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Object Recognition using Higher Order Moments

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Abstract: In this paper, for boundary representation of the image some invariable features are extracted using higher order moments. Moment based invariants, in various forms, have been widely used over the years as features for recognition in many areas of image analysis. Here the moment based method combines the original moment invariants and the contour moment invariant, which is called a relative contour moment invariant. This algorithm is discussed and tested with scaling, translation and rotation invariance.

As all the possible views of an object caused by translation, scaling and rotation are represented as a single point here we also describe shape space method to represent objects as points on a high-dimensional surface for efficient recognition of object. Then we compare both the relative contour invariant method and shape space method.

Key words: Complex hyper plane, landmarks, manifold, moment invariant, object recognition

INTRODUCTION:

OBJECT recognition is of considerable interest in the field of image analysis and computer vision. Object recognition is the process of matching a test image with the data base images irrespective of the translation, rotation, scaling and occlusion of the test image. Because shape representation plays a very important role in the object recognition, a large number of shape description techniques have been studied. Generally speaking, these methods can be divided into two categories:

- 1. Region based object recognition
- 2. Boundary based object recognition
- 1. Region based object recognition: The region-based techniques take into account the whole area of the object i.e. the region bounded by the boundary line.
- 2. Boundary based object recognition: The boundarybased techniques concentrate merely on its boundary lines. The boundary-based methods are more popular than region-based methods, because the size of the boundary information is significantly smaller than the original 2-D object images.

To adopt boundary-based techniques we have to go for Edge tracing process, which is one of the basic topics in image processing. The aim of the process is to evaluate image information and reduce it to adequate contour line by eliminating the unnecessary information that takes time for recognition process. The task of edge tracing plays an important role in object recognition. We can explain it as follows: The human seeing system looks at any object firstly during the recognition period and runs

an eye over the contour points of it. After tracing contour points, geometricalinformation of objects is obtained. This information is transformed to electrical signals and transmitted to brain and recognition process comes to an end. When we apply this approach to the artificial seeing systems, it is essential to trace edges of objects effectively to reach a successful recognition.

Many shape descriptors, including global features moment invariants, Fourier descriptors such autoregressive models and eigen values of Dirichlet Laplacian, as well as local features such as chain codes, shape context, curvature scale space (CSS) representation and wavelet descriptors have been developed to describe the boundaries of different patterns. The advantages of methods using global features are that they usually require less computational effort and are invariant to size, translation, and orientation changes. The boundary based methods are more popular than region-based method, because the size of the boundary information is significantly smaller than the original 2-D object images. One of the boundary based technique i.e. Moment invariant technique which is discussed here.

OBJECT RECOGNITION USING DISCRETE MOMENT INVARIANT:

Recognition is the basic capacity of human. Pattern recognition is the automatic recognition of the computer system. When the computer system recognizes the image, a value is invariable regardless of the image scaling, translation and rotation. The value is moment invariant. This method was brought forward by M.K.Hu in 1962. He gave the definition and the property of continuous function moment invariant. Moreover he proved the scaling, translation and rotation invariance and gave seven moment invariant functions for continuous function. A recognizing test was done for two letters in computers. Moment invariant functions by Hu need computing all pixels in target area. Though much arithmetic was researched by some researchers, they are fairly time-consuming. Target contour's pixels are generally much fewer than target area pixels. A researcher provided contour moment invariant which only needs computing the moment of contour. He also proved the scaling, translation and rotation invariance. Apparently this arithmetic has much advantage. We call this arithmetic contour moment invariant in order to distinguish Hu's moment invariant. The above contour moment invariant is continuous function's moment invariant. It has the scale, translation and rotating invariance for continuous function. But image is discrete. The above contour moment invariant

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for discrete function only has the translation and rotating invariance but not has the scale invariance. For this case, a new contour moment invariant is provided in this paper. It has the **scale**, **translation and rotating invariance**. This arithmetic is used in the image's recognition and is validated effectively. It is called a **relative contour moment invariant arithmetic**.

The definition of contour moment invariant for discrete function:

Above we discuss the contour moment for continuous function but in fact discrete function is usually used. So the research of contour moment invariant for discrete function is needed. Moment invariant of order (p+q) for discrete function is defined as :-

$$\begin{split} & \mu_{pq} = \sum_{(x,y) \in \mathcal{C}} (x - \overline{x})^p (y - \overline{y})^q f(x,y) \\ & m_{pq} = \sum_{(x,y) \in \mathcal{C}} x^p y^q f(x,y) \\ & \overline{x} = \frac{m_{10}}{m_{00}} = \frac{\sum_{(x,y) \in \mathcal{C}} x f(x,y)}{\sum_{(x,y) \in \mathcal{C}} f(x,y)} \\ & \overline{y} = \frac{m_{01}}{m_{00}} = \frac{\sum_{(x,y) \in \mathcal{C}} y f(x,y)}{\sum_{(x,y) \in \mathcal{C}} f(x,y)} \\ & \eta_{pq} = \frac{\mu_{pq}}{\mu_{00}} / \mu_{00}^{p+q+1} \quad p+q=2,3 \dots \end{split}$$

From the above the seven moment invariants are

From the above the seven moment invariants are
$$\phi_1 = \eta_{20} + \eta_{02}$$

$$\varphi_2 = (\eta_{20} - \eta_{02})^2 + 4\eta_{11}^2$$

$$\phi_3 = (\eta_{30} - 3\eta_{12})^2 + (\eta_{21} - \eta_{03})^2$$

$$\phi_4 = (\eta_{30} + 3\eta_{12})^2 + (\eta_{21} + \eta_{03})^2$$

$$\phi_5 = (\eta_{30} - 3\eta_{12})(\eta_{30} + \eta_{12})[(\eta_{30} + \eta_{12})^2 - 3(\eta_{21} + \eta_{03})^2] + (3\eta_{21} - \eta_{03})(\eta_{21} + \eta_{03})[3(\eta_{30} + \eta_{12})^2 - (\eta_{21} + \eta_{03})^2]$$

$$\phi_6 = (\eta_{20} - \eta_{02})[(\eta_{30} + \eta_{12})^2 - (\eta_{21} + \eta_{03})^2] + 4\eta_{11} (\eta_{30} + \eta_{12})(\eta_{21} + \eta_{03})$$

$$\phi_7 = (3\eta_{21} - \eta_{03})(\eta_{30} + \eta_{12})[(\eta_{30} + \eta_{12})^2 - 3(\eta_{21} + \eta_{03})] + (3\eta_{12} - \eta_{03})(\eta_{21} + \eta_{03})[3(\eta_{30} + \eta_{12})^2 - (\eta_{21} + \eta_{03})^2]$$

Here we will prove the translation and rotating invariance and discuss the change of moment if image magnifies and reduces in discrete case.

A.THE TRANSLATION INVARIANCES

 Δx is the translation quantity in x direction and Δy is the translation quantity in y direction.(x, y)is the coordinate before translation and (x', y')is the coordinate after translation.

$$\begin{cases} x' = x + \triangle x & (x, y) \in c \\ y' = y + \triangle y & (x', y') \in c' \end{cases}$$

We can obtain m'_{pq} :

$$m'_{pq} = \sum_{(x',y') \in c'} (x')^p (y')^q f'(x',y')$$

The relation of f'(x', y') and f(x, y) is followed:

$$f'(x',y') = f(x,y)$$

Now we can obtain the followed equation:

$$\mu'_{pq} = \sum_{(x',y') \in c'} \left(x' - \overline{x}'\right)^p \left(y' - \overline{y}'\right)^q f'\left(x',y'\right)$$

$$= \sum_{(x,y) \in c} \left(x + \Delta x - \frac{m'_{10}}{m'_{00}} \right)^p \left(y + \Delta y - \frac{m'_{01}}{m'_{00}} \right)^q f(x,y)$$

$$= \sum_{(x,y)\in c} \left\{ \begin{bmatrix} x + \Delta x - \frac{\sum_{(x',y')\in c'} x'f'(x',y')}{\sum_{(x',y')\in c'} f'(x',y')} \end{bmatrix}^{p} \times \left\{ y + \Delta y - \frac{\sum_{(x',y')\in c'} y'f'(x',y')}{\sum_{(x',y')\in c'} f'(x',y')} \right\}^{q} \times f(x,y) \right\}$$

$$= \sum_{(x,y)\in c} \left\{ \begin{bmatrix} x + \Delta x - \frac{\sum_{(x,y)\in c} (x + \Delta x) f(x,y)}{\sum_{(x,y)\in c} f(x,y)} \end{bmatrix}^{p} \times \begin{bmatrix} x + \Delta x - \frac{\sum_{(x,y)\in c} (x + \Delta x) f(x,y)}{\sum_{(x,y)\in c} f(x,y)} \end{bmatrix}^{q} \times f(x,y) \right\}$$

$$= \sum_{(x,y)\in c} \left(x - \frac{\sum\limits_{(x,y)\in c} xf(x,y)}{\sum\limits_{(x,y)\in c} f(x,y)}\right)^p \left(y - \frac{\sum\limits_{(x,y)\in c} yf(x,y)}{\sum\limits_{(x,y)\in c} f(x,y)}\right)^q f(x,y)$$

$$= \sum_{(x,y) \in c} \left(x - \frac{m_{10}}{m_{00}} \right)^p \left(y - \frac{m_{01}}{m_{00}} \right)^q f(x,y)$$

$$= \sum_{(x,y)\in C} (x-\overline{x})^p (y-\overline{y})^q f(x,y)$$

$$=\mu_{po}$$

Now η_{pq} can prove having the translation invariance. In terms of the above relation, the seven moments in $\Phi_1 \sim \Phi_7$ have the translation invariance.

B. THE ROTATING INVARIANCES

If θ is the image's rotating angle, (x, y) is the coordinate before rotating and (x', y') is the coordinate after rotating -

$$\begin{cases} x' = x\cos\theta + y\sin\theta \\ y' = y\cos\theta - x\sin\theta \end{cases}$$

From above, we can obtain the followed equation:

$$x' - \overline{x}' = x\cos\theta + y\sin\theta - \frac{m'_{10}}{m'_{00}}$$

$$= x \cos \theta + y \sin \theta - \frac{\sum\limits_{(x,y) \in c} \left(x \cos \theta + y \sin \theta\right) f\left(x,y\right)}{\sum\limits_{(x,y) \in c} f\left(x,y\right)}$$

$$= x\cos\theta + y\sin\theta - \cos\theta \frac{m_{10}}{m_{00}} - \sin\theta \frac{m_{01}}{m_{00}}$$

$$=(x-\overline{x})\cos\theta+(y-\overline{y})\sin\theta$$

Similarly, we can obtain the followed formula

$$y' - \overline{y}' = (y - \overline{y})\cos\theta - (x - \overline{x})\sin\theta$$

The relation among μ'_{20} , μ_{20} and θ is followed:

$$\mu'_{20} = \sum_{(x',y')\in c'} (x' - \overline{x}')^2 f'(x',y')$$

$$= \sum_{(x,y)\in c} \left[\left(x - \overline{x} \right) \cos \theta + \left(y - \overline{y} \right) \sin \theta \right]^2 f(x,y)$$

$$= \sum_{(x,y)\in c} \left[\frac{(x-\overline{x})^2 \cos^2 \theta + (y-\overline{y})^2 \sin^2 \theta}{+2(x-\overline{x})(y-\overline{y})\sin \theta \cos \theta} \right] f(x,y)$$

$$= \mu_{20} \cos^2 \theta + \mu_{02} \sin^2 \theta + 2\mu_{11} \sin \theta \cos \theta$$

Similarly, The relation among μ'_{02} , μ_{02} and θ is followed:

$$\mu'_{02} = \mu_{02}\cos^2\theta + \mu_{20}\sin^2\theta - 2\mu_{11}\sin\theta\cos\theta$$

Because

$$\eta'_{20} = \mu'_{20} / {\mu'_{00}}^3 = \mu'_{20} / {\mu'_{00}}^3$$

$$\eta'_{02} = \mu'_{02} / {\mu'_{00}}^3 = {\mu'_{02}} / {\mu'_{00}}^3$$

$$\varphi_1' = \eta_{20}' + \eta_{02}' = \frac{\left(\mu_{20}' + \mu_{02}'\right)}{\mu_{00}^3}$$

$$= \frac{\left(\mu_{20}\cos^2\theta + \mu_{02}\sin^2\theta + 2\mu_{11}\sin\theta\cos\theta + \mu_{02}\sin^2\theta + 2\mu_{11}\sin\theta\cos\theta\right)}{\mu_{00}^3}$$

$$=\frac{\left(\mu_{20}+\mu_{02}\right)}{\mu_{00}^3}=\eta_{20}+\eta_{02}=\varphi_1$$

From above, the moment Φ_1 has the rotating invariance in discrete situation. Similarly, the other moments has also the rotating invariance in discrete situation.

C. THE SCALE INFLUENCE

If ρ is the image's scale value, (x, y) is the coordinate before changing the image's scale and (x', y') is the coordinate after changing the image's scale.

$$\begin{cases} x' = \rho x \\ y' = \rho y \end{cases}$$

Now we can obtain:

$$x' - \overline{x}' = \rho x - \frac{m'_{10}}{m'_{00}}$$

$$= \rho x - \frac{\sum_{(x,y)\in c} x \rho f(x,y)}{\sum_{(x,y)\in c} f(x,y)} = \rho(x - \overline{x})$$

Similarly, we can obtain formula

$$y' - \overline{y}' = \rho(y - \overline{y})$$

From these formulas we can obtain μ'_{pq} .

$$\mu_{pq}' = \sum_{(x',y') \in c'} \left(x' - \overline{x}'\right)^p \left(y' - \overline{y}'\right)^q f'\left(x',y'\right)$$

$$= \sum_{(x,y)\in c} \rho^{p} (x - \overline{x})^{p} \rho^{q} (y - \overline{y})^{q} f(x,y)$$

$$= \rho^{p+q} \mu_{pq}$$

Now we can obtain η'_{pq} .

$$\eta'_{pq} = \mu'_{pq} / (\mu'_{00})^{p+q+1} = \rho^{p+q} \mu_{pq} / \mu_{00} = \rho^{p+q} \eta_{pq}$$

From above, we can find that moment has not the scale invariance. The moment relates not only with ρ but also with p+q. In theory, the seven moments has the scale invariance in continuous situation but not in discrete situation. Therefore, a new contour moment is provided in this paper which is called a relative contour moment invariant.

Relative contour moment invariant:

Aiming at the above, Φ_1 , Φ_2 ,.... Φ_7 are combined again and then we can obtain six relative contour moments invariant. Relative contour moment invariants have the translation, rotating and scale invariance.

$$\psi_1 = \frac{\sqrt{\phi_2}}{\phi_1}$$
 $\psi_2 = \frac{\phi_3}{\phi_2 \phi_1}$ $\psi_3 = \frac{\phi_4}{\phi_3}$

$$\psi_4 = \frac{\sqrt{\phi_5}}{\phi_4} \qquad \psi_5 = \frac{\phi_6}{\phi_4 \phi_1} \qquad \psi_6 = \frac{\phi_7}{\phi_5}$$

 Ψ_1,Ψ_2 , Ψ_6 have the translation , rotating and scale invariances. Here we only prove the scale invariances.

If ρ is the image's scale value, Ψ'_1 is the relative contour moment invariant after scaling.

$$\psi_1' = \frac{\sqrt{\varphi_2'}}{\varphi_1'} = \frac{\sqrt{\left(\eta_{20}' - \eta_{02}'\right)^2 + 4\eta_{11}'^2}}{\eta_{20}' + \eta_{02}'}$$

$$=\frac{\sqrt{\left(\rho^2\eta_{20}-\rho^2\eta_{02}\right)^2+4\left(\rho^2\eta_{11}\right)^2}}{\rho^2\eta_{20}+\rho^2\eta_{02}}$$

$$=\frac{\rho^2\sqrt{\varphi_2}}{\rho^2\varphi_1}=\frac{\sqrt{\varphi_2}}{\varphi_1}=\psi_1$$

Similarly, $\Psi'_{2} = \Psi_{2},..., \Psi'_{6} = \Psi_{6}$ Relative contour invariant moments have the translation, rotating and scale invariance.

OBJECT RECOGNITION USING SHAPE SPACE:

Among the many cues proposed, such as color, texture, motion, context and function, shape is perhaps the most common and dominant. This work concerns shape representation and shape-based object recognition. Indeed, the recognition of many common objects in natural settings, such as cars and people in outdoor scenes, is still beyond the capability of current techniques and systems. The main difficulty, as pointed out by Ullman, lies in the tremendous view variability associated with the images of a given object. For example, depending on the viewing angle, the pictures of a car may look very different. As a result, an algorithm designed based on a single or a few views may not work on a picture of the object taken from a new view. So, the idea here is to represent objects as points on a high-dimensional surface (i.e., a manifold), called the shape space. For example, in a shape space of 2D objects, all possible views of an object caused by translation, scaling and rotation are represented as a single point.

Object recognition can then be achieved for invariant object recognition, the shape space approach has several advantages. First, it provides a complete, rather than a partial, object representation that is invariant to similarity transformations. It is also relatively insensitive to noise and occlusion. Second, through statistical shape analysis, classical statistical pattern recognition techniques can be extended to the non-Euclidean shape space.

Nevertheless, we believe it represents a new approach to invariant object recognition and is worthy of further investigation. In this work, the shape space approach is studied in the context of 2D object recognition. Potentially, this approach can also be used for 3D object recognition Suppose a 2D object is represented as a set of pointson the plane, calledlandmarks. For example, they may be perceptual salient points on the object boundary, such ashigh-curvature and extreme points. Let the landmarks berepresented by a vector,

$$\mathbf{X} = [x_1, x_2, \dots, x_n],$$

where n is the total number of landmarks and xi is the position of the ith landmark, represented as a complex number. Then, x is a point in Cn, the n-dimensional complex space (Cn can be identified with R2n).

According to Kendall, the shape of x is "what is left when the effects associated with translation, scaling and rotation are filtered away". To remove the effect of translation we let

$$\mathbf{x}' = [x_1', x_2', \dots, x_n'] = [x_1 - \bar{x}, x_2 - \bar{x}, \dots, x_n - \bar{x}],$$

$$\bar{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$$

is the centroid of $x_1, x_2,, x_n$. Now, x' satisfies

$$\sum_{i=1}^n x_i' = 0.$$

Hence, x' is a point on a n - 1 dimensional complex hyperplane (isometric to Cⁿ⁻¹) passing through the origin ofCⁿ, as illustrated in Fig. 2. Similarly, to remove the effect of rotation and scaling, we associate x' with an equivalence class (a set)

$$\mathbf{x}^* = \{\lambda \mathbf{x}', \ \lambda \in \mathbf{C}\},\$$

where C is the set of complex numbers. As \(\frac{1}{2}\) varies over C, x* covers all possible scaling and rotations of x'. Now x* is the shape of x.

Notice that x*, as illustrated in Fig. 2, represents a complex line passing through origin and on the n - 1 dimensional complex hyper plane. Therefore, x* is a point in a space isometric to \mathbb{CP}^{n-2} , the n-2 dimensional complex projective space. This is a smooth and curved non-Euclidean space (i.e., a differentiable manifold) which we will now call the shape space. Its most important geometric property, for the purpose of object recognition, is perhaps the geodesic distance between two points. As shown by Kendall

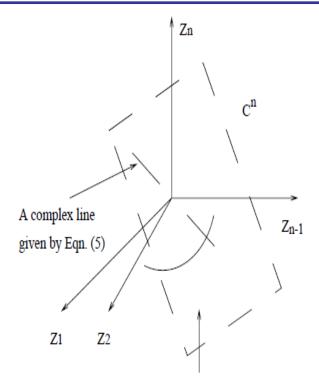
$$d(\mathbf{x}^*, \mathbf{y}^*) = \arccos\left(\frac{|\langle \mathbf{x}', \mathbf{y}' \rangle|}{\|\mathbf{x}'\| \cdot \|\mathbf{y}'\|}\right),$$



The six moment invariant or the 10 different classes are given in table-1

Table-1

		40		45	40	40
	φ_1	φ_2	φ3	φ_4	φ_5	φ_6
Class	0.195	1.634	0.01	2.341	2.15	1.12
-1	1	8	84	3	46	03
Class	0.050	13.91	0.40	6.141	5.09	-
-2	7	3	69	3	57	10.1 15
Class	0.000	-	0.13	4.443	28.1	6.81
-3	1	7.546 8	89	6	239	047
Class	0.024	81.77	0.10	7.324	12.8	21.4
-4	8	5	44	8	273	518
					4	
Class	0.032	-	0.82	11.03	9.02	-
-5	1	11.91	33	42	333	14.2
						478
Class	0.099	-	0.39	8.931	3.66	-
-6	1	2.790	54	40	775	1.11
		7				12
Class	0.036	-	0.07	5.866	-	-
-7	1	24.13	449	76	0.12	46.3
		9			407	245
						8
Class	0.200	0.353	0.00	3.318	-	-
-8	2	7	58	41	7.03	0.63
					78	679
Class	0.338	0.724	0.98	13.66	28.1	-
-9	2	5	45	85	240	33.0
					3	391
Class	0.014	-	0.06	1.976	26.0	0.11
-10	3	265.0	46	1	168	88



An (n-1) dimensional subspace of Cⁿ passing through origin given by Eqn. (4)

Fig. 2. Illustration of the geometric aspects of the definition of shape.

$$d(\mathbf{x}^*, \mathbf{y}^*) = \arccos\left(\frac{|\langle \mathbf{x}', \mathbf{y}' \rangle|}{\|\mathbf{x}'\| \cdot \|\mathbf{y}'\|}\right),$$

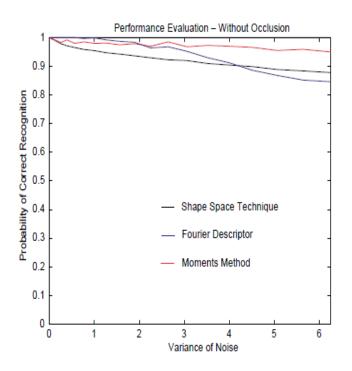
For the object of class-1 the relative contour moment invariants are calculate for different scale, translation and rotation value which is given in table-2.

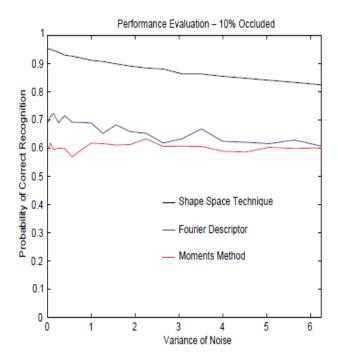
Table-2

Δx	Δy	ρ	θ	ϕ_1	ϕ_2	ϕ_3	ϕ_4	ϕ_5	ϕ_6
0	0	1	0	0.1	1.6	0.0	2.3	0.1	1.1
				951	348	184	413	546	203
30	0	1	0	0.1	1.6	0.0	2.3	0.1	1.1
				951	348	184	413	546	203
0	50	1	0	0.1	1.6	0.0	2.3	0.1	1.1
				951	348	184	413	546	203
10	10	1	0	0.1	1.6	0.0	2.3	0.1	1.1
				951	348	184	413	546	203
0	0	2	0	0.1	1.6	0.0	2.3	0.1	1.0
				888	465	173	417	669	074
0	0	1	3	0.1	1.5	0.0	2.5	0.2	1.1
			0	988	465	273	117	869	174
8	15	0.	3	0.2	1.5	0.0	2.2	0.2	1.1
		5	5	391	648	987	413	346	763
10	20	1.	1	0.1	1.6	0.0	2.3	0.9	1.2
		4	5	745	950	140	117	023	176
5	2	3	4	0.1	1.6	0.0	2.3	0.1	1.3
			0	788	465	073	117	869	074
45	15	1	1	0.1	1.6	0.0	2.3	0.1	1.1
			0	951	348	184	413	546	203

Through the experiment result we can see that the relative contour moment invariants basically keep the same value, so the relative contour moment invariants suit with pattern recognition.

COMPARISON BETWEEN SHAPE SPACE AND MOMENT INVARIANT METHOD:





CONCLUSION:

The image's discrete contour moment is analyzed and proved in theory. The result is the image's discrete contour moment without the scale invariance. In terms of this situation, the arithmetic of the relative contour moment invariants is brought forward. This arithmetic is based on the original seven contour moments. The original seven contour moments are combined into the six relative contour moment invariants. six relative contour moment invariants have the translation, rotating and scale invariance, so the veracity of pattern recognition improves. Though need some quantity of computing moment invariants in the whole object area. So the quantity of computing reduces much and the speed of pattern recognition improves much.

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