

Numerical Analysis of Two Phase Flow Boiling Heat Transfer through Micro-Channel

Dalvir Singh

Dept. of Mechanical Engineering,
Meerut Institute of Engineering
Technology, Meerut India

Santosh Kumar Rai

Dept. of Mechanical Engineering,
Meerut Institute of Engineering
Technology, Meerut India

Sanjeev Kumar Shukla

Dept. of Mechanical Engineering,
Meerut Institute of Engineering
Technology, Meerut India

Abstract - Day by day rapid miniaturization of electronics devices in electronic industry have resulted in continuous raise of heat removal requirements for making the more efficient the electronic devices, thereby making a call for highly thermal efficient cooling technology. Two phase flow boiling heat transfer is the one of the potential solution for heat dissipation for electronic devices. For highly efficient performance and reliability of micro-electronic and mechanical systems (MEMS) devices, the working temperate should be keep below some specific temperature less than 90 °C. The purpose of the work is to develop a numerical model to predict the behaviour of two phase forced convection in micro-channels using de-ionize water (DIW) as the coolant with uniform heat flux in laminar and turbulent flow regime. A 1-D thermal-hydraulic - homogeneous equilibrium model (TH-HEM), consisting of mass, momentum and energy conservation equations and empirical correlation for laminar and turbulent flow, and properties of substance equation as dryness fraction relation with liquid and vapour density, are solved numerically using a finite-difference upwind scheme for single as well as two phase flow and algebraic equations. Finally, the TH-HEM model is used to evaluate the location of boiling front, it's variation with uniform input power, Variation in dryness fraction in two phase region, pressure distribution of fluid along the axial length, wall and fluid temperature distribution along the axial length, for one fixed inlet temperature and fixed outlet pressure condition.

Keywords— Two phase, Boiling, force convectio,; micro-channel, thermal hydraulic homogenous equilibrium model

INTRODUCTION

With the development of micro fabrication technology, micro-fluidic systems have been increasingly used in different scientific disciplines such as biotechnology, physical and chemical sciences, electronic technologies, sensing technologies etc. Micro-channels are one of the essential geometry for micro-fluidic systems; therefore, the importances of convective transport phenomena in micro-channels and micro-channel structures have increased drastically. In recent years, a number of researchers have reported the heat transfer and pressure drop data for laminar and turbulent liquid or gas flow in micro-channels.

Flow boiling heat transfer in micro-channels is now the most popular topic in heat transfer, as the need has arisen for very high heat flux cooling for the new generation of computer chips. Understandings of macroscopic flow and heat transfer have reached a mature stage, but when it comes to micro-channel flow, flow becomes notably different and complex. The universal use of MEMS devices, micro-heat

exchangers, micro-fluidics, other biomedical applications like micro drug delivery, have opened a new field for research.

The quick development of excessive power electronics devices with the expanded scaling down of micro-electronic devices and thermal issues and high speed processing are influencing general system performance and electronic packaging. In the previous couple of decade, the requirements of uniform heat dissipation from electronics devices have increased drastically from 10 W/cm² to 1000 W/cm² which exceeds the system capability of present cooling technology "[1]". Tuckerman and Pease expressed that single phase convective cooling in micro-channels ought to be attainable for input power 1000 W/cm or more than 1000 W/cm, and exhibited a micro-channel heat sink that dissipate 790 W/cm with 71°C temperature increment at 600 mL/min mass flow rate "[2]".

The increase in heat flux, the temperature of MEMS system and electronic devices is also increase but the performance of the devices is decreased due to thermal issue. So improvement of performance of MEMS system and electronic devices are required to reduce thermal issue. So increase the performance of MEMS system and electronic devices, the maximum heat flux should remove from the device or reduce the thermal issue. That why, flow boiling heat transfer method is used to extraction of heat flux from the device, because in flow boiling due to extraction of latent heat devices can dissipate heat without rise in temperature. Also, convective heat transfer coefficient is 0.1 MW/m for laminar flow of water in a 250µm square channel, whereas flow boiling heat transfer coefficient can exceed 1 MW/m²-°C, which makes more attractive for cooling of MEMS systems and electronic devices. In this present study, TH- HEM model has been adopted for flow boiling heat transfer through micro-channel. Numerical simulation is performed with a micro-channel dimension of 500 µm hydraulic diameter and having length of 3 cm. Numerical simulation is carried out to analyze of the two phase flow boiling through micro channels using DI water as the working fluid medium to predict the location of boiling front, pressure drop, variation of fluid coolant temperature and wall temperature along the length of micro channel.

With the increase in heat flux dissipation, device temperature also increases, limiting the heat dissipation capability "[3-5]". But flow boiling due to extraction of latent heat component can dissipate heat without increase in temperature. Also, single

phase heat transfer coefficient for laminar flow of water in a 200 μm square channel is around 0.1 MW/m²-°C, whereas flow boiling heat transfer coefficient can exceed 1 MW/m²-°C making two phase flow more attractive for cooling of electronic devices “[6-10]”. In the present study, TH-HEM model has been adopted for two phase flow through micro channel. Numerical analysis has been carried out on micro channels of having diameter 250 μm and length 3 cm. Results of TH-HEM studies on two phase flow through micro channels using water as the fluid medium were analyzed to predict the location of boiling front, pressure drop, variation of fluid coolant temperature and wall temperature along the length of micro channel

Problem Definition

In two phases boiling heat transfer, Thermal-hydraulic Homogeneous Equilibrium Model (TH-HEM) and thermal-hydraulic Annular Flow Model (TH-AFM) are mostly adopted [5]. The mixture remains in equilibrium in TH-HEM while void fractions occur in TH-AFM. The TH-HEM works on the principle that the mixture (two phase) acts like pseudo single phase fluid whose mass/weight is similar to that of the mass/weight of vapour and liquid contents. At this stage only latent heat exchange within the phases takes place. Due to pressure change, variation of property occurs in the micro channel, resulting in complicated terms. Properties like density, viscosity and enthalpy behave dynamically and hence quality becomes important.

Numerical simulations were carried out with a micro-channel diameter of 250μm having length of 3 cm. DI Water was taken as coolant that enters the channel at ambient temperature of 25°C. Constant heat flux was applied to the surface. Fig 1 shows schematic diagram of micro-channel with boundary condition on which simulation was performed. DI Water extracts heat continuously, resulting in phase transition leading to a two phase predominant flow.

It is very important to obtain the location of boiling front. Beyond this point vapour quality is greater than zero hence two phase flow exist while before this point, flow is in single phase. Location of boiling front can be extracted by characteristics of saturation enthalpy and bulk fluid enthalpy as shown in Fig 2. Effectiveness of cooling is obtained in terms of temperatures of wall and fluid. For the same two set of equation have been solved for two distinct zones.

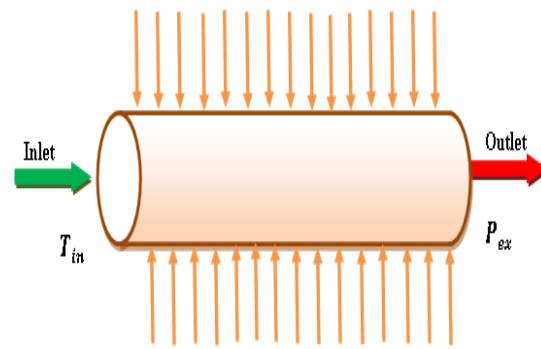


Figure 1: schematic diagram of micro channel

Mathematical Modeling of Th-Hem Assumption

Applying Dirichlet boundary temperature condition at inlet and system pressure at outlet of micro-channel shown in Fig 1, pressures and temperature at discrete point along axial length of microchannel have been computed. All the other properties namely enthalpy of fluid, wall temperature, enthalpy, density, dryness fraction were obtained by state of equation.

Determination of Boiling Front

The equ. 1 is essentially an energy conservation equation. Here i_1 is input heat flux supplied to the micro-channel, L is length of micro-channel, while \dot{W} is mass flow rate of DI water. With pressure distribution known along the axial length of the micro-channel, enthalpy of saturated liquid was evaluated using saturation properties. The location at which bulk fluid enthalpy obtained from equ. 1 and that of saturation enthalpy become equal and intersect to each other, give the location of boiling front known as X_c .

$$i_{f(x)} = i_1 + \frac{Q \cdot x}{L \cdot \dot{W}} \tag{1}$$

Calculation of Dryness fraction (Vapour Quality)

Dryness fraction is the ratio of vapour mass to the total mass. It is zero in sub cooled liquid, and varies in two phase from zero to 1 and more than 1. Hence it was evaluated in the two phase region by equ. 2. Equation 2 establishes relationship between enthalpy of liquid, vapour contained, and mixture. Before boiling front, dryness fraction was zero but after boiling front, that is two phase zone the quality of liquid, Vapour quality (Dryness fraction) was determined by using equ. 2. Where i_f is bulk fluid enthalpy, i_l is the saturation enthalpy at liquid zone and i_v is the saturation enthalpy at vapour zone at given system pressure

$$i_f(j) = (1 - X(j))i_l(j) + X(j) * i_v(j) \tag{2}$$

Determination of Pressure for Single Phase Zone

Pressure distribution in single phase zone was obtained by using the pressure equation 3. Where f_{sp} is single phase friction

factor, G is mass flux in Kg/s-m^2 and ρ is DI water density in Kg/m^3 . f_{sp} was calculated using laminar flow correlation for flow inside a pipe $f_{sp}=64/\text{Re}$ for this. In calculations effect of pressure drop due to contraction has been ignored as cross section area was constant and smooth.

$$\Delta P_{sp} = \frac{f_{sp} * G^2 * X_c}{2 \rho * D_h} \quad (3)$$

Where G , ρ Re and f_{sp} are kg/s-m^2 , kg/m^3 , Reynolds number, friction factor in single phase respectively.

Pressure Equation for Two Phase Region

The equ 4 is mainly pressure drop equation derived from Navier strokes momentum conservation equation. Pressure distribution was calculated by using equ. 4. Here in the equation the right hand side first term is known as signifies friction drop while second term signifies convective acceleration term. Here effect of gravity body force has been disregarded because micro-channel is horizontal. Also capillary effect i.e. surface tension effects have been not taking to simplify the problem. Hydraulic dryness D_h was used to make this case analogous to pipe flow. All the properties: density, viscosity, enthalpy, friction factor of two phase (f_{TP}) was dynamic so average properties were used.

$$-\frac{dp}{dx} = \frac{f_{TP} * G^2}{2 \rho * D_h} + \frac{d}{dx} \left(\frac{G^2}{\rho} \right) \quad (4)$$

Average density ρ_m was computed by equ. 5.

$$\frac{1}{\rho_m} = \frac{X}{\rho_v} + \frac{1-X}{\rho_l} \quad (5)$$

Similarly average viscosity μ_m and two phase friction factor f_{TP} was computed using equ. 6 and 7 respectively. Here ρ_l and ρ_v are saturated liquid and saturated vapour density at specified pressure.

$$\mu_m = \rho_m \left(\frac{X * \mu_v}{\rho_v} + \frac{(1-X) * \mu_l}{\rho_l} \right) \quad (6)$$

$$f_{tp} = \frac{64}{\text{Re}} = \frac{64 * \mu_m}{G * D_h} \quad (7)$$

In equ (6) μ_m and μ_l are saturated vapour and liquid viscosity at given pressure.

Energy Equation use to calculat temperatur

Energy equation was used to calculate the bulk fluid temperature and wall temperatures. In single phase as well as two phase zone fluid temperature was computed using equ. 8

$$T_f(x) = T_1 + \frac{Q * x}{\dot{W} * C_{pl} * L} \quad (8)$$

Here C_{pl} is saturated specific heat capacity at specified pressure. In two phase region temperature of fluid (T_f) is equal to saturated temperature at specified pressure. Also, temperature of water (T_w) was calculated using equ. 9.

$$T_w = T_f + \frac{Q}{h_{conv}(wL + \eta 2dL)} \quad (9)$$

η is fin efficiency and is heat transfer coefficient. i_f was computed using equ. 10.

$$\dot{W} \frac{di_f}{dx} - \eta h_{conv} P_c (T_w - T_f) = 0 \quad (10)$$

Here \dot{W} is mass flow rate, P_c is perimeter of cross section.

Heat Transfer Coefficient Calculation

Convective heat transfer coefficient (h_{conv}) for single phase was computed using correlation for laminar flow through a tube for constant heat flux condition. In two phase region, heat transfer coefficient h_1 was computed using correlation of Kandlikar[15] for homogeneous flow through a given tube.

$$h_{conv} = 4.36 * \frac{k}{D_h} \quad (11)$$

$$\frac{h_{TP}}{h_1} = \beta_1 C_0^{\beta_2} + \beta_3 B_0^{\beta_4} \quad (12)$$

$$C_0 = \left(\frac{1-x}{x} \right)^{0.8} * \left(\frac{p_v}{p_l} \right)^{0.5} \text{ is convention Number}$$

β_1 - β_4 is constant dependent upon fluid properties, h_1 was found using Detous Boelter correlation [12-14].

$$h_l = 0.023 * \text{Re}^{0.8} * \text{Pr}^{0.4} * \frac{k}{D_h} \quad (13)$$

Numerical Simulation Algorithm

GDE's are used to performed simultaneous equation to be solved for pressure and temperature together for all node points. Numerical algorithm developed for solving these equations is given in the following sub section. Figure 2 is showing the schematic diagram of discrete physical domain with inlet and outlet boundary conditions.

Algorithm

- #.Find out $i_f(j)$ at all grid points using given temperature at first node and equ. 1 by marching in forward direction.
- #.Assume pressure $P(j)$ at all grid points maintaining negative pressure gradient based on outflow Dirichlet pressure BC's.
- #.Evaluate saturation properties at all discretized points for assumed pressure $P(j)$ like $T_{fsat}(j)$, $i_f(j)$, $\mu_l(j)$, $\mu_v(j)$, $\rho_l(j)$, $\rho_v(j)$, $P_l(j)$, $R_{e_l}(j)$.
- #.Use i_f and i_f saturated to find out location of boiling front. At the location of boiling front, these values should be equal.
- #.Find $X(j)$ in two phase region using and properties of and using equ. 2.
- #.Find $\rho_m(j)$ and $\mu_m(j)$ using equ. 5 and equ. 6 respectively for two phase region.
- #.Similarly find f_{tp} and f_{sp} using equ. 7.
- #.Solve pressure equation for single phase and two phase region using discretized equ. 3 and equ. 4 respectively. Iterate the process till pressure $P(i)$ gets converged.

- #.Find $T_f(j)$ for single phase region by using equ. 8. In two phase region it will be equal to T_f saturated.
- #.Find $h_{conv}(j)$ using equa. 11 and equ. 12 for single phase and two phase region respectively.
- #.Find $T_w(j)$ using equ. 9.
- #.Find if using equ. 10. Iterate if till convergence is achieved.

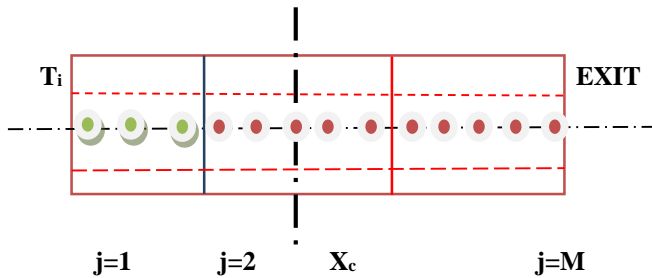


Figure 2: Discretization of physical domain.

RESULTS AND DISCUSSION

Numerical simulation was carried out for fixed inlet temperature and fixed outlet system pressure condition. The present work are presented in the form of location of boiling front, It's variation with heat fluid supplied Q, Variation in dryness fraction X in single and two phase region, pressure distribution of fluid along axial length, wall and fluid temperature distribution along the axial length.

Boiling Front Location

In the Fig 3 red curve shows bulk enthalpy characteristics while blue shows saturated enthalpy characteristics at saturated pressure. The point of intersection gives boiling front location. The saturatin enthalpy first contant and then decrease minimal rate but bulk entholpy contounslly increase hence saturated enthalpy and bulk enthalpy intersect to each other at a point. This point is known as boiling front location.

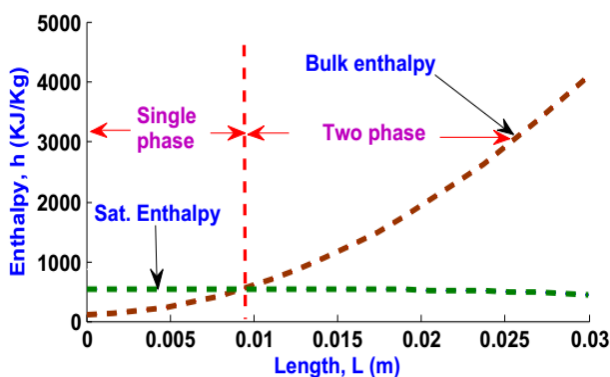


Figure 3: Boiling Front Location.

Variation of Boiling Front with Input power

With the increased input power supplied to the wall of micro-channel, input power supplied boiling will start early. Fig 4 shows intensely the shift of boiling front location towards inlet

section with the increase in input power supplied. With 0.5 W input power supplied it was at 8 mm while with 2 W input power supplies it was at 3 mm boiling front location. The rate of shift however would decrease and becomes almost constant; boiling front took almost fixed position beyond 2.5 W input powers supplied.

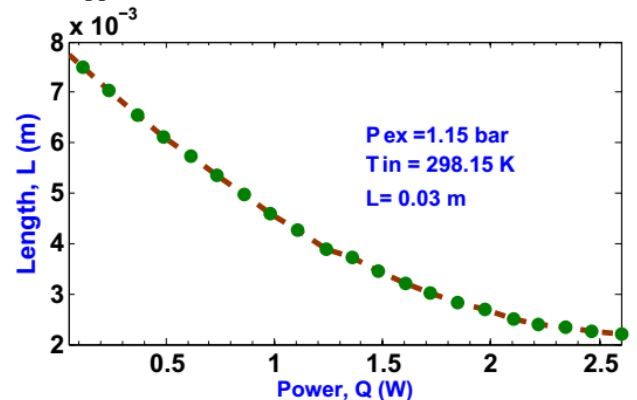


Figure 4: Variation of Boiling front with respect to input power supplied.

Vapour Quality along the Length of Channel

In single phase region dryness fraction is zero and only sub cooled liquid single face exists. In two phase region beyond X_c , X increases almost linearly from 0 to 3 in downstream locations as fluid will get more and more heat while moving in downstream direction. Fig 5 depicts almost liner variation of vapour quality X with channel length. It can be seen clearly that throughout two phase region faster heat transfer takes place as X has not crossed value of 1.0.

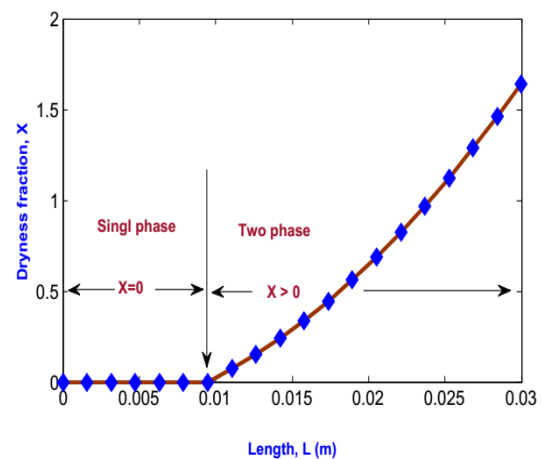


Figure 5: Variation in vapour quality in downstream direction points.

Pressure Variation along the Length

The variation of system pressure in single phase region is very low while that in two phase region is very high. The reason being in single phase region pressure drop is only due to friction while in later acceleration terms also contribute to pressure drop. Also friction loss is accompanied with a multiplier point whose value is greater. Pressure drop due to acceleration term dominates in two phase flow Fig 6.

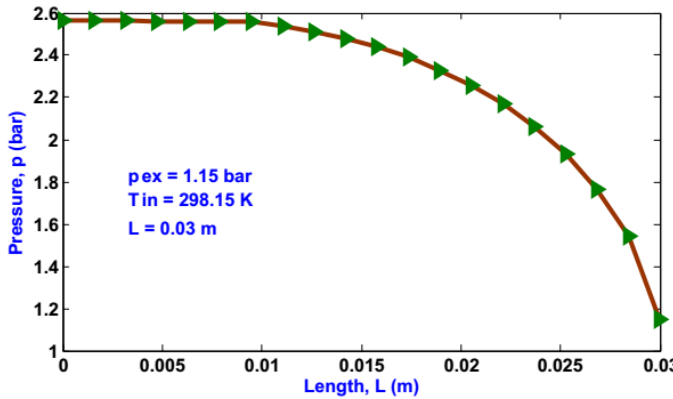


Figure 6: Variation in Pressure distribution in downstream direction Points.

Pressure Drop Variation with Input power

Pressure drop (ΔP) increases with increase in input power because with increase in input power there is increase in convection current (more turbulence) which in turn increases pressure drop. Moreover as input power increases, two phase region would be larger and hence more pressure drop take place Fig 7.

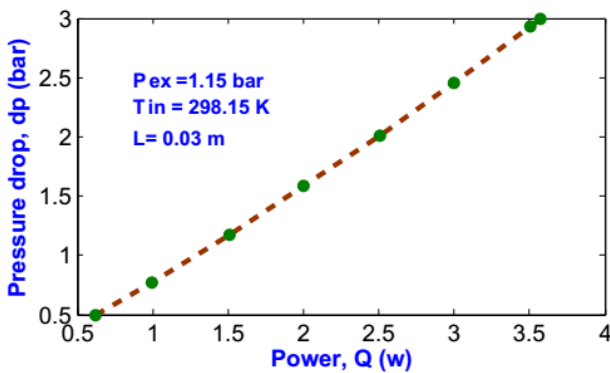


Figure 7: Variation in pressure drop with respect to power input.

Bulk Temperature and Wall Temperature Variation Along the Length

Figure 8 shows in single phase region both bulk temperature (T_f) and wall temperature (T_w) increases because of increased fluid enthalpy as a result of heat input. In two phase region beyond X_c due to existence of saturation condition and to maintain favorable pressure gradient both T_f and T_w decreases.

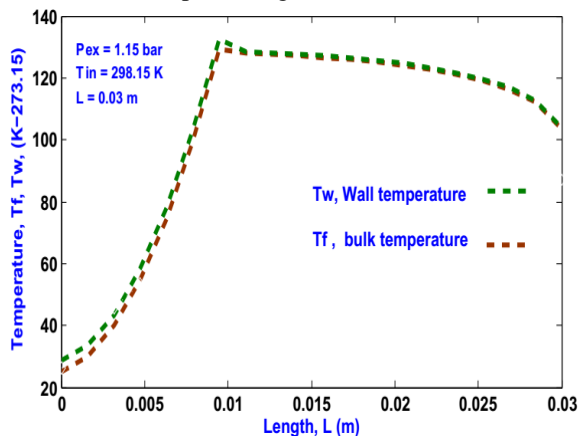


Figure 8: Variation of T_w and T_f along micro-channel length

CONCLUSION

A numerical analysis was conceded out to estimate the existence of location of boiling front, pressure drop, and pressure drop variation with input power, variation of boiling front with input power, bulk temperature (T_f) and wall temperature (T_w) and variation of quality of fluid along the length of micro-channel. The present results of TH-HEM studies on two phase flow through micro-channels using DI water as the fluid medium were analyzed. GDE's analysis incorporates effects of fluid flow rate, heat transfer and power input. The GDE's were solved to predict the location of boiling front, pressure drop and variation of quality of fluid along the length of micro-channel.

- Increasing in power input location of boiling front decreases
- Increasing in power input pressure drop increases linearly.
- Variation of pressure along length first decrease with minimal rate in single phase and after reaching in two phase zone pressure is drastically decreases
- Bulk temperature (T_f) and wall temperature (T_w) increases up to single phase after reaching in two phase zone the bulk temperature and wall temperature decrease and both the temperature are almost equal

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Nomenclature

T_f	bulk temperature
T_w	wall temperature
Q	heat fluid supplied
i_l	heat supplied
L	length of micro-channel
W	mass flow rate
i_l	saturation enthalpies of liquid
i_v	saturation enthalpies of vapour
i_f	bulk fluid enthalpy
f_{sp}	single phase friction factor
G	mass flux in Kg/s-m^2
ρ	D water density in Kg/m^3
Re	Reynolds number
D_h	Hydrolic dryness
F_{tp}	friction factor of two phase
ρ_m	Average density
μ_m	average viscosity
ρ_l	saturated liquid density at specified pressure.
ρ_v	saturated vapour density at specified pressure.
C_{pl}	saturated specific heat capacity at specified pressure.
η	fin efficiency
P_c	perimeter of cross section