

Anti-Roll Bar Design and Material Selection for the Torsion Member for A Formula Student Vehicle

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Abstract_- The following study will be dealing with the design procedure, constraints, and limitations that were dealt with during the design of the Anti-roll bar system of a formula student vehicle. Also, simulations with proper forces for torsion on the torsional member to select the best possible material for the torsion member was done.

Keywords- FSAE, Anti-roll bar, Roll, Formula student

INTRODUCTION –

Anti-roll bar sometime also known as a stabilizer bar or sway bar is used for the purpose of controlling the roll motion of the vehicle. It provides better stability during cornering. Roll motion referred as to the motion in the lateral direction on the Y-axis during which the vehicle rolls around the central axis of the vehicle.

Image Courtesy- RHD-JAPAN
 Anti- Rollbar increases overall roll stiffness of the vehicle, thus providing a number of advantages to the vehicle and its performance.

One of the major advantages is that it provides better traction during cornering the vehicle.

METHOD USED –

The calculations were done in the following syntax -
 RIDE RATES - ROLL ANALYSIS - ARB DIMENSIONS
 AND MATERIAL SELECTION

Ride rates were calculated by first determining the desired Natural frequencies of the front as well as rear but separately. These values were chosen using the general values which have validated after years of experimentation and observation.

Natural frequency for the front suspension = 2 Hz

Natural frequency for the rear suspension = 2.5Hz

The reason behind aiming for higher natural frequency in the rear is to compensate for the response delay, since its always the front suspension which has to act first.

Then, the ride rates were calculated for the front and rear individually using the following expression-

$$K_{RF} = \frac{4\pi^2 \omega_F^2 (W_{SF}/2)}{386.4}$$

Here, Krf= Ride Rate front
 wF=Natural Frequency Front
 Wsf= Sprung mass front

Roll Analysis - Here the first which needs to be calculated is the COG height of the sprung mass.

which can be calculated using the following expression -
 Here, hs= sprung COG ht., h=COG ht., Wuf=Unsprung

$$h_s = \frac{W_T h - W_{UF} R_{LF} - W_{UR} R_{LR}}{W_S}$$

wt. Front,

RLf= Tire loaded radius(Static) front, Wur=Unsprung wt. Rear

RLr=Tire loaded radius(Static) Rear

Sprung Wt. distribution = Sprung wt front/Total sprung mass.

Rolling Moment (lever Arm) =

(Sprung mass cog ht.)-(Front Roll Centre ht.+(Rear Roll Centre ht.-Front Roll Centre ht.)(1-sprung mass wt. distribution)]

Rolling moment per g lateral acceleration =

$$\frac{M_\phi}{A_y} = \frac{h_{RM} W_S}{12}$$

Here, Hrm= Rolling moment (lever arm) -----

---- Calculated above

Now, dividing this value with the desired roll gradient will give us the Roll Rate required(KΦ).

Roll gradient should be taken between 1.5 - 3deg/g for an fs vehicle.

Now calculate available Front spring roll rate by using the following expression -

$$K_{\phi SF} = \frac{K_{RF} T_F^2}{1375}$$

	A	B	C	D	E	F	G	H	I	J	K	L	M
1	RIDE AND ROLL RATES												
2													
3													
4													
5	Roll Gradient(table 16.1)	1.2											
6	ϕ	0.8											
7	Motion Ratio (sheet 1)	0.7											
8	Wf(NF)	2	Wr(NF)	2.5									
9	Wsf(sprung wt.)	220.462	Wsr	343.921									
10													
11	Krf(ride rate front)	45.04904865	Krr	109.8071									
12													
13													
14	Kw(wheel rate)(sheet1)	47.1967											
15													

Table 16.1 Typical Roll Gradients, Based on Ref. 91

Very Soft—Economy and basic family transportation, both domestic and import, pre-1975.	8.5 deg/g
Soft—Basic family transportation, domestic and import, after 1975.	7.5
Semi-Soft—Contemporary middle-market sedans, domestic and import.	7.0
Semi-Firm—Imported sport sedans.	6.0
Firm—Domestic sport sedans.	5.0
Vary Firm—High-performance domestic, such as Camaro Z-28 and Firebird Trans Am.	4.2
Extremely Firm—Contemporary very-high-performance sports, such as Corvette, and street cars extensively modified to increase roll stiffness.	3.0
Hard—Racing cars only.	1.5
Active Suspension—Servo-controlled roll stiffness. Roll-in, zero-roll, and roll-out all possible.	—

Here, $K\Phi_{sf}$ = Front spring roll rate
 K_{rf} = Ride rate front (calculated during ride analysis)
 T_f = Track width front

Similarly, by using adequate value, the available rear spring roll rate ($K\Phi_{sr}$) can be determined.

Adding both the front and rear roll rates will give us the total available roll rate.

So, arb must provide = Required roll rate - available roll rate

Now, to size the front and rear bars, we need to calculate this requirement based on the weight distribution of the vehicle.

Multiply this with %load transfer X 100 to get front/rear load transfer.

Front Roll Stiffness ($K_{\phi f}$) =

$$\frac{FLT}{A_y} = \frac{12(K_{\phi F})\phi}{T_F} + \frac{W_{SF}Z_F}{T_F} + \frac{W_{UF}RL_F}{T_F}$$

Here, ϕ = Roll Gain (0.5 - 1 for non-aero fs vehicles)

From here, it can be calculated that the rear arb must provide

ROLL ANALYSIS													
16													
17													
18													
19	Sprung mass CG ht.					Sprung mass wt dist.				rolling moment lever arm			
20													
21	Wt(total wt)	617.294				Wsf(sprung wt F)	220.462			hs	9.91634		
22	h(CG ht)	9.84252				as	0.390624806			Zf	2.16575		
23	Wuf(unsprung mass)	26.4555				%	39.06248062			Zr	2.27992		
24	RLf(tire radius loaded static)	9.05512								hrm	7.68102		
25	Wur	26.4555											
26	RLr	9.05512											
27	total sprung wt(Ws)	564.383											
28	hs	9.91633888											
29													
30	Rolling moment per g lat. Acc					REQd roll rate				Front /Rear Spring roll rate			
31													
32	hrm	7.6810165				M ϕ /Ay	361.2529281			Krf	45.049	Krr	109.807
33	Ws	564.383				Roll Gradient	1			Tf(t/w front)	46.4567	Tr(t/w rear)	42.1575
34	M ϕ /Ay	361.252928				K ϕ	361.2529281			K ϕ_{sf}	70.7098	K ϕ_{sr}	141.981
35													
36													
37													
38	Total roll rate by springs	212.640753				Total Load Transfer				front Reqd Stiffness			
39													
40	ARB roll rate(Karb)	148.612176				Wt	617.294			FLT/Ay	127.006		
41						h	9.84252			Tf	46.4567		
42						Tavg	21.07874015			Wsf	220.462		
43										Zf	2.16575		
44						TLT/Ay	288.2396432			Wuf	26.4555		
45						Front load transfer	127.0055369			RLf	9.05512		
46													
47													
48													
49													
50	REQD BAR STIFFNESS REAR	-126.22698	lb-ft/deg										
51	diff	274.839158											
52	REQD BAR STIFFNESS FRONT	560.896242	lb-ft/deg										
53													

Here, TLT/A_y = Total load transfer during lateral acceleration.

T_{ave} = Average of Front and Rear track width

the difference between the total, rear, and that provided by the rear springs.

$K_{\phi}(\text{arb})_{\text{rear}} = K_{\phi} - K_{\phi f} - K_{\phi sr}$

Divide this by the Linkage ratio(rear) to get the final requirement.

For the front,

$$K\phi(\text{arb})_{\text{front}} = (K\phi_f - K\phi_{sf})/\text{linkage ratio}(\text{front})$$

RESULTS AND DISCUSSION FOR THE METHOD

The whole calculation was done by preparing a spreadsheet to facilitate the calculations. For which the results are shown as followed -

It can be seen that the required stiffness for the rear comes out to be negative, which symbolizes that the rear suspension is stiff enough and does not require an arb setup.

MATERIAL SELECTION

The following materials were considered-

- Mild steel - AISI 1020 80 GPa shear modulus
- Aluminum - AL-7075 T6 26.9 GPa shear modulus
- Magnesium alloy - AZ31B 17 GPa shear modulus

Although magnesium alloy provides great weight reduction advantage it is expensive and also for the same thickness, withstands lower stress than aluminum.

After running simulations aluminum was considered as the optimal choice as it provided enough durability, is lightweight, and cheaper than magnesium alloy.

The size was determined by comparing the required area moment of inertial to the area moment of inertia of the arb system torsion bar with desired dimensions.

$$\text{Required area moment of inertia} = [(\text{Required Roll stiffness} \times \text{Length of tube})/\text{Shear Modulus}]$$

$$\text{Area moment of inertia for cylindrical tube} = [\pi(D^4 - d^4)]/32$$

The following simulation was done by applying 650N on both ends in torsion that sums up to 1300N in total.

Reqd bar stiffness Front	760.473193
G	2.6E+10
L	0.573
i	1.676E-08
MATERIAL	7075 T6
i	3.7276E-08
D	0.035
d	0.015

With dimensions OD= 35mm
 ID= 15mm

CONCLUSION -

Anti-roll bar torsion member with outer diameter of 35mm and inner diameter 15mm was designed to provide roll stiffness of 760.4731927 Nm/mm.

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Softwares Used - CAD Modelling - Solidworks 2020
 Simulation - Ansys R17.2

REFERENCES

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