Design of Digital PID Controller for Blood-Glucose Monitoring System

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Abstract - The objective of this paper is designing a digital PID controller based on Field Programmable Gate Array (FPGA) device for regulating blood glucose level of diabetic patients. The Zeigler’s Nichol method is used to tune the controller as a diabetic patient model in MATLAB and Simulink environment. Since the speed of controller has effect on their performance and stability, Field Programmable Gate Array (FPGA) device is considered. A Simulink to FPGA flow is applied to the structure of PID controller with simple Simulink blocks and Xilinx blocks in Simulink/Matlab. The results of blood glucose of diabetic patient model are simulated. System Generator tools are used for generating the HDL (Verilog) code. Xilinx Integrated Software Environment (ISE) tool is used to check the device utilization and timing analysis of the controller.

Key Words:- Digital PID controller, diabetic patients, blood glucose, Sumulink/MATLAB.

I. INTRODUCTION

Diabetes mellitus is a metabolic disease in which the body does not produce or properly use insulin. The pancreatic hormones insulin and glucagon which are secreted from β-cells and α-cells respectively are responsible for keeping the blood glucose concentration level in a normal range. There are 3 types of diabetes: type I and type II and Gestational diabetes. Type-I diabetes mellitus (TIDM) is a disease characterized by absence or death of the β-cells. High average glucose concentration (above 110mg/dL) is called Hyperglycaemia. Hypoglycaemia is a complication that occurs for TIDM when the blood glucose level is too low (less than 70 mg/dL). Since the β-cells are responsible to produce insulin, external insulin injections in TIDM are required to regulate the blood glucose level. Type-II diabetes mellitus occurs when the body does not respond or can’t use its own insulin. Gestational diabetes occurs in some pregnant women and is similar to type-II diabetes.

The frequently used controller is the PID controller. The word PID stands for Proportional-Integral-Differential control. Each of these, the P, I and D are terms in a control algorithm, and each term has a specific purpose. Sometimes certain terms are not considered because they are not needed in the control design. This is possible to have just a P control, PI or PID control. It is very rare to have an ID control. A PID controller calculates an “error” values as the difference between the measured variable and the set point. The control objective of the glucose-insulin system is shown in table 1. Since the speed of the control system depends on the system performance, stability and complexity FPGAs are the good choice since they are fast and power efficient. The organisation of this paper is as follows: in section II, Related work III, Designing of the controllers IV, Implementation in Simulink/MATLAB and Xilinx ISE design tool V, Simulation Results.

II. Related Work
1. In this thesis all the basics necessary to understand the working of the PID controller is provided. The different tuning methods have been implemented. [1]
2. In this paper, blood-glucose regulation controller using sliding mode techniques is presented. The robustness to the uncertainties makes this controller attractive in designing the insulin supplying pumps. [2]
3. In this paper, the PID controller design using classical method and Genetic Algorithm is presented.[3]
4. In this research, the blood glucose-insulin regulation model is designed based on Stolwijk and hardy’s dynamic model. [4]
5. This paper gives the design and implementation of FPGA based on PID controller has focused on building a multi-channel PID controller by FPGA’s. The main objective is to optimize the power consumption and delay due to PWM modulator and A/D. [5]
6. This paper presents tuning of PID controller based on Fruit Fly optimization Algorithm and Genetic algorithm and compared. [6]
7. In this paper, design and Implementation of Multiplierless digital PID controller. The proposed method is based on Distributed Arithmetic Architecture (DA). The architecture is implemented using SysGen and Implemented on to FPGA in VHDL. [7]

III. DESIGNING OF THE CONTROLLERS

The basic equation of the PID controller is given as:
\[ U(t) = K_p e(t) + K_i \int_0^t e(\tau) d\tau + K_d \frac{d}{dt} e(t) \]  
Where \(K_p\) = Proportional gain, \(K_i\) = Integral gain, \(K_d\) = Derivative gain, \(e\) = Error = Setpoint – Measured value, \(t\) = time, \(\tau\) = variable of integration.

Both the PI and PID controllers are designed. In the PI controller the derivative term is neglected. The transfer function of the controller is
\[ G_c(s) = K_p \left( 1 + \frac{1}{sT_i} + sT_d \right) \]  (2)

Where \( T_i \) is integral time and \( T_d \) is derivative time.

Considering the system transfer function as in equation 3, we find the \( K_p \) and the timing constraints of both integral and differential systems using Routh array method. By using Zeigler’s Nichol’s method we can find the gain parameter values of the controller as shown in table 1.

\[ G_c(s) = \frac{1}{s(s+1)(s+5)} \]  (3)

Thus the transfer function of the controller becomes:

\[ C(s) = \frac{R(s)}{s(s+1)(s+5) + K_p} \]  (4)

<table>
<thead>
<tr>
<th>Controller</th>
<th>( K_p )</th>
<th>( K_i )</th>
<th>( K_d )</th>
</tr>
</thead>
<tbody>
<tr>
<td>PI</td>
<td>0.45 ( K_0 )</td>
<td>( 2K_0/T_0 )</td>
<td>0</td>
</tr>
<tr>
<td>PID</td>
<td>0.6 ( K_0 )</td>
<td>( 2K_0/T_0 )</td>
<td>( K_0T_0/8 )</td>
</tr>
</tbody>
</table>

Table 1: Ziegler’s-Nichol Tuning table

From Routh array stability method the values of critical gain ‘\( K_0 \)’ and period of sustained oscillations ‘\( T_0 \)’ are found. Using these values in the table 1 we can find all the parameters required for designing the controller.

a. PI controller

For this controller the differential part is neglected, thus \( K_d = 0 \). From the above table the parameter values obtained are adjusted till the oscillations in the step response is decreased. From the step response for the obtained parameters, we can analyse the response of the system via the following parameters: Rise time \( (t_r) = 0.85 \text{sec} \), Delay time \( (t_d) = 1.3 \text{ sec} \), Settling time \( (t_s) = 14.8 \text{sec} \).

b. PID controller

Similarly as PI controller we also find the parameter values for PID controller from the table 1. We adjust the parameter values until the system is stable. From step response, the Rise time \( (t_r) = 0.35 \text{sec} \), Delay time \( (t_d) = 0.55 \text{sec} \), Settling time \( (t_s) = 7.79 \text{sec} \). Thus from the step response analysis, the PID controller is suitable compared to PI controller.

c. Using Simulink basic blocks

From the obtained gain parameters using Simulink/MATLAB basic blocks we design the controller equation. The figure 3 shows PI controller designed using Simulink blocks. The figure 4 shows the design of PID controller. The control objectives of the blood glucose-insulin system are shown in table 2.

<table>
<thead>
<tr>
<th>Glucose Level</th>
<th>Control Objectives</th>
</tr>
</thead>
<tbody>
<tr>
<td>From 70 to 99 mg/dL</td>
<td>Normal glucose tolerance</td>
</tr>
<tr>
<td>From 100 to 125 mg/dL</td>
<td>Pre-diabetes</td>
</tr>
<tr>
<td>More than 126 mg/dL</td>
<td>Diabetes</td>
</tr>
</tbody>
</table>

Table 2: Control objectives of the blood glucose-insulin system

d. Using Xilinx blocks

The controllers designed using Simulink basic blocks are again designed using Xilinx blocks in Simulink. These blocks are used to generate the HDL code to simulate in Modelsim/Xilinx ISE tools to find the design summary and Timing analysis.

The figure 5 and figure 6 shows the PI and PID controller depicted using Xilinx blocks. Insert the System Generator block in the designed model to generate the HDL code.
Figure 3: PI controller using Simulink Blocks

Figure 4: PID controller using Simulink Blocks

Figure 5: PI controller depicted using Xilinx blocks
IV. SIMULATION RESULTS

a) Simulink results

For both the PI and PID controller the inputs are given from the Workspace and the result is obtained in Workspace. The maximum input glucose value given for both the controllers is 128mg/dL. The figure 7a and figure 7b depicts the input exogenous glucose and exogenous insulin output of the PI controller. The figure 8a and 8b depicts the input and output of the PID controller.

Figure 7a: PI controller input-glucose and Figure 7b: PI controller output-insulin

Figure 8a: PID controller input-glucose and Figure 8b: PID controller output-insulin

a. Xilinx results

Once we design the controller using Xilinx blocks then generate the HDL code using system generator for the required device implementation. The device considered is Virtex 2 pro FPGA and Verilog HDL code generated. Simulation results for both the PI and PID controllers are shown in figure 10 and Figure 11 respectively.

Since the considered output is an unsigned 10 bit number the range is from “-512 to 511”. In the simulation results as the output exceeds the range, the value is represented in negative format as depicted in below figure 9 and 10 respectively.

Figure 9: PI controller simulation

Figure 10: PID controller simulation
The simulation results obtained from Xilinx and the results obtained from the Simulink/Matlab are same. The device utilization of both the PI and PID controllers are compared in the table 3.

<table>
<thead>
<tr>
<th>Logic Utilization</th>
<th>PI</th>
<th>PID</th>
<th>PI</th>
<th>PID</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of Slices</td>
<td>360</td>
<td>558</td>
<td>13,696</td>
<td>3%</td>
</tr>
<tr>
<td>Number of slices flip flops</td>
<td>440</td>
<td>600</td>
<td>27,392</td>
<td>1%</td>
</tr>
<tr>
<td>Number of 4 inputs LUTs</td>
<td>375</td>
<td>527</td>
<td>27392</td>
<td>1%</td>
</tr>
<tr>
<td>Number of bonded IOBs</td>
<td>104</td>
<td>150</td>
<td>556</td>
<td>18%</td>
</tr>
<tr>
<td>Number of BUFGMUXs</td>
<td>1</td>
<td>2</td>
<td>16</td>
<td>6%</td>
</tr>
</tbody>
</table>

Table 3: Synthesis report

V. CONCLUSION

There can be vast differences produced by different tuning procedures. The step response of PID controller is better than the PI controller. Since we had considered only Hyperglycaemia, the exogenous blood glucose should reduce as early as possible, thus the PID controller injects better Insulin dosage compared to PI controller. From the design summary and Timing analysis PI controller is good compared to PID controller, but by using PID controller we can achieve better speed and better performance. The results show that implementation of PID controller on FPGA device in ISE tool is compact, high speed and this promotes the designer to evaluate and implement different designs easy and simple.

Future work:- The same controller can be designed by different algorithms such as Genetic algorithm, Fruit-fly optimization technique, Ant-colony. The complete closed-loop system can be considered and designed for real-time glucose values. The number of bits used in Xilinx blocks can be increased.

REFERENCES


AUTHORS PROFILE:

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