

# MRC Receiver in Correlated Hoyt Fading Channel with Multiple Modulation Technique

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**Abstract**— In this paper the performance of diversity receivers and M-ary modulation over hoyt fading channels is analysed. M-ary modulation scheme has been tested on hoyt fading channel as it is more realistic representation of fading in satellite link. We have tested it for 16-PSK, 4-PSK and 32 PSK scheme for various fading and correlation coefficient parameters of hoyt channel. Hoyt channel is derived form nakagami-m channel and also known as nakagami-q channel. The classical PDF based approach has been followed to derive the performance measures of basic diversity combiner namely Maximal ratio combining (MRC) receiver over Hoyt. The analysis is carried out for both independent and correlated fading channels for various coherent and noncoherent modulation schemes. For independent diversity receivers the analysis has been carried out for arbitrary number of input branches. The effect of diversity order and fading parameters on performance measures is studied with the help of the numerical evaluation of the obtained expressions. For dual correlated receivers the analysis is carried out for arbitrary correlation, whereas for  $L$  diversity receivers it is for most important practical correlation models exponential correlation. Exponential correlation is used to model the system when the receiving antennas are placed in a linear array. The effect of correlation on the receiver performance is studied for all the systems. To validate the derived expressions Monte carlo simulation is performed.

**Keywords**—M-Array Modulation; Diversity; Nakagami-m fading channel.

## I. INTRODUCTION

In past few years, wireless communication has played an important role in information technology as information can be transmitted without the need of dedicated link between transmitter and receiver unlike wired communication, where a dedicated link/channel exist between transmitter and receiver. Compared to wired communication systems, wireless systems introduce a very interesting feature 'mobility'. In any kind of communication, wired or wireless, there are some parameters like bandwidth, transmitted power, data rate etc. which decide the reliability of a system. The one which optimizes all of them is said to be a perfect system. In recent years, lots of research has been done on both kinds of communication so that a reliable system can be designed with high bandwidth, low transmitted power, high data rates and low bit or symbol error probability.

## A. Wireless Communication System

In a wireless communication system, data is transmitted in the form of electromagnetic waves using antennas. When signal propagates through the wireless media, phenomena such as reflection and scattering through buildings, trees etc. and refraction through the edges causes the signal to follow multiple paths having different path loss factors and different delays. Thus, at the receiver, the received signal consists of multiple copies of same information bearing signal having different amplitudes and different phases arising due to different path lengths. Figure 1 shows a typical urban/suburban mobile radio environment. In the figure the direct path between the transmitter and the receiver is called line-of-sight (LOS) path,

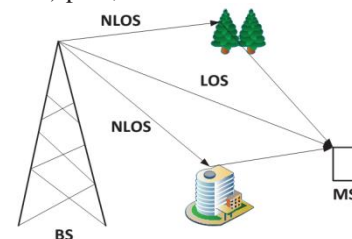


Figure 1 Paths between transmitter and receiver

Whereas, the path corresponding to reflected signal is called on line-of-sight (NLOS) path. These multipaths have different phases corresponding to different path-delays, so that they interfere at the receiver either constructively or destructively resulting in variation in signal-to-noise ratio. In addition, mobility introduces time variation in channel response, i.e. if a very short pulse is transmitted; the received signal appears as a train of pulses due to presence of multipath. Secondly, as a result of time varying response, if same procedure is followed multiple times, a change is observed in the received pulse train over time, which will include changes in the sizes of individual pulses, changes in relative delays among the pulses and often, changes in the number of pulses observed. Hence, the equivalent low-pass time varying impulse response of the channel can be modelled as [1]:

$$c(\tau; t) = \sum_i \alpha_i(t) e^{-j2\pi f_c \tau_i(t)} \delta[t - \tau_i(t)]$$

Where,  $\alpha_i(t)$  and  $\tau_i(t)$  are time varying attenuation factor and path delay for  $i$ th path respectively. For a transmitted signal  $s(t) = 1$  the received signal for the case of discrete multipath is given by [1]:

$$r_l(t) = \sum_i \alpha_i(t) e^{-j\theta_i(t)}$$

The  $\alpha_i(t)$  and  $\tau_i(t)$  associated with different signals vary at different rates and in random manner. So, received signal  $r_l(t)$  can be modelled as a random process. For large number of paths, central limit theorem can be applied and  $r_l(t)$  can be modeled as complex-valued Gaussian random process i.e.  $c(\tau; t)$  is also a complex-valued random process in  $t$  variable [1].

## II. DIVERSITY COMBINING TECHNIQUES

There are different types of diversity combining techniques used in practice [2], which are as follows:

### A. Maximal Ratio Combining

In maximal ratio combining technique, the received multiple faded copies of the transmitted signal are co-phased. The co-phased signal copies are weighted individually in proportion to their strength to maximize SNR at the output of the combiner. Assuming the received signal SNR at the input of the combiner is  $\gamma_i$ ,  $i = 1, 2, \dots, N$ , the output SNR can be shown to be [5]:

$$\gamma_{MRC} = \sum_{i=1}^N \gamma_i$$

The MRC operation requires estimation of phase and amplitude of each received input branch signal. Hence, the complexity of implementation is high.

### B. Equal Gain Combining

Different weights for each branch may not be convenient as it may increase the complexity of the receiver as in the case of MRC. So it is convenient to set all the gains to unity, while co-phasing all signals before combining [2]. This technique of combining is called Equal Gain Combining.

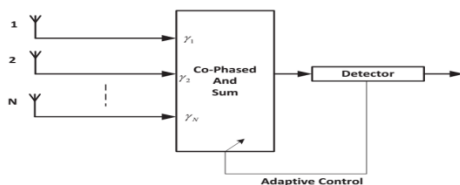


Figure 2: Block diagram of Equal Gain Combiner [2]

For EGC, the output SNR is given as [2]:

$$\gamma_{EGC} = \frac{(\sum_{i=0}^N \alpha_i^2) E_s}{\sum_{i=0}^N P_{N_i}}$$

where,  $\alpha_i$  is the fading amplitude for  $i$ th copy of the transmitted signal.

### C. Selection Combining

In selection combining (SC), the system chooses the received signal having maximum SNR out of all copies of signals received. In this scheme the output SNR can be given as [2]:

$$\gamma_{SC} = \max \{ \gamma_1, \gamma_2, \dots, \gamma_N \}$$

### D. Switch and Stay Combining

The switch and stay combining (SSC) technique discussed here is presented in [2] and also shown in Figure 4. In this system, there are only two copies of fading signals are used. The combiner has only two antennas to receive fading signals. The received signal is fed as shown in Figure 4. In this scheme the received SNR  $\gamma_1$  at antenna L1 is compared with a predefined threshold  $\gamma_T$ . Switching occurs to the input branch L2 if  $\gamma_1 < \gamma_T$ . And it again switches to first branch if  $\gamma_1 > \gamma_T$ . It may happen that after switching the input SNR  $\gamma_2$  at L2 is less than  $\gamma_T$  or even less than  $\gamma_1$ , in such case the switch will still be connected to L2 until the SNR of first branch becomes greater than  $\gamma_T$ . Switching from branch L2 to branch L1 is done in similar manner.

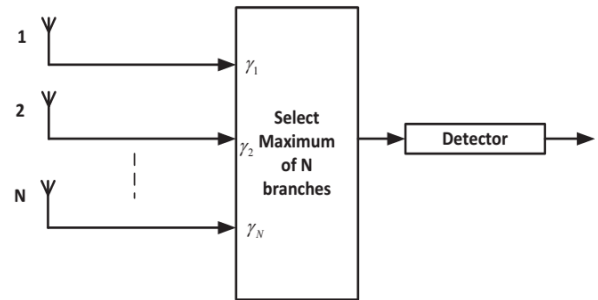


Figure 3: Block diagram of Selection Combiner

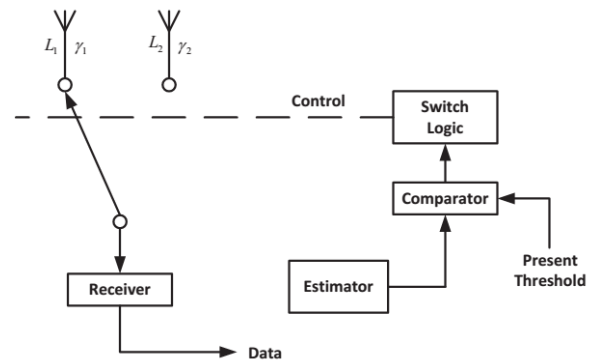


Figure 4: Block diagram of Dual branch Switch and Stay Combiner

The SSC output SNR,  $\gamma_{SSC}$  can be given as:

$$\gamma_{SSC} = \begin{cases} \gamma_1 & \text{if } \gamma_1 \geq \gamma_T \\ \gamma_2 & \text{otherwise} \end{cases}$$

### E. Switch and Examine Combining

Unlike SSC combining scheme, switch and examine combining (SEC) adds the benefit of having multiple branches at the receiver, especially when they are independent and identically distributed (i.i.d.) or equicorrelated and identically distributed. In SSC scheme, receiver switches between the

best two paths, adding a path does not improve the performance unless the added path is better than at least one of the best two ones. In SEC combining scheme, the receiver starts examining from the first path. If first path is acceptable, it continues to receiver from it, else, it switches and examines the next available path. This process continues until an acceptable path is found or all paths have been examined. In the latter case, the receiver stays on the last examined path [6] or selects the best path for reception [7].

### III. PROPOSED WORK

In our work we have tested the hoyt fading channel performance in two different systems. One is M-ary PSK simulation and other is MRC diversity scheme in monte-carlo simulation for correlated hoyt fading channel. The motivation behind MPSK is to increase the bandwidth efficiency of the PSK modulation schemes. In BPSK, a data bit is represented by a symbol. In MPSK,  $n = \log_2 M$  data bits are represented by a symbol, thus the bandwidth efficiency is increased to  $n$  times. Among all MPSK schemes, QPSK is the most-often-used scheme since it does not suffer from BER degradation while the bandwidth efficiency is increased. Since the description about M-ary PSK modulation scheme is not so important to inherit in this chapter. So we have put that detail in appendix below.

Correlation among received fading signals cannot be avoided due to reasons discussed in [1, 2]. Analysis of diversity receivers for correlated channels is relatively more complicated compared to the independent fading case. In this section, performance of dual-MRC, receivers are analyzed for correlated Hoyt fading channels. For MRC receiver an analysis for unequal fading parameters is also presented in addition to the equal fading parameter case. Unequal channel fading parameters may be observed in urban fading environments where diversity channels may have different characteristics. In the analysis presented here the PDF based approach is used. Some conditions are followed for MRC simulation which are:

1. We have N receive antennas and one transmit antenna.
2. The channel is flat fading – In simple terms, it means that the multipath channel has only one tap. So, the convolution operation reduces to a simple multiplication.
3. The channel experienced by each receive antenna is randomly varying in time. For the  $i^{\text{th}}$  receive antenna, each transmitted symbol gets multiplied by a randomly varying complex number  $h_i$ . As the channel under consideration is a hoyt channel, the real and imaginary parts of  $h_i$  are Gaussian distributed having mean  $\mu_{h_i}$  and variance  $\sigma_{h_i}^2 = 1/2$ .
4. The channel experience by each receive antenna is independent from the channel experienced by other receive antennas.
5. On each receive antenna, the noise  $\mathcal{N}$  has the Gaussian probability density function with

$$p(n) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(n-\mu)^2}{2\sigma^2}}$$

with  $\mu=0$  and  $\sigma^2 = \frac{N_0}{2}$ .

The noise on each receive antenna is independent from the noise on the other receive antennas.

6. At each receive antenna, the channel  $h_i$  is known at the receiver.

7. In the presence of channel  $h_i$ , the instantaneous bit energy to noise ratio at  $i^{\text{th}}$  receive antenna is  $\frac{|h_i|^2 E_b}{N_0}$ . For notational convenience, let us define,

$$\gamma_i = \frac{|h_i|^2 E_b}{N_0}$$

#### A. Maximal Ratio combining diversity scheme

A signal transmitted at a particular carrier frequency and at a particular instant of time may be received in a multipath null. Diversity reception reduces the probability of occurrence of communication failures (outages) caused by fades by combining several copies of the same message received over different channels. In general, the efficiency of the diversity techniques reduces if the signal fading is correlated at different branches. The most common and efficient diversity scheme is maximal ratio combining (MRC). In Maximum Ratio combining each signal branch is multiplied by a weight factor that is proportional to the signal amplitude. That is, branches with strong signal are further amplified, while weak signals are attenuated as shown in figure 5.

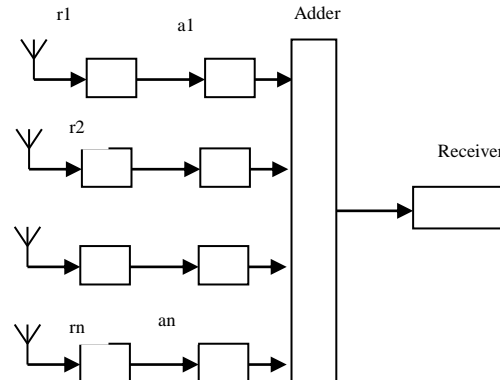


Figure 5: L-branch antenna diversity receiver (L = 5). With

MRC, the attenuation/amplification factor is proportional to the signal amplitude  $a_i = r_i$  for each channel  $i$ .

On the  $i^{\text{th}}$  receive antenna, the received signal is,

$$y_i = h_i x + n_i$$

Where  $y_i$  the received symbol on the  $i^{\text{th}}$  is receive antenna,  $h_i$  is the channel on the  $i^{\text{th}}$  receive antenna,  $x$  is the transmitted symbol and  $n_i$  is the noise on  $i^{\text{th}}$  receive antenna.

$y_i$  Expressing it in matrix form, the received signal is,

$$Y = Hx + n, \text{ where}$$

$y = [y_1, y_2, \dots, y_n]^T$  is the received symbol from all the receive antenna

$h = [h_1, h_2, \dots, h_n]^T$  is the channel on all the receive antenna  $x$  is the transmitted symbol and

$n = [n_1, n_2, \dots, n_n]^T$  is the noise on all the receive antenna.

The term,  $h^H h = \sum_{i=1}^N |h_i|^2$  i.e sum of the channel powers across all the receive antennas.

#### B. Complex Gaussian Model of Hoyt Random Variables

The complex Gaussian model of Hoyt RV  $\alpha_l = |Z_l|$  for  $l$ th ( $l = 1, 2, \dots, L$ ) branch can be given as

$$Z_l = X_l + jY_l, \quad l = 1, 2, \dots, L$$

In this representation, the Hoyt RV  $\alpha_l = |Z_l|$  has the PDF given in Equation. For the convenience of presentation but without loss of generality, we assume  $\sigma_{xl} = 1$ , this result  $\sigma_{yl} = q$ . Assuming  $\sigma_{xl}^2 = \sigma_x^2$  and  $\sigma_{yl}^2 = \sigma_y^2 \forall l$ , from above equation, we can obtain  $\Omega_l = E[\alpha_l^2] = 1 + q^2$ . Substituting this value of  $\Omega_l$  in Equation and expressing  $I_0(\cdot)$  in terms of confluent hyper geometric function, Equation 1.1.2.3 can be rewritten as

$$f_{\alpha_l}(\alpha_l) = \frac{\alpha_l e^{-\frac{1}{2q^2}\alpha_l^2}}{q} F_1\left(\frac{1}{2}; 1; \frac{1-q^2}{2q^2}\alpha_l^2\right)$$

For equal branch average power i.e.  $\Omega_1 = \Omega_2 = \dots = \Omega_L = \Omega$  (equivalently, for  $\bar{\gamma}_1 = \bar{\gamma}_2 = \bar{\gamma}_3 \dots = \bar{\gamma}$ ),  $Eb/N_0$  can be expressed in terms of the fading parameter  $q$  as

$$\bar{\gamma} = \Omega \left( \frac{Eb}{N_0} \right) = (1 + q^2) \left( \frac{Eb}{N_0} \right)$$

#### C. Characteristic Function of Sum of Hoyt Square RVs

In the mathematical model of Hoyt RVs i.e.  $\alpha_l^2 = x_l^2 + y_l^2$  is independent. So the joint CF of  $\alpha_{2l}$  can be given as  $\phi_{\alpha_1^2, \alpha_2^2}(j\omega_1, j\omega_2)$

$$= \frac{1}{(1-\rho^2)(2\sigma_x\sigma_y)^2} \sum_{k=0}^{\infty} \sum_{t=0}^{\infty} \frac{(2k-1)!!(2t-1)!!}{k!t!} \left[ \left( \frac{1}{2(1-\rho^2)\sigma_x^2} + j\omega_1 \right) \left( \frac{1}{2(1-\rho^2)\sigma_y^2} + j\omega_2 \right) \right]^{k+\frac{t}{2}}$$

$$\phi_{\alpha_1^2, \dots, \alpha_L^2}(j\omega_1, j\omega_1, \dots, j\omega_L)$$

$$= \phi_{X_1^2, \dots, X_L^2}(j\omega_1, j\omega_1, \dots, j\omega_L) \phi_{Y_1^2, \dots, Y_L^2}(j\omega_1, j\omega_1, \dots, j\omega_L)$$

An expression for  $\phi_{X_1^2, \dots, X_L^2}(j\omega_1, j\omega_1, \dots, j\omega_L)$  can be derived as shown below:

From the PDF of  $X_l$ , performing transformation of random variable operation, PDF of a  $X_l^2$  can be obtained as

$$f_{X_l^2}(X_l^2) = \frac{1}{\sqrt{2\pi\sigma_x^2}x_l} e^{-\frac{x_l^2}{2\sigma_x^2}}$$

From above equation  $X_l^2$  can be obtained as

$$\phi_{X_l^2}(j\omega_1) = E[e^{j\omega_1 X_l^2}]$$

$$= \frac{1}{(2\pi\sigma_x^2)^{1/2}} \int_0^{\infty} \frac{1}{\sqrt{x_l}} e^{-\left(\frac{1}{2\sigma_x^2} + j\omega_1\right)x_l} dx_l$$

Performing the integration we obtain

$$\phi_{X_l^2}(j\omega_1) = \frac{1}{\sqrt{2\sigma_x^2\left(\frac{1}{2\sigma_x^2} + j\omega_1\right)}}$$

Since  $X_l$ s are independent their joint CF is the product of individual CFs, hence

$$\phi_{X_1^2, \dots, X_L^2}(j\omega_1, j\omega_1, \dots, j\omega_L) = \frac{1}{(2\sigma_x^2)^{L/2}} \prod_{i=1}^L \frac{1}{\sqrt{\left(\frac{1}{2\sigma_x^2} + j\omega_i\right)}}$$

Similarly the joint CF of RVs  $Y_1^2 \dots Y_L^2$  can be obtained as

$$\phi_{Y_1^2, \dots, Y_L^2}(j\omega_1, j\omega_1, \dots, j\omega_L) = \frac{1}{(2\sigma_y^2)^{L/2}} \prod_{i=1}^L \frac{1}{\sqrt{\left(\frac{1}{2\sigma_y^2} + j\omega_i\right)}}$$

Hence, the joint CF in Equation can be obtained as

$$\phi_{\alpha_1^2, \dots, \alpha_L^2}(j\omega_1, j\omega_1, \dots, j\omega_L) = \phi_{X_1^2, \dots, X_L^2}$$

$$= \frac{1}{(2\sigma_x^2\sigma_y^2)^{L/2}} \prod_{i=1}^L \frac{1}{\sqrt{\left(\frac{1}{2\sigma_x^2} + j\omega_i\right)\left(\frac{1}{2\sigma_y^2} + j\omega_i\right)}}$$

#### D. Probability Distribution Analysis

Receiver In this analysis correlation between the fading envelopes  $\alpha_l$  ( $l = 1, 2$ ) is assumed. A general expression for the combined output SNR  $\gamma_{MRC}$  is given in below Equation. It can be expressed for the dual diversity case as

$$\gamma_{MRC} = \frac{E_b}{N_0} (\alpha_1^2 + \alpha_2^2)$$

An expression for the PDF of  $\gamma_{MRC}$  i.e.  $f_{\gamma_{MRC}}(\gamma_{MRC})$ , when  $\alpha_1$  and  $\alpha_2$  are correlated with correlation coefficient  $\rho$  can be obtained using the complex Gaussian model of Hoyt RV in [13]. Using the PDF  $f_{\gamma_{MRC}}(\gamma_{MRC})$ , performance measures such as average output SNR, outage probability and ABER for binary, coherent and non-coherent modulations are derived. PDF of Combiner Output Signal-to-Noise Ratio From above Equation, it can be observed that an expression for the PDF of  $\gamma_{MRC}$  can be obtained from the PDF of the RV  $\alpha_1^2 + \alpha_2^2$ . Using the complex Gaussian model for Hoyt distribution, an expression for the joint CF of RVs  $\alpha_1^2$  and  $\alpha_2^2$  is reproduced below.

$$\times \left[ \frac{\rho}{\sqrt{8}\sigma_x^2(1-\rho^2)} \right]^{2(k+t)} \frac{1}{\left[ \left( \frac{1}{2(1-\rho^2)\sigma_x^2} + j\omega_1 \right) \left( \frac{1}{2(1-\rho^2)\sigma_y^2} + j\omega_1 \right) \right]^{t+\frac{1}{2}}}$$

An expression for the PDF of  $\alpha^2 = \alpha_1^2 + \alpha_2^2$  can be obtained by substituting  $\omega_1 = \omega_2 = \omega$  in above Equation and subsequently taking the inverse Fourier transform to the resulting expression. This can be given as

$$f_{\alpha^2}(\alpha^2)$$

$$= \frac{1}{8\pi(1-\rho^2)(\sigma_x\sigma_y)^2} \sum_{k=0}^{\infty} \sum_{t=0}^{\infty} \frac{(2k-1)!!(2t-1)!!}{k!t!}$$

$$\times \left[ \frac{\rho}{\sqrt{8}\sigma_x^2(1-\rho^2)} \right]^{2(k+t)} \frac{e^{j\omega\alpha}}{\left( \frac{1}{2(1-\rho^2)\sigma_x^2} + j\omega \right)^{2k+1} \left( \frac{1}{2(1-\rho^2)\sigma_y^2} + j\omega \right)^{2t+1}}$$

The combined output SNR can be given as  $\gamma_{MRC} = \left( \frac{Eb}{N_0} \right) \alpha^2$ . Thus, the PDF of  $\gamma_{MRC}$  can be obtained by scaling equation corresponding to the multiplying factor  $Eb/N_0$ , applying the concept of transformation of RVs. For identical branch average power i.e.  $\Omega_1 = \Omega_2 = \Omega$  (equivalently,  $\bar{\gamma}_1 = \bar{\gamma}_2 = \bar{\gamma}_3 \dots = \bar{\gamma}$ ), it can be shown that  $Eb/N_0 = \bar{\gamma}/(1+q^2)$ . Substituting this relation, subsequent to the transformation of RV, an expression for  $f_{\gamma_{MRC}}(\gamma_{MRC})$  can be obtained as



$$f_{\gamma_{mrc}}(\gamma_{mrc}) = \left( \frac{1+q^2}{2q\sqrt{(1-\rho^2)\gamma}} \right)^2 \sum_{k=0}^{\infty} \sum_{t=0}^{\infty} \frac{(2k-1)!!(2t-1)!!}{k!t!(2(k+t+1))} \times \left[ \frac{\rho(1+q^2)}{\sqrt{8\gamma}(1-\rho^2)} \right]^{2(k+t)}$$

#### E. Outage Probability

Outage probability is an important performance measure of any communication receiver. For the output SNR, it is defined as the probability that the output SNR  $\gamma$ , falls below a certain threshold value  $\gamma_{th}$ . Mathematically, it can be given as

$$P_{out}(\gamma_{th}) = \int_0^{\gamma_{th}} f_{\gamma}(\gamma) d\gamma$$

Putting  $f_{\gamma_{mrc}}(\gamma_{mrc})$  from previous equation into this equation, an expression for the outage probability for correlated dual-MRC receiver can be expressed as

$$P_{out}(\gamma_{th}) = \left( \frac{1+q^2}{2q\sqrt{(1-\rho^2)\gamma}} \right)^2 \sum_{k=0}^{\infty} \sum_{t=0}^{\infty} \frac{(2k-1)!!(2t-1)!!}{k!t!(2(k+t+1))} \times \left[ \frac{\rho(1+q^2)}{\sqrt{8\gamma}(1-\rho^2)} \right]^{2(k+t)} \times \int_0^{\gamma_{th}} e^{-\frac{(1+q^2)}{2q\sqrt{(1-\rho^2)\gamma}} \gamma_{mrc}} \gamma_{mrc}^{2k+2t+1} F_1\{2k+1; 2(k+t+1); \frac{1-q^4}{2q^2\gamma(1-\rho^2)} \gamma_{mrc}\} d\gamma_{mrc}$$

where  $\gamma_{th}$  is the threshold value of the combined output SNR. The integral in Equation cannot be solved in the given form. By expressing the hyper geometric function in infinite series, above equation can be rewritten as

$$P_{out}(\gamma_{th}) = \left( \frac{1+q^2}{2q\sqrt{(1-\rho^2)\gamma}} \right)^2 \sum_{k=0}^{\infty} \sum_{t=0}^{\infty} \frac{(2k-1)!!(2t-1)!!}{k!t!(2(k+t+1))} \times \left[ \frac{\rho(1+q^2)}{\sqrt{8\gamma}(1-\rho^2)} \right]^{2(k+t)} \times \int_0^{\gamma_{th}} \gamma_{mrc}^{2k+2t+r+1} e^{-\frac{1+q^2}{2q^2\gamma(1-\rho^2)} \gamma_{mrc}} d\gamma_{mrc}$$

#### IV. RESULT

We have earlier noticed that nakagami-q channel or hoyt fading channel is the mathematical formulation of fading in satellite link or other fading which is more similar to actual signal losses. In previous chapter we have described mathematically the hoyt fading channel and its derivation for outage probability for correlated hoyt fading channels. Results have been analysed by outage probability and bit error rate. We have observed the performance of hoyt fading channel considering M-ary modulation and MRC.

MATLAB R2013a has been used as a simulation tool as it provides a wide range of designed mathematical functions which proved to be useful in calculation of channel response. For example the complex calculation of outage probability for MRC is made easier by MATLAB's hypergeometric function, zeroth order Bessel function and gamma function.

##### CASE I- M-ARY MODULATION IN HOYT FADING CHANNEL

We have tested the performance of nakagami-q channel for 16-PSK modulation. The input data for a short interval is shown in figure 5. The constellation diagram for it is shown in figure 6.

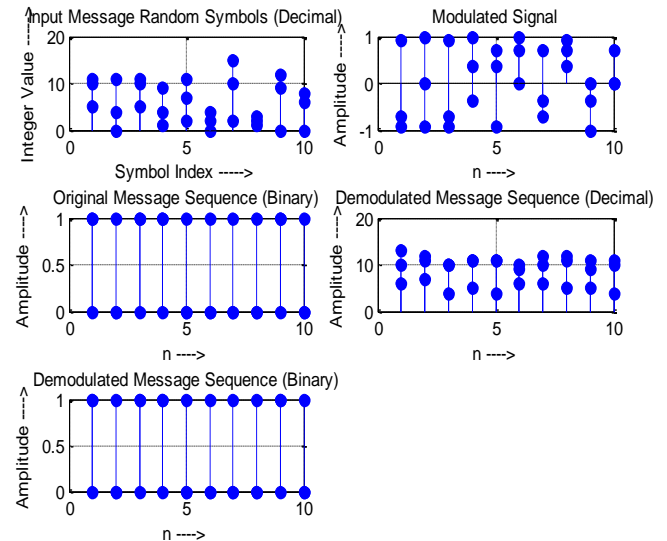


Figure 6: 16-PSK modulated input symbol

Constellation diagram provides a graphical representation of the complex envelope of each possible Symbol state. The x-axis of the constellation diagram represents the in-phase component of the complex envelope and the y-axis represents the quadrature component of the complex envelope. The distance between the signals on the constellation diagram relates to how different the modulation waveform are, and how well a receiver can differentiate between all possible symbols when random noise is present.

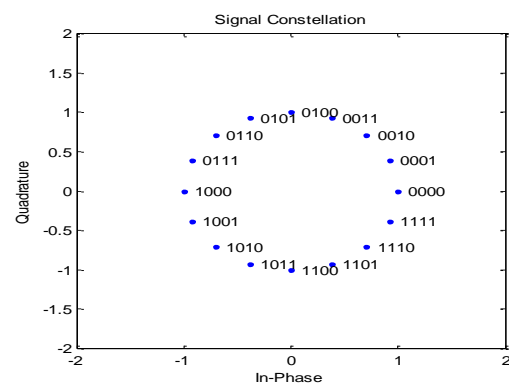


Figure 7: constellation diagram of 16-ary PSK modulation

In the previous chapter the channel response of hoyt fading channel depends upon the hoyt fading parameter. Variation in this value results in change in pdf of channel. Fading parameter ( $q$ ) is the ratio of unequal variances  $\sigma_x$  and  $\sigma_y$ . A channel response for hoyt channel is shown in figure 8. As per central limit theorem if there is sufficiently much scatter, the channel impulse response will be well-modelled as a Gaussian process irrespective of the distribution of the individual components. If there is no dominant component to the scatter, then such a process will have zero mean and phase evenly distributed between 0 and  $2\pi$  radians. The envelope of the channel response will therefore be Hoyt distributed. In this case for  $q=0.2$  is more similar to Gaussian distribution. The

response curve is not ideal which is in case when random variable alpha is 1. We have tested this on different value of alpha which are:

RV alpha	0.0539909665336576	0.247921068062695	0.342198280312217
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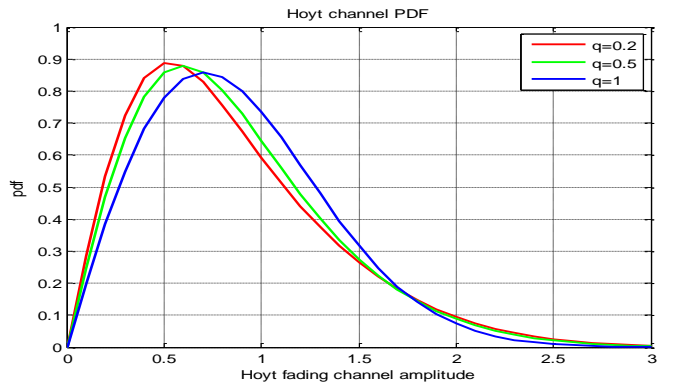


Figure 8: channel response of nakagami -q channel

The outage probability curve for 16- ary PSK modulation is shown in figure 9. the outage occurs if signal drops below the noise power level. From the figure it is clear that with variation of correlation coefficient  $\rho$ , higher values provides less outage probability which means less loss of signal whereas for it is highest for combination of fading coefficient value 1 and correlation coeff =0. From this simulation curve 16- ary PSK modulation it is proved that if fading coeff (q) has range in between 0.4-0.5 and correlation coefficient  $\rho$  is 1 then outage in signal will be least. A bit error rate curve for this case is shown in figure 10. it must be kept in consideration here that the M-ary simulation has been checked for single transmitter and receiver antenna. The bit error rate curve in 4.5 shows that minimum value is for q=0.5, which is in accordance with outage probability. To validate the simulation results we have tested the M-ary results for 4 and 32 PSK as shown in table 4.1. These simulation curves of outage probability also proves that for q=1 and  $\rho = 0$ , outage probability is highest in hoyt fading channel. Here  $\rho = 0$  represents the un-correlation case as it is correlation coefficient. So in other words for uncorrelated case the hoyt fading channel performs least.

#### Case II: MRC monte carlo simulation

The next case considered is MRC scheme with monte carlo simulation. In this case we have considered 2 receivers with BPSK modulation. Results have been shown in figure 11 and 1.7 for outage probability and bit error rate. These are checked for different values of L, q and  $\rho$ . for now only 2 receivers case is being analysed, but the script developed is dynamic and can be used for more number of receivers.

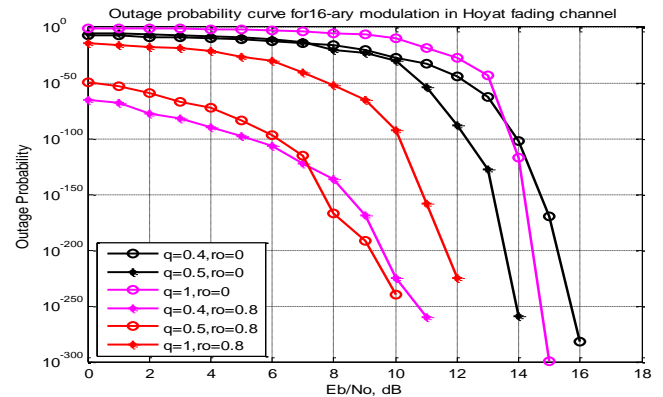


Figure 9: outage probability curve for 16-ary simulation of Hoyt fading channel

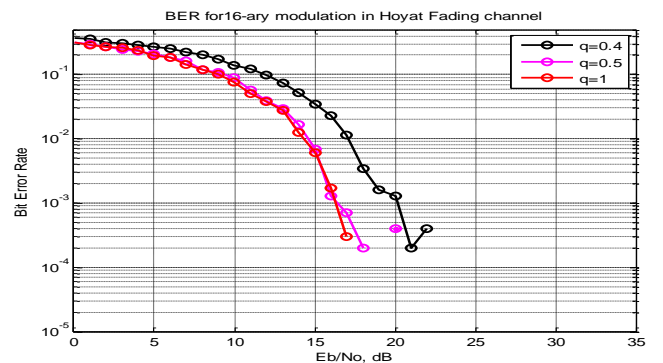


Figure 10: BER curve for 16-ary simulation of Hoyt fading channel

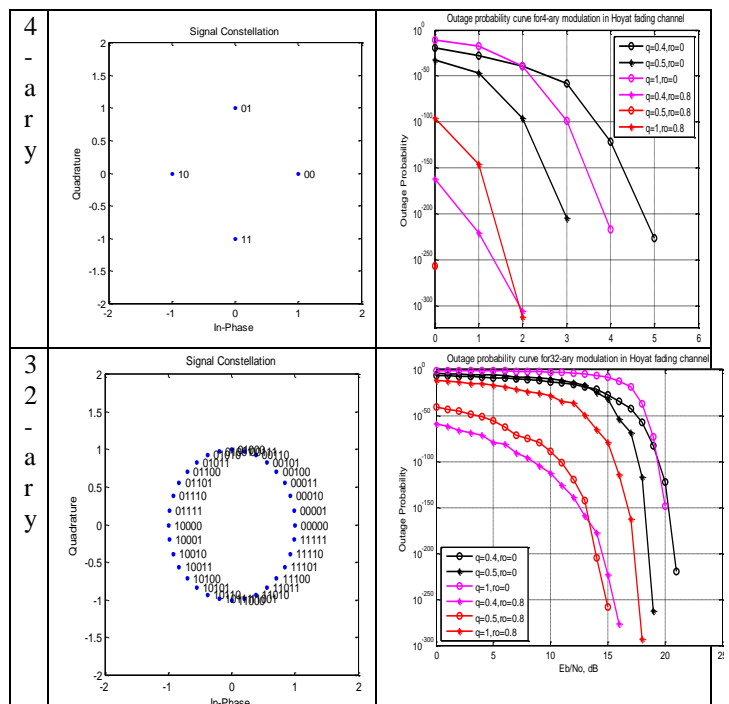


Figure 11: MRC with monte carlo

The effect of branch correlation on the outage can be observed by comparing the outage values for  $\rho = 0.8$  against the values for  $\rho = 0$  (uncorrelated case). Clearly, with the increase in  $\rho$  the receiver suffers more outage, for a fixed value of  $q$  and  $L$ . Again as expected, increase in input branches reduces the probability of outage. The least outage probability is observed at  $q=0.5$ ,  $\rho = 0.8$  and  $L=2$  & maximum outage probability is at  $q=0.4$ ,  $\rho = 0$  and  $L=1$ . Similar is the case with BER, for  $q=0.4$  and  $L=1$ , it is highest and  $q=1$  and  $L=2$ , it is lowest as shown in figure 12. So increasing the number of receivers lower the effect of fading in Hoyt fading channel which fulfil the MRC purpose since MRC is used to reduce the noise effect in transmitted signal.

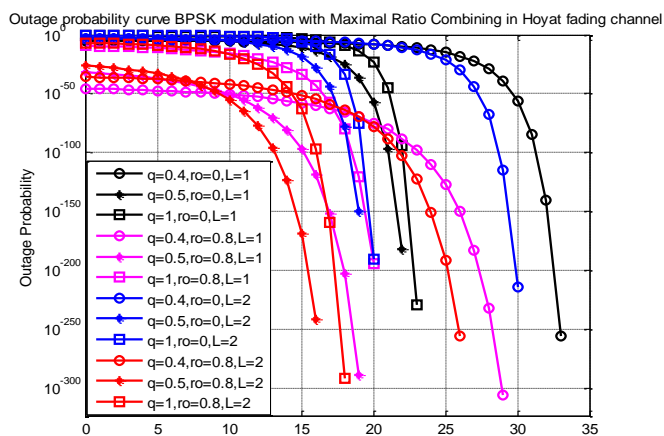


Figure 12: outage probability curve for MRC in hoyt fading channel

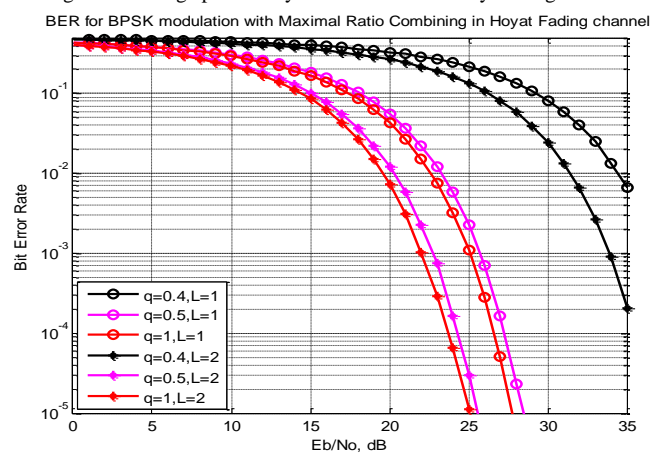


Figure 13: BER for MRC in hoyt fading channel

## V. CONCLUSION

Hoyt fading channel is more realistic satellite link channel. In this work, Performance of M-ary modulation scheme and MRC diversity receivers are analyzed over Hoyt fading channels. Focusing on the analytical approach, mathematical expressions for various performance measures such as outage probability and BER of diversity receivers have been obtained. The PDF based analytical approach has been preferred in all analyses for these performance measures, wherever possible. It is stressed to analyze diversity receivers with arbitrary order of diversity with correlated fading channels since these cases

are encountered frequently in the field deployment of diversity receivers. Results are compared with various correlation coefficients value of Hoyt fading channel and different number of receiver antennas and different set of fading coefficients. It has been observed that in case of M-ary simulation with  $M=16$ , fading coeff ( $q$ ) has range in between 0.4-0.5 and correlation coefficient  $\rho$  is 1 for least outage probability. These values are validated by checking on 4-ary and 32-ary simulation too.

In case of MRC scheme, 2 receivers are compared for different values of  $q$  and  $\rho$ . It is observed that with increase in number of antennas, outage probability and BER decreases. The least outage probability is observed at  $q=0.5$ ,  $\rho = 0.8$  and  $L=2$  & maximum outage probability is at  $q=0.4$ ,  $\rho = 0$  and  $L=1$ . These results are successfully simulated using MATLAB's communication toolbox.

## REFERENCES

- [1]. Rupaban Subadar and P. R. Sahu, "Performance of L-MRC Receiver over Equally Correlated Hoyt Fading Channels", IETE JOURNAL OF RESEARCH, VOL 57, ISSUE 3, MAY-JUN 2011
- [2]. Vladeta Milentijević1, Dragan Denić1, Mihajlo Stefanović1, Stefan R. Panić2, Dragan Radenković, "Relative Measurement Error Analysis in the Process of the Nakagami-  $m$  Fading Parameter Estimation", SERBIAN JOURNAL OF ELECTRICAL ENGINEERING Vol. 8, No. 3, November 2011, 341-349
- [3]. Suvarna P. Jadhav, Vaibhav S. Hendre, "Performance of Maximum ratio combining (MRC) MIMO Systems for Rayleigh Fading Channel", International Journal of Scientific and Research Publications, Volume 3, Issue 2, February 2013
- [4]. D.B. Smith and T.D. Abhayapala, "Maximal ratio combining performance analysis in practical Rayleigh fading channels", IEE Proc.-Commun., Vol. 153, No. 5, October 2006
- [5]. R. Subadar and P. R. Sahu, "Performance of L-MRC receiver over independent Hoyt fading channels," Communications (NCC), 2010 National Conference on, Chennai, 2010, pp. 1-5.
- [6]. G. K. Karagiannidis, N. C. Sagias and D. A. Zogas, "Error analysis of M-QAM with equal-gain diversity over generalised fading channels," in IEE Proceedings - Communications, vol. 152, no. 1, pp. 69-74, 24 Feb. 2005.
- [7]. V. G. Venkatesan1, S. Karthik2, P. Agilan, "Performance Comparison of L-MRC Receivers over Nakagami-M Fading and Hoyt Fading Channels", International Journal of Science and Research (IJSR), Volume 2 Issue 3, March 2013.
- [8]. In-Ho Lee, "SER Performance of Enhanced Spatial Multiplexing Codes with ZF / MRC Receiver in Time-Varying Rayleigh Fading Channels", The Scientific World Journal Volume 2014.
- [9]. Wamberto J. L. Queiroz, Francisco Madeiro, Waslon Terllizze A. Lopes, Member, IEEE, and Marcelo S. Alencar, Senior-Member, IEEE, "Error Probability of Multichannel Reception with  $\theta$ -QAM Scheme Under Correlated Nakagami-m Fading, JOURNAL OF COMMUNICATIONS AND INFORMATION SYSTEMS, VOL. 29, NO. 1, MAY 2014"
- [10]. R. Deepa, Dr.K.Baskaran, Pratheek Unnikrishnan, Aswath Kumar, "Study Of Spatial Diversity Schemes In Multiple Antenna Systems", Journal of Theoretical and Applied Information Technology, 2009
- [11]. A K M Arifuzzman, Md. Anwar Hossain, Nadia Nowshin, Mohammed Tarique, "A COMPARATIVE PERFORMANCE ANALYSIS OF MRC DIVERSITY RECEIVERS IN OFDM SYSTEM" International Journal of Distributed and Parallel Systems (IJDPSS) Vol.2, No.4, July 2011.

- [12]. Vivek K. Dwivedi, Pradeep Kumar, and G. Singh, "Performance Analysis of OFDM Communication System over Correlated Nakagami- $m$  Fading Channel", PIERS Proceedings, Beijing, China, March 23–27, 2009.
- [13]. Surbhi Sharma, Palvinder Singh, "Analysis of MRC and OC with OFDM In Terms Of BER Using Different Modulation Techniques over Rayleigh Channel", International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering (An ISO 3297: 2007 Certified Organization) Vol. 3, Issue 6, June 2014
- [14]. Satyendra Chadokar, Pravin Barmashe, "Performance Evaluation of Equalizers and Different Diversity Techniques using OFDM", International Journal of Computer Technology and Electronics Engineering (IJCTEE), Volume 1, Issue 3, 2013
- [15]. Marco Krondorf, Gerhard Fettweis, "OFDM Link Performance Analysis under Various Receiver Impairments", EURASIP Journal on Wireless Communications and Networking, December 2007
- [16]. Juan M. Romero-Jerez, Senior Member, IEEE, and F. Javier Lopez-Martinez, Member, IEEE, "A New Framework for the Performance Analysis of Wireless Communications under Hoyt (Nakagami- $q$ )", arXiv:1403.0537v3 [cs.IT] 5 May 2015
- [17]. D. A. Zogas, G. K. Karagiannidis and S. A. Kotsopoulos, "Equal gain combining over Nakagami- $n$  (rice) and Nakagami- $q$  (Hoyt) generalized fading channels," in *IEEE Transactions on Wireless Communications*, vol. 4, no. 2, pp. 374-379, March 2005.
- [18]. Jos'e F. Paris and David Morales-Jim'enez, "Outage Probability Analysis for Nakagami-(Hoyt) Fading Channels under Rayleigh Interference", IEEE TRANSACTIONS ON WIRELESS COMMUNICATIONS, VOL. 9, NO. 4, APRIL 2010.
- [19]. R. M. Radaydeh and M. M. Matalgah, "Average BER Analysis for  $M$ -ary FSK Signals in Nakagami- $Q$  (Hoyt) Fading With Noncoherent Diversity Combining," in *IEEE Transactions on Vehicular Technology*, vol. 57, no. 4, pp. 2257-2267, July 2008.
- [20]. Li Tang Zhu Hongbo, Analysis and Simulation of Nakagami Fading Channel with MATLAB", Asia-Pacific Conference on Environmental Electromagnetics CEEM 2003, China.
- [21]. Gayarti S. Prabhu and P. Mohana Shankar "simulation of flat fading using MATLAB for classroom instruction" IEEE Transactions on Education Vol. 45, No. 1, Feb. 2002.
- [22]. Md. Golam Sadeque, Shadhon Chandra Mohonta, Md. Firoj Ali, "Modeling and Characterization of Different Types of Fading Channel", International Journal of Science, Engineering and Technology Research (IJSETR)