	0.917	0.9288	0.929	0.9291
Baboon	0.5439	0.5879	0.5991	0.6064	0.6092	0.6059
Barbara	0.7531	0.7633	0.7811	0.7795	0.7855	0.7741
Bridge	0.6483	0.6688	0.676	0.684	0.7139	0.7112
Coastguard	0.6147	0.6392	0.6575	0.6621	0.6626	0.6631
Comic	0.699	0.7571	0.7617	0.7798	0.7805	0.7909
Face	0.7984	0.8012	0.8234	0.8271	0.8283	0.8257
Flowers	0.8013	0.8301	0.8405	0.8524	0.8538	0.8533
Foreman	0.906	0.9133	0.9302	0.94	0.9405	0.9418
Lenna	0.8582	0.865	0.8805	0.8851	0.8864	0.8848
Man	0.7495	0.776	0.79	0.8	0.8021	0.8011
Monarch	0.9198	0.9292	0.9377	0.9471	0.947	0.9503
Pepper	0.8698	0.8676	0.8856	0.8921	0.8923	0.8907
Ppt3	0.8746	0.906	0.9127	0.9378	0.9305	0.94
Zebra	0.7943	0.8298	0.8449	0.8508	0.8531	0.8528
Average	0.7985	0.8184	0.8319	0.8416	0.8439	0.8442

6. DICTIONARYS

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