

# Application of Modal Analysis to Modify Chassis Structure using Strain Energy Density

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**Abstract**— The performance assessment of a vehicle structure relates to its strength and rigidity to achieve a level sufficient to support its own load and weight. In vehicle dynamic system modeling, the model can be simplified such as mass, spring and damper. Finite element analysis produces algebraic equations simultaneously as a solution to a structural problem that refers to determination of displacement at each node. Modal analysis generalizes displacement assuming there is no force on the damper in the eigenvalue problem so that dynamic characteristics in the structure can be obtained as natural frequencies and mode shapes. Information about the amount of mass in a structure is known by the participation factor in each mode. Structural modification is done by utilizing elastic materials to store strain energy. The strain energy distributed in the structure per unit volume is known as the strain energy density. An unknown mass was added to strengthen the chassis structure. To determine the natural frequency of the vehicle chassis structure, modal modeling has been done on Ansys Mechanical. Finally, the study evaluates the strain on the chassis and modifies it to obtain new results with a stronger chassis.

**Keywords**— Chassis structure, Three-wheeled electric vehicle, Modal analysis, Strain energy density and Modified structure.

## I. INTRODUCTION

The vehicle chassis structure is a resonant system with an unlimited number of natural frequencies. Modal analysis represents the behavior in the resonance region and all parameters can be determined experimentally<sup>3</sup>. so that the performance of the vehicle chassis structure can be achieved by minimizing unwanted vibrations<sup>1</sup>. Data from modal analysis can be used as an analysis of a system<sup>4</sup>. Such as structural modification<sup>5</sup>, prediction of structure response<sup>6</sup> or detection of structural damage<sup>7</sup>. Structural modifications make changes to the mass, stiffness or damping of the system. This physical change will certainly change the dynamic behavior of the system. By using the system modal model, simulation and prediction can be performed. Physical changes can be made by adding mass to a part of the system, hence the existing modal model and mass together should predict the new modal model after structural modification.

Structural modification technique as an analytical application is used to determine the effect of changes in the physical parameters of a structural system on its dynamic properties in the form of natural frequency and mode shape. Structural modification theory uses a mass and stiffness matrix so that changes in physical parameters are projected into changes in the mass and stiffness properties of the system. For a simple mass-spring system, the actual physical parameters are the mass and stiffness values of the physical elements. For continuous systems such as cantilevers, this parameter can be either the thickness or the length of the beam section so that its

changes can affect the mass and stiffness properties. For real structures such as automobile chassis, the physical parameters can be changes in mass and local stiffness caused by changes in cross-sectional area or by additional welded components between two locations. So that structural modification does not have to depend on knowing the mass and stiffness matrices<sup>2</sup>.

The elastic behavior of a material is a form of the material's effort to store strain energy or potential energy. The external force will be equal to the stored strain energy. In expressing strain energy there are several assumptions such as a material must be elastic, stress is at a proportional limit and loads are applied gradually. If the strain energy is distributed evenly within the material, then the strain energy per unit volume is known as the strain energy density. Most structures are designed with the expectation that the material will remain within the elastic range assuming the stresses in the material reach the elastic limit. As long as the load is below the elastic limit, all strain energy is restored and there is no permanent deformation. Thus the material acts as an elastic spring that stores and releases energy when a load is applied and removed.

In this study, the mode shape generated by modal analysis is considered to be participatory so that the strain energy density of the chassis structure can be used as a modification idea to add mass or connection with the result of increasing the strength of the structure.

## II. METHOD

### A. Design

Three-wheeled electric vehicle design was generated by Solidwork and imported into Ansys Mechanical, the material properties and boundary conditions are specified in Table I and Fig 1.

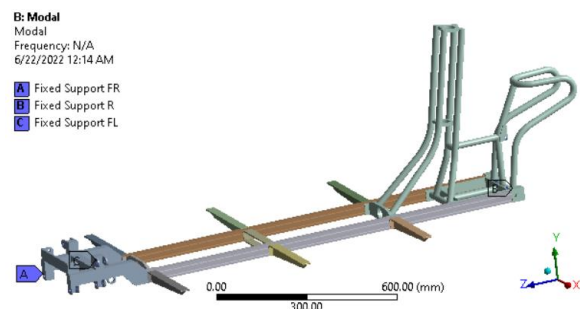


Fig. 1. Magnetic field distribution of in-wheel motor

There are 3 components of plate, pipe and profile with two types of materials. Plates and pipes use 6061 T6 aluminum material, while profiles use 6063 T5 aluminum material.

TABLE I. MECHANICAL PROPERTIES OF MATERIAL

Material Properties	6061 T6	6063 T5
Density (g/cm <sup>3</sup> )	2.7	2.7
Ultimate strength (Mpa)	310	185
Yield strength (Mpa)	275	145
Elastis modulus (Gpa)	69	69
Poisson's ratio (N/A)	0.33	0.33
Bulk modulus (GPA)	69	69
Shear modulus (Gpa)	26	26

Boundary conditions of the modal simulation only use fix supports placed on the front and rear swing arm mountings and suspensions. There is no effect of gravity or force on modal analysis. Modal analysis settings use 10 modes maximum by generating mode shapes based on frequency results. The value of deformation in the structure can be obtained based on the mode shape. The result of the deformation of the mode shape can be used to evaluate the component because it displays a certain dynamic behavior.

*B. Modal Analysis*

Modal analysis is performed on all parts of the chassis structure with 10 selected modes. Structural deformation was observed based on the frequency value. Chassis strength is increased by identifying the most influential components.

Modification of the structure is done by identifying the most influential components. There are several procedures used to determine the modification target for each mode shape.

- 1) Modal analysis to get natural frequency and mode shape
- 2) Participation factor to identify significant mode
- 3) Strain energy density to provide design change ideas

The first step by using modal analysis to determine the natural frequency and mode shape of the chassis structure. The structure can be modeled using a linear dynamic system, the mathematical model consists of a mass matrix [M] and a stiffness matrix [K]. This matrix corresponds to the natural frequency  $\omega_r$  and the mode shape  $\{\phi\}_r$  ( $r = 1, 2, \dots, N$ ) of the eigenvalue equation

$$([K] - \omega_r^2[M])\{\phi\}_r = \{0\} \tag{1}$$

If the modification of the structure is quantified by changes in the mass and stiffness matrices which are denoted respectively as  $[\Delta M]$  and  $[\Delta K]$ , hen the eigenvalue equation of the system is modified to

$$([K] + [\Delta K] - \omega_r^2[M] + [\Delta M])\{\mu\} = \{0\}, \quad r = 1, 2, \dots, N(2)$$

Modification matrices characterize mass and stiffness modifications in the spatial model. Modifications are not made to the matrix but to physical components or parameters such as beam elements in the structure<sup>8</sup>.

The value of deformation in the structure can be obtained based on the mode shape. The result of the deformation of the mode shape can be used to evaluate the component because it displays a certain dynamic behavior. The natural frequency modification target is determined by selecting the ratio of the participation factors close to 1 that may resonate<sup>6</sup>.

The participation factor identifies the amount of mass moving in each direction in the mode shape. This information is used to eliminate the number of mode shapes.

TABLE II. PARTICIPATION FACTOR

Mode	Frekuensi (Hz)	Deformation (mm)	Ratio		
			X Direction	Y Direction	Z Direction
1	54.602	32.385	0.84789	0.00006	0.00015
2	72.296	56.294	1.00000	0.00062	0.00037
3	75.351	32.213	0.00037	0.90680	1.00000
4	79.231	50.154	0.68916	0.00014	0.00002
5	97.263	48.5	0.61770	0.00024	0.00075
6	120.67	25.347	0.00005	1.00000	0.22612
7	128.94	39.506	0.00119	0.71659	0.83122
8	149.04	62.656	0.14830	0.00050	0.00095
9	159.83	66.179	0.00051	0.05361	0.00332
10	163.4	38.964	0.00006	0.65466	0.49913

The modulus of elasticity is the formula for elastic strain energy. When a force is applied to an object, the object changes shape. And if force is no longer applied, the object regains its dimensions and all strain energy is released. The elastic behavior of a material is a form of work in the material to store strain energy.

$$U = \frac{1}{2} V \sigma \epsilon \tag{3}$$

If the strain energy is evenly distributed in the object, then the strain energy per unit volume is known as the strain energy density. Its value is given by

$$U = \frac{1}{2} \sigma \epsilon \tag{4}$$

The location of the strain energy in the structure becomes the idea for the modification model.

III. RESULTS AND DISCUSSION

Structural modification technique as an analytical application is used to determine the effect of changes in the physical parameters of a structural system on its dynamic properties in the form of natural frequency and mode shape.

A. Original Structure

Based on the participation factor data, it can be concluded that there are five modes that affect the structure shown in Table III.

TABLE III. PARTICIPATION FACTOR RATIO

Mode	Direction	
1	X	
2	X	
3	Y	Z
6	Y	
7	Y	Z

The third step is to give the output energy per volume of the selected mode shape.

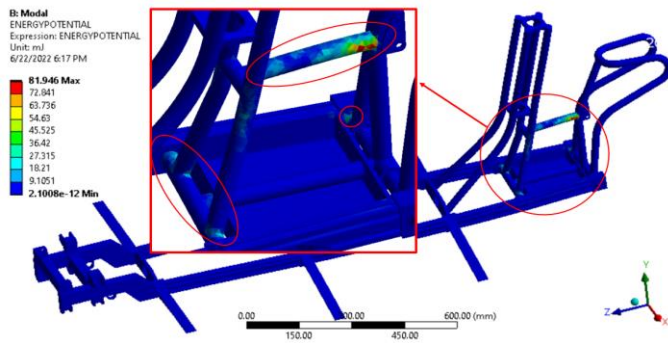


Fig. 2. Mode shape 1

Mode shape 1 provides three modification points. In this area, the contours with the maximum mass amount are experienced. The direction of movement is in accordance with Table III for X direction.

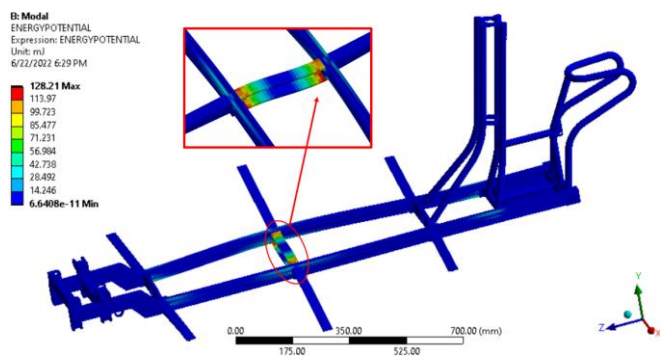


Fig. 3. Mode shape 2

In mode shape 2, mass will be added in the X direction.

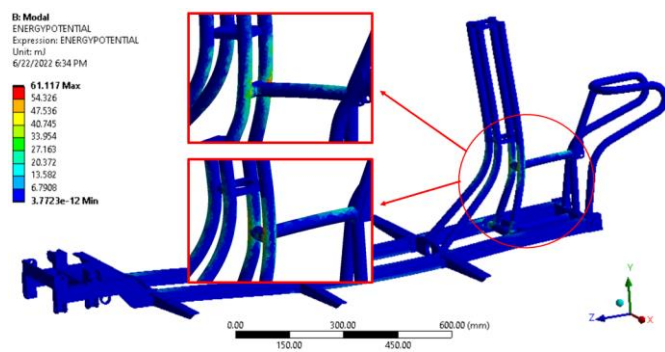


Fig. 4. Mode shape 3

Modifications were made by changing the components in modes 3.

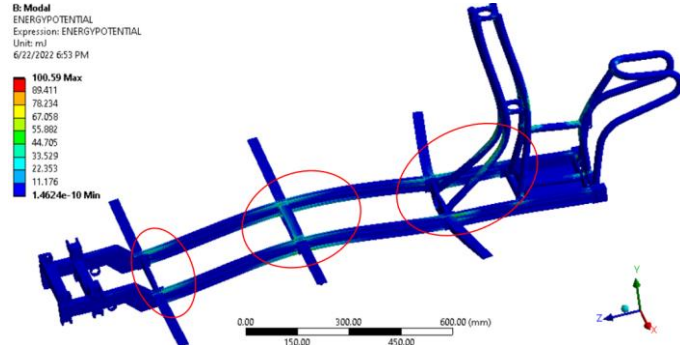


Fig. 5. Mode shape 6

In mode shape 6 there is a limitation that the long members come from aluminum profiles. So for that area, an additional plate covering the area of the cargo base is added.

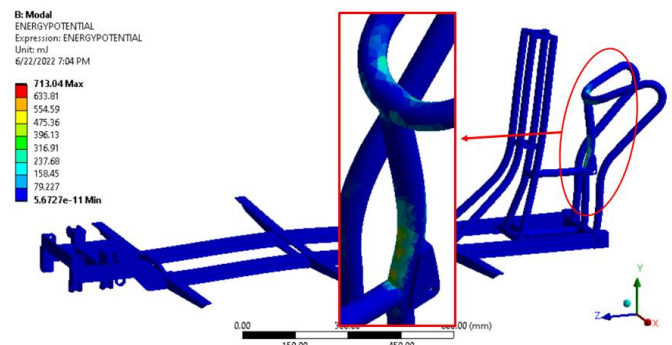


Fig. 6. Mode shape 7

TABLE IV. NATURAL FREQUENCY AND STRAIN ENERGY DENSITY OF ORIGINAL STRUCTURE

Mode	Frekuensi (Hz)	Strain Energy Density (J/m <sup>3</sup> )
1	54.602	81.946
2	72.296	128.21
3	75.351	61.117
6	120.67	100.59
7	128.94	713.04

In the Table IV, the value of the strain energy density in each mode on the natural frequency of the vehicle structure is shown.

### B. Structure Modification

The cases that occur in mode shape 1, 3 and 7 are the same, namely in the driver's seat and the steering wheel. But the mode shape 2 and 6 have a different case. In mode shape 2 is located on the cross members in the middle of the chassis structure while in mode shape 6 is located along the connection of long members and trust members.

The results of the overall structure modification are shown in Fig 8. With the new structure, re-testing is carried out to determine the possibility of the structure resonating in each mode shape.

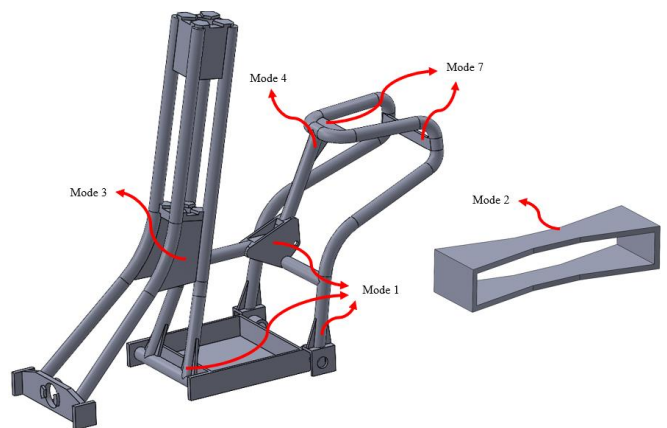


Fig. 7. Modification based on mode shape



TABLE V. PARTICIPATION FACTOR STRUCTURE MODIFICATION

Mode	Frekuensi (Hz)	Deformation (mm)	Ratio		
			X Direction	Y Direction	Z Direction
1	43.104	48.669	-0.006	0.000	0.000
2	52.893	77.296	0.000	0.032	-0.004
3	53.869	62.479	-0.004	0.001	0.000
4	57.384	77.055	0.000	0.046	-0.004
5	67.772	29.227	0.047	0.000	0.000
6	84.272	50.388	0.012	0.000	0.000
7	86.845	29.533	0.000	-0.054	0.031
8	122.53	26.899	0.000	-0.038	-0.012
9	129.08	33.627	0.000	-0.021	-0.019
10	130.95	59.533	0.038	0.000	0.000

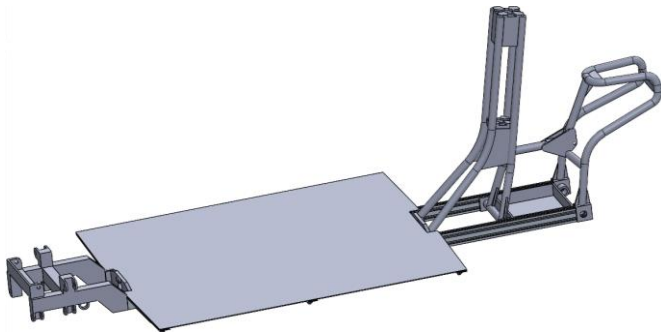


Fig. 8. Structural modification

In the participation ratio, there is no significant change in mass in the direction of the XYZ axis with a value of less than 1. So it can be stated that the modification of the chassis structure has achieved its goal and has sufficient strength.

#### IV. CONCLUSIONS

The chassis structure has been tested according to its participation factor and has been analyzed with 10 mode shape.

Modification of the chassis structure using modal strain energy where this strategy utilizes the results of the modal analysis to continue analysis. In the original chassis, the frequency range is 54,602 Hz to 163.4 Hz in mode 1 and mode 10. While in the modified structure, the frequency value is in the range of 43.104 Hz to 130.95 Hz in mode 1 and mode 10. This value is affected by mass so that it has an impact on stiffness in the chassis structure. And not found that the form of the mode that significantly affects the resonance of the structure on the participation factor.

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