

# Inverse Band Reject and All Pass Filter Structure Employing CMOS CDBAs

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**Abstract**— In this paper a new voltage-mode (VM) circuit for the realization of second order tuneable inverse band reject filter (IBRF) and inverse all pass filter (IAPF) have been introduced. The proposed circuit uses two current differencing buffered amplifiers (CDBA), two capacitors and four/five resistors. PSPICE simulation results employing CMOS CDBA implemented in 0.18 $\mu$ m CMOS TSMC technology have been presented to validate the workability of the configuration.

**Keywords**— Analog Inverse Filters, Current Differencing Buffered Amplifier, Analog Signal Processing

## I. INTRODUCTION

An analog inverse filter provides frequency selective characteristics which are opposite to those of the corresponding analog filter. These inverse filters are used to remove the effect of distortion introduced in the signal while it is processed through a system. Inverse filters find applications in control, instrumentation and communication systems [1]. Recently, a number of analog inverse active filters with different properties have been realised with different active building blocks (ABB) like operational amplifiers (op-amps) [2], current feedback operational amplifiers (CFOAs) [3]-[7], second generation current conveyors CCIIs [8], [9], four terminal floating nullors (FTFNs) [10], [11], operational transresistance amplifiers (OTRAs) [13], [14] current differencing buffered amplifiers (CDBAs) [15], [16], current differencing transconductance amplifiers CDTAs [17], [18], operational transconductance amplifiers OTAs [19], differential difference current conveyors (DDCCs) [20] and voltage differencing transconductance amplifiers (VDTAs) [21]. However, there are few number of research publications for realising second order IBRF [3], [4], [7], [12], [14], [16] and IAPF [11], [12] and [14].

The CDBA has received prominent attention in analog signal processing and signal generation circuits due to its important property of providing at its input terminals virtual ground, which eliminates the effect of parasitic at the input terminals. Apart from this, its low output impedance enables the CDBA based circuit configurations to be cascaded easily.

From existing literature survey, it has been observed that only two circuit structures have been reported so far to

realize second-order inverse active filters employing CDBAs [15], [16]. [15] has reported two CDBA based second order inverse low pass filter (ILPF) with four resistors and two capacitors, inverse high pass filters (IHPF) using two resistors and four capacitors and inverse band pass filter (IBPF) with three resistors and three capacitors whereas in [16] the ILPF circuit is realized with four resistors and two capacitors the other four circuits namely, IHPF, IBPF, IBRF and IAPF have been realised with 3-4 capacitors and 2-4 resistors. Also none of these two reported inverse filters have utilized the intrinsic (current differencing) property of the CDBA, as n-terminal of one of the CDBA has been left open resulting into employment of more than two capacitors for realization of second order inverse filters of different types in many cases (IBPF, IHPF, IBRF and IAPF).

Therefore, the purpose of this communication is to present a new inverse filter circuit configuration employing two CDBAs with their intrinsic (current differencing) property fully utilized, four/five resistors and only two capacitors along with a switch. The realised second order IBRF has independent control of cut-off frequency and bandwidth while IAPF has independent tunability of cut-off frequency. The workability of the presented inverse filters has been verified using PSPICE simulations implemented in TSMC 0.18 $\mu$ m CMOS technology.

## II. THE PROPOSED CONFIGURATION

The symbolic representation of the CDBA is shown in Fig. 1, where p and n are current input terminals (with ideally zero input impedances), w is the voltage output terminal (ideally zero output impedance) and z is the current output terminal (ideally infinite output impedance).

The characterising terminal equations of an ideal CDBA are given by:

$$I_z = (I_p - I_n), V_p = 0 = V_n \text{ and } V_w = V_z \quad (1)$$

The proposed configuration for the realization of IBRF and IAPF with two capacitors and four/five resistors is shown in Fig. 2.

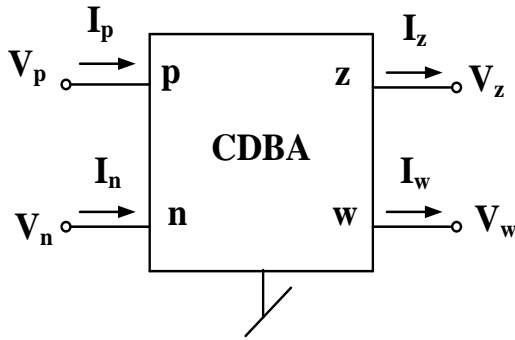


Fig. 1 Symbolic representation of CDBA

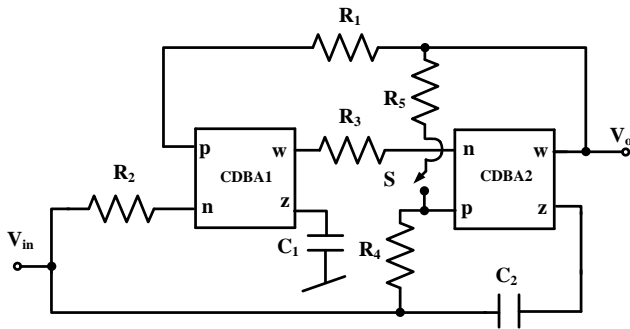


Fig. 2. The proposed inverse filter structure

Realization of IBRF and IAPF responses from Fig. 2 is as follows:

**Case I:** When switch ‘S’ is open the resulting transfer function becomes

$$\frac{V_o(s)}{V_{in}(s)} = \frac{1}{s^2 + \frac{1}{R_1 R_3 C_1 C_2}} \quad (2)$$

which represents an IBRF with cut-off frequency ( $\omega_0$ ) and bandwidth (BW) given by:

$$\omega_0 = \frac{1}{\sqrt{R_2 R_3 C_1 C_2}} \quad \text{For } R_1 = R_2 \quad (3)$$

$$BW = \frac{1}{R_4 C_2}$$

**Case II:** When switch ‘S’ is closed the resulting transfer function will be given by:

$$\frac{V_o(s)}{V_{in}(s)} = \frac{1}{s^2 - \frac{1}{R_7 C_6} s + \frac{1}{R_1 R_3 C_1 C_2}} \quad (4)$$

which realizes an IAPF with  $\omega_0$  and BW given by:

$$\omega_0 = \frac{1}{\sqrt{R_2 R_3 C_1 C_2}} \quad \text{For } R_1 = R_2 \quad (5)$$

$$BW = \frac{1}{R_4 C_2} \quad \text{For } R_4 = R_5$$

Thus, it is clear that from equation (3), both  $\omega_0$  and BW can

be tuned independently i.e.  $\omega_0$  through  $R_3/C_4$  and BW through  $R_4$

### III. NON-IDEAL ANALYSIS

The non-ideal representation of the CDBA taking into account the parasitic at various terminals is shown in Fig.3, where parallel combination of  $R_z$  and  $1/sC_z$  is the parasitic impedance at port z,  $R_p$  and  $R_n$  are the parasitic resistances at terminals p and n respectively and  $R_o$  is the parasitic output resistance at terminal w.

A practical CDBA can be described [22] by the following relationships that take into account the non-idealities of the device:

$$V_p = V_n = 0, I_z = \beta_p I_p - \beta_n I_n \text{ and } V_w = \alpha V_z \quad (6)$$

where  $\beta_p = (1 - \epsilon_p)$  and  $\epsilon_p (|\epsilon_p| \ll 1)$  is the current tracking error from p-terminal to z-terminal,  $\beta_n = (1 - \epsilon_n)$  where  $\epsilon_n (|\epsilon_n| \ll 1)$  is the current tracking error from n-terminal to z-terminal, and  $\alpha = (1 - \epsilon_v)$  with  $\epsilon_v (|\epsilon_v| \ll 1)$  is the voltage tracking error from z-terminal to w-terminal of the CDBA. In addition to the above, if we also consider parasitic impedances at z-terminal and parasitic resistances at p, n and w terminals of CDBA as shown in Fig. 3 and reanalyze the circuits of Fig. 2, we get the following non-ideal transfer functions of inverse active filters:

The non-ideal expression of IBRF is given by

$$\left. \frac{V_o(s)}{V_{in}(s)} \right|_{\text{IBRF}} = \frac{1}{s^2 + Bs + C} \quad (7)$$

where

$$B = \frac{1}{\alpha_2 C_1 (C_2 + C_{Z2}) + \alpha_2 C_{Z1} (C_2 + C_{Z2})} \left( \frac{C_1}{R_{Z2}} + \frac{C_{Z1}}{R_{Z2}} + \frac{C_2}{R_{Z1}} + \frac{C_{Z2}}{R_{Z1}} \right)$$

$$C = \frac{1}{\alpha_2 C_1 (C_2 + C_{Z2}) + \alpha_2 C_{Z1} (C_2 + C_{Z2})} \left( \frac{\alpha_1 \alpha_2 \beta_{n1} \beta_{p2}}{R_1 R_3} \right)$$

$$M = \frac{1}{\alpha_2 C_1 (C_2 + C_{Z2}) + \alpha_2 C_{Z1} (C_2 + C_{Z2})} \left( \frac{\alpha_2 C_1}{R_{Z2}} + \frac{\alpha_2 C_{Z1}}{R_{Z2}} + \frac{\alpha_2 C_2}{R_{Z1}} + \frac{\alpha_2 C_{Z2}}{R_{Z1}} + \frac{C_4 \beta_{p2}}{R_4} + \frac{C_{Z1} \beta_{p2}}{R_4} \right)$$

$$N = \frac{1}{\alpha_2 C_1 (C_2 + C_{Z2}) + \alpha_2 C_{Z1} (C_2 + C_{Z2})} \left( \frac{\alpha_1 \alpha_2 \beta_{n1} \beta_{n2}}{R_2 R_3} + \frac{\alpha_2}{R_{Z2} R_{Z1}} \right)$$

The non-ideal expressions of IAPF when switch ‘S’ is closed:

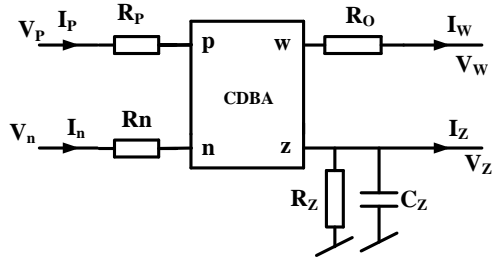


Fig. 3. Non-ideal CDDBA with Parasitic elements

$$\left. \frac{V_O(s)}{V_{in}(s)} \right|_{IAPF} = \frac{1}{\alpha_2} \frac{1}{s^2 + Bs + C} \quad (8)$$

where

$$B = \frac{1}{\alpha_2 C_1 (C_2 + C_{Z2}) + \alpha_2 C_{Z1} (C_2 + C_{Z2})} \left( \frac{C_1}{R_{Z2}} + \frac{C_{Z1}}{R_{Z2}} + \frac{C_2}{R_{Z1}} + \frac{C_{Z2}}{R_{Z1}} - \frac{\alpha_2 \beta_{p2} (C_4 + C_{Z1})}{R_4} \right)$$

$$C = \frac{1}{\alpha_2 C_1 (C_2 + C_{Z2}) + \alpha_2 C_{Z1} (C_2 + C_{Z2})} \left( \frac{\alpha_1 \alpha_2 \beta_{n1} \beta_{p2}}{R_1 R_3} - \frac{\alpha_2 \beta_{p2}}{R_{Z1} R_4} \right)$$

$$M = \frac{1}{\alpha_2 C_1 (C_2 + C_{Z2}) + \alpha_2 C_{Z1} (C_2 + C_{Z2})} \left( \frac{\alpha_2 C_4}{R_{Z2}} + \frac{\alpha_2 C_{Z1}}{R_{Z2}} + \frac{\alpha_2 C_6}{R_{Z1}} + \frac{\alpha_2 C_{Z2}}{R_{Z1}} + \frac{C_4 \beta_{p2}}{R_4} + \frac{C_{Z1} \beta_{p2}}{R_4} \right)$$

$$N = \frac{1}{\alpha_2 C_1 (C_2 + C_{Z2}) + \alpha_2 C_{Z1} (C_2 + C_{Z2})} \left( \frac{\alpha_1 \alpha_2 \beta_{n1} \beta_{n2}}{R_2 R_3} + \frac{\alpha_2}{R_{Z2} R_{Z1}} \right)$$

Since the value of  $R_z$  is very high and the value of  $C_z$  is very low, therefore, the inverse filter transfer functions can be approximated as:

$$\left. \frac{V_O(s)}{V_{in}(s)} \right|_{IBRF} \cong \frac{1}{\alpha_2} \frac{1}{s^2 + \frac{\alpha_1 \beta_{n1} \beta_{p2}}{R_1 R_3 C_1 C_2} s + \frac{\alpha_1 \alpha_2 \beta_{n1} \beta_{p2}}{C_1 C_2 R_2 R_3}} \quad (9)$$

which realizes IBRF with cut-off frequency ( $\overline{\omega_0}$ ) and bandwidth ( $\overline{BW}$ ) given by:

$$\overline{\omega_0} = \sqrt{\frac{\alpha_1 \alpha_2 \beta_{n1} \beta_{n2}}{C_1 C_2 R_2 R_3}} = \omega_0 \sqrt{\alpha_1 \alpha_2 \beta_{n1} \beta_{n2}} \quad \text{For } R_1 = R_2$$

$$\overline{BW} = \frac{\beta_{p2}}{C_2 R_4} = \beta_{p2} BW \quad (10)$$

and

$$\left. \frac{V_O(s)}{V_{in}(s)} \right|_{IAPF} \cong \frac{1}{\alpha_2} \frac{1}{s^2 + \frac{\beta_{p2}}{C_2 R_4} s + \frac{\alpha_1 \alpha_2 \beta_{n1} \beta_{p2}}{C_2 C_4 R_1 R_3}} \quad (11)$$

which realizes IAPF for with  $\overline{\omega_0}$ , and  $\overline{BW}$  given by:

$$\overline{\omega_0} = \sqrt{\frac{\alpha_1 \alpha_2 \beta_{n1} \beta_{n2}}{C_1 C_2 (1 + \beta_{n1}) R_2 R_3}}$$

$$= \omega_0 \sqrt{\frac{\alpha_1 \alpha_2 \beta_{n1} \beta_{n2}}{(1 + \beta_{n1})}} \quad \text{For } R_1 = R_2 \quad (12)$$

$$\overline{BW} = \frac{\beta_{p2}}{C_2 R_4} = \beta_{p2} BW \quad \text{For } R_5 = R_4$$

Equations (10) and (12) reveal that the cut-off frequency, and bandwidth of the IBRF and IAPF are dependent on voltage/current tracking error coefficients of the CDDBA terminals, hence subsequently introduce errors in the  $\omega_0$  and  $BW$  of the inverse filters.

#### IV. SENSITIVITY ANALYSIS

The active and passive sensitivities of  $\omega_0$  and  $BW$  of inverse active filters (IBRF and IAPF) are tabulated in Table 1 which shows that the sensitivities with respect to active and passive components are small.

Table-1 Sensitivity analysis of inverse filters

Filter	Sensitivity
IBRF	$S_{R_2}^{\omega_0} = S_{R_3}^{\omega_0} = -\frac{1}{2}, S_{C_1}^{\omega_0} = S_{C_2}^{\omega_0} = -\frac{1}{2}, S_{R_1}^{\omega_0} = S_{R_4}^{\omega_0} = 0$
	$S_{\alpha_1}^{\omega_0} = S_{\alpha_2}^{\omega_0} = S_{\beta_{n2}}^{\omega_0} = \frac{1}{2}, S_{\beta_{p1}}^{\omega_0} = S_{\beta_{p2}}^{\omega_0} = 0$
	$S_{R_4}^{BW} = S_{C_2}^{BW} = -1, S_{R_2}^{BW} = S_{R_3}^{BW} = S_{C_4}^{BW} = 0$
	$S_{\beta_{p1}}^{BW} = 0, S_{\beta_{p2}}^{BW} = 1, S_{\alpha_1}^{BW} = S_{\alpha_2}^{BW} = S_{\beta_{n2}}^{BW} = 0$
IAPF	$S_{R_2}^{\omega_0} = S_{R_3}^{\omega_0} = -\frac{1}{2}, S_{C_1}^{\omega_0} = S_{C_2}^{\omega_0} = -\frac{1}{2},$
	$S_{R_1}^{\omega_0} = S_{R_4}^{\omega_0} = S_{R_5}^{\omega_0} = 0$
	$S_{\alpha_1}^{\omega_0} = S_{\alpha_2}^{\omega_0} = S_{\beta_{n2}}^{\omega_0} = \frac{1}{2}, S_{\beta_{p1}}^{\omega_0} = S_{\beta_{p2}}^{\omega_0} = 0$

#### V. SIMULATION RESULTS

The validity of the proposed inverse filters has been examined through PSPICE simulations using an exemplary CMOS CDDBA architecture derived from [23], shown here in Fig. 4. The DC power supplies used were  $\pm 2.5V$  and the bias current was taken  $40\mu A$ . The aspect ratios used for implementation of CDDBA are given in Table 2. The inverse filters were designed for a nominal value of the cut-off frequency of 159 kHz and quality factor  $Q = 1$ . The passive components were selected as  $C_1 = C_2 = 100pF$ ,  $R_1 = R_2 = R_3 = R_4 = R_5 = 10k\Omega$ . Fig. 5 displays the frequency responses of IBRF and Fig. 6 shows the gain and phase responses of IAPF. The tunability of cut-off frequency and quality factor

of the IBRF have been shown in Fig. 7 and Fig. 8 respectively. The input signal level during PSPICE simulations were kept at 1 V<sub>pp</sub>.

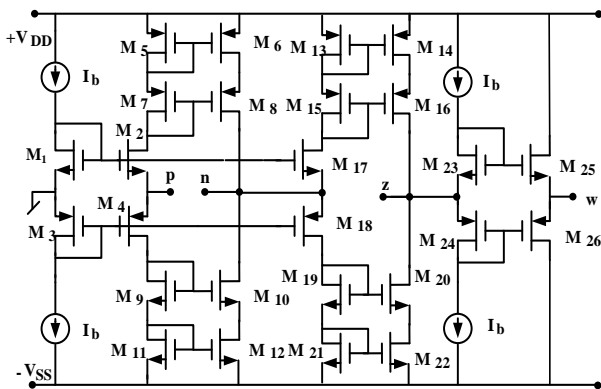


Fig.4 CMOS realization of CDBA derived from [23]

TABLE -2. Aspect ratios of MOSFETs used for realization of CDBA

MOSFETS	$\frac{W}{L}$ ratios
M <sub>1</sub> ,M <sub>2</sub> ,M <sub>17</sub> ,M <sub>23</sub> ,M <sub>25</sub>	50/0.5
M <sub>3</sub> ,M <sub>4</sub> ,M <sub>18</sub> ,M <sub>24</sub> ,M <sub>26</sub>	100/0.5
M <sub>5</sub> -M <sub>16</sub> ,M <sub>19</sub> -M <sub>22</sub>	3.33/0.5

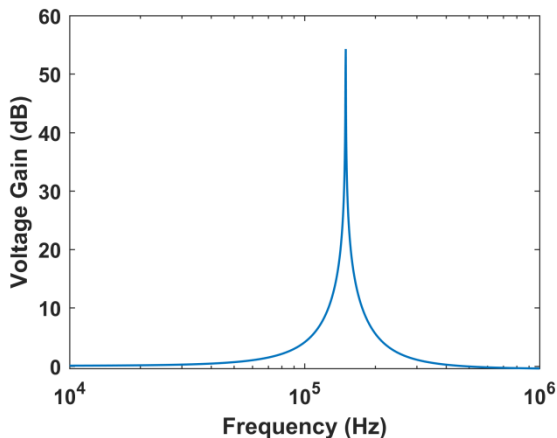


Fig. 5. Frequency responses of IBRF

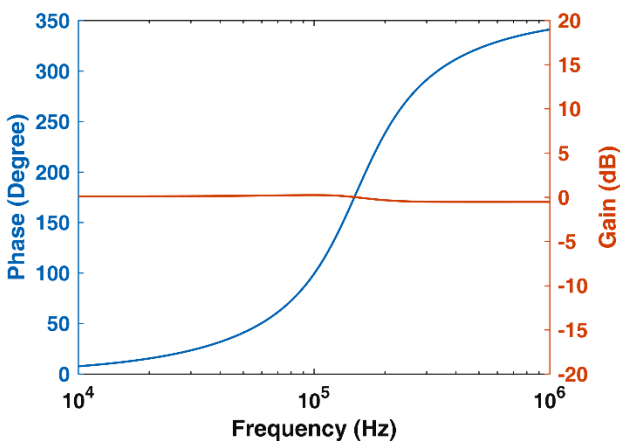


Fig. 6. Gain and phase responses of IAPF

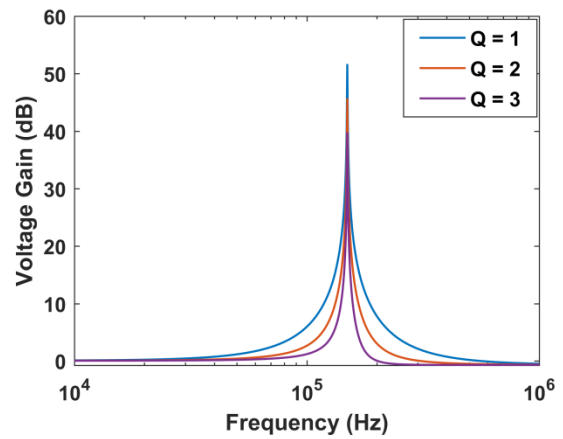


Fig. 7. Tunability of bandwidth for different value of Q for IBRF

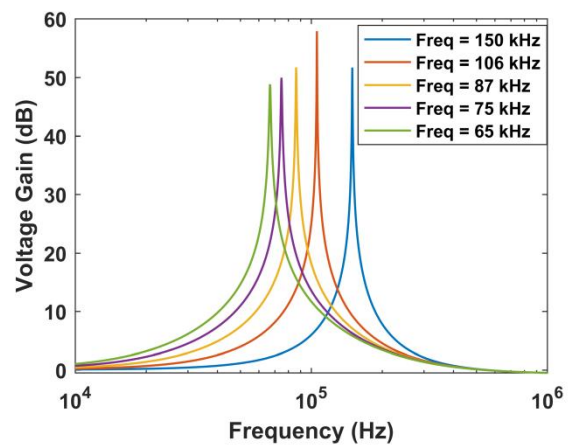
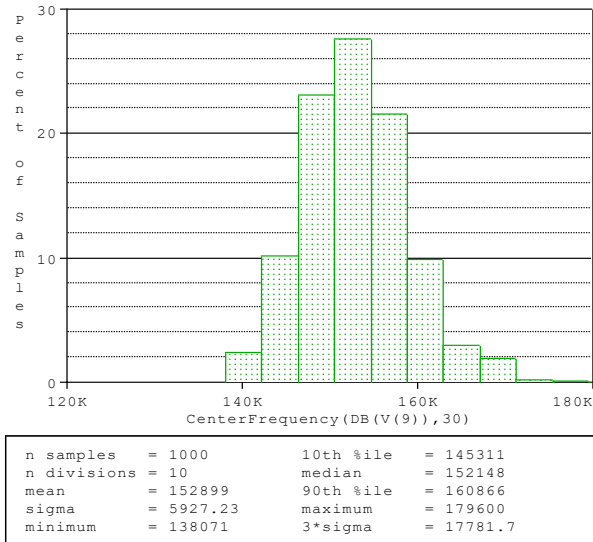
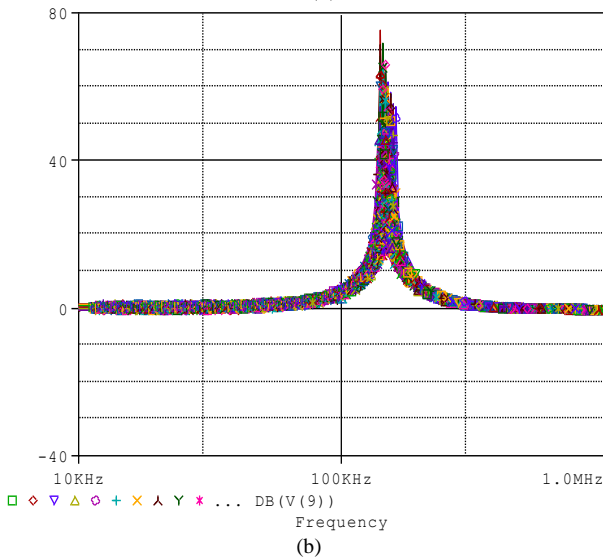


Fig. 8. Tunability of cut-off frequency for IBRF

The Monte Carlo simulation results of the inverse active filters showing variation of gain and cut-off frequency for 5% variation in resistance and capacitance values and have been displayed in Fig. 9 and Fig. 10 respectively. For IBRF the cut-off frequency obtained from the simulations was found to be 150 kHz while Monte Carlo analysis shows that median value of cut-off frequency as 152.148 kHz and similarly for IAPF corresponding to a simulated gain of 0 dB, the Monte Carlo analysis shows that median value of gain as 0.3 dB which shows that the mismatch in the passive component values do not have large effect on the cut-off frequency and gain.

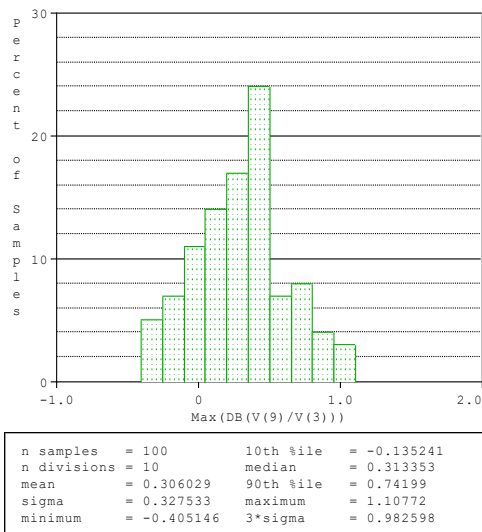


(a)

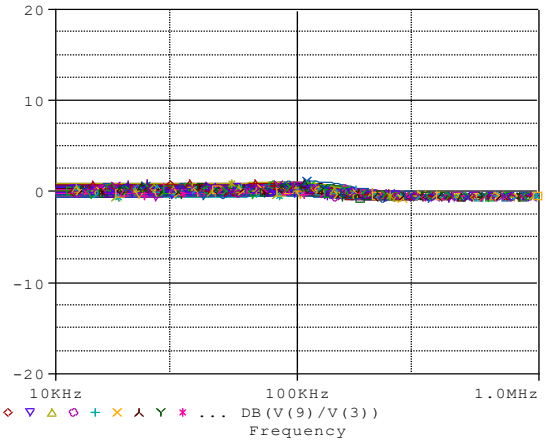


(b)

Fig. 9. Monte-Carlo analysis of IBRF showing variation of cut-off frequency for 5% variation in resistance and capacitance (a) Histogram (b) frequency response.



(a)



(b)

Fig. 10. Monte-Carlo analysis of IAPF showing variation of gain for 5% variation in resistance and capacitance (a) Histogram (b) frequency response.

## VI. CONCLUSIONS

A new VM analog circuit for realizing IBRF and IAPF response has been proposed employing two fully utilised CDBAs, two capacitors, four/five resistors and a switch. The proposed IBRF offers independent tunability of cut-off frequency and quality factor whereas, the IAPF has independent control of cut-off frequency. Non-ideal analysis of both the inverse filters has revealed that there is a little error in the cut-off frequency due to inclusion of the parasitic of the CDBAs. The active and passive sensitivities of presented inverse filters are low. The validity of inverse filters has been confirmed through PSPICE simulations using an exemplary CMOS CDBA architecture implemented in TSMC 0.18 $\mu$ m CMOS technology. These simulation results have been found to be in good agreement with the theoretical results.

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