

# A Two-stage Identification based on Seed and Grow Algorithm against Anonymized Social Networks

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**Abstract**— In a internet based social networking services the digital traces left behind even after anonymization they are more sensitive in privacy breaches. The sociologist tracks the feasibility of such an attack. There is an algorithm called Seed and Grow which identifies users from an anonymized social graph based only on graph structure. The algorithm first identifies a seed sub graph either planted by the attacker or by any one ant then grows the seed layer based on the attackers existing knowledge of the users social relations. The algorithm identifies and relaxes implicit assumptions taken by previous work and improves the identification effectiveness and accuracy.

**Index Terms**— Feasibility, Identification, Privacy and Accuracy, Graph.

## I. INTRODUCTION

Social networks like Friendster.com, tagged.com, Xanga.com, LinkedIn including Facebook and Twitter, two popular online social networking services, rank at 2nd and 9th place respectively they have developed on the Internet over the past several years and these social networks have been successful in attracting many users, a decades ago only Telecommunication service providers and Intelligence agencies used to provide the critical information's like date of birth and other user generated contents, now through social networks the users engage with each other for various purposes, including business, entertainment and knowledge sharing. The commercial success of social networks depends on the number of users it attracts, and by encouraging users to add more users to their networks and to share data with other users in the social networks. End users are, however often not aware of the anonymization attacks and advertisements.

Due to the strong correlation between use data and the users sociality entity, privacy is a major concern dealing with social network data in context such as storage, processing and publishing. Privacy control, through which a user can tune the visibility of her profile, is an essential feature in any major social networking service.

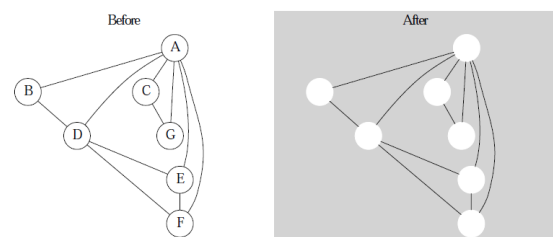


Figure 1.1 An illustration of naïve anonymization. Each node represents a user ID attached. Naïve anonymization simply removes the ID, but retains the network structure.

The common practice for privacy-sensitive social network data publishing is through anonymization, i.e., remove plainly identifying label such as name, social security number, post lore mail address, and retain the structure of the network as published data. Figure 1.1 is as implemented illustration of this process. The motivation behind such processing prior to data publishing is that, by removing the “who” information, the utility of the social networks is maximally preserved without compromising users’ privacy. Narayanan and Shmatikov report several high profile cases in which “anonymity has been unquestioningly interpreted as equivalent to privacy” Can the aforementioned “naïve” anonymization technique each I ever privacy preservation in the context to privacy-sensitive social network data publishing? This interesting and important question was posed only recently by Backstrom et al. A few privacy attacks have been proposed to circumvent the naïve anonymization protection..

Meanwhile, more sophisticated anonymization techniques

have been proposed to provide better privacy protection [4, 5, 6, 7, 8]. Nevertheless, research in this area is still in its infancy and a lot of work, both in attacks and defenses, remains to be done.

In this paper, we describe a two-stage identification attack, *Seed-and-Grow*, against anonymized social networks. The name suggests a metaphor for visualizing its structure and procedure. The attacker first plants a *seed* into the target social

network before its release. After the anonymized data is published, the attacker retrieves the seed and makes it *grow* larger, thereby further breaching privacy.

More concretely, our contributions include:

- We propose an efficient seed construction and re-recovery algorithm. More specifically, we drop the assumption that the attacker has complete control over the connection between the seed and the rest of the graph (Section 3.1.2); the seed is constructed in a way which is only visible to the attacker (Section 3.1.2); the seed recovery algorithm examines at most the two-hop local neighborhood of each node, and thus is efficient (Section 3.1.3).
- We propose an algorithm which grows the seed (i.e., further identifies users and hence violates their privacy) by exploiting the overlapping user bases among social network services. Unlike previous works which require arbitrary parameters for probing aggressiveness, our algorithm automatically finds a good balance between identification effectiveness and accuracy (Section 3.2).
- We demonstrate the significant improvements in identification effectiveness and accuracy of our algorithm over previous works with real-world social-network datasets.

## II. RELATED WORK

A natural mathematical model to represent a social network is a graph. A graph  $G$  consists of a set  $V$  of vertices and a set  $E \subseteq V \times V$  of edges. Labels can be attached to both vertices and edges to represent attributes.

In this context, *privacy* can be modeled as the knowledge of existence or absence of vertices, edges, or labels. An extension is to model privacy in terms of metrics, such as betweenness, closeness, and centrality, which originate from *social network analysis* studies [9].

The naive anonymization is to remove those labels which can be uniquely associated with one vertex (or a small group of vertices) from  $V$ . This is closely related to traditional anonymization techniques employed on relational datasets [10]. However, the information conveyed in edges and its associated labels is susceptible to privacy breaches. Backstrom et al. [3] proposed an identification attack against anonymized graph, and coined the term *structural steganography*.

Besides privacy, other dimensions in formulating privacy attacks against anonymized social networks, as identified in numerous previous works [5, 6, 8, 11], are the published data's *utility*, and the attacker's *background knowledge*.

*Utility* of published data measures information loss and distortion in the anonymization process. The more information that is lost or distorted, the less useful published data is. Existing anonymization schemes [4, 5, 6, 8, 11] are all based on the trade-off between the usefulness of the published data. These graphs, he manages to identify 100 more users from the anonymized graph (the "Dissimilarity" interlude in Section 3.2 illustrates a way to do this). By doing so, Bob

and the strength of protection. For example, Hay et al. [8] propose an anonymization algorithm in which the original social graph is partitioned into groups before publication, and "the number of nodes in each partition, along with the density of edges that exist within and across partitions," are published.

Although a trade-off between utility and privacy is necessary, it is hard, if not impossible, to find a proper balance overall. Besides, it is hard to prevent attackers from proactively collecting intelligence on the social network. It is especially relevant today as major online social networking services provide APIs to facilitate third-party application development. These programming interfaces can be abused by a malicious party to gather information about the network.

*Background knowledge* characterizes the information in the attacker's possession which can be used to compromise privacy protection. It is closely related to what is perceived as privacy in a particular context.

The attacker's background knowledge is not restricted to the target's neighborhood in a single network, but may span multiple networks and include the target's alter egos in all of these networks [2]. This is a realistic assumption. Consider the status quo in the social networking service business, in which service providers, like Facebook and Flickr, offer complementary services. It is very likely that a user of one service would simultaneously use another service. As a person registers to different social networking services, her connections in these services, which relate to her social relationships in the real world, might reveal valuable information which the attacker can make use of to threaten her privacy.

The above observation inspires Seed-and-Grow, which exploits the increasingly overlapping user-bases among social networking services. A concrete example is helpful in understanding this idea.

[Motivating scenario.] Bob, as an employee of a social networking service provider F-net, acquires from his employer a social-network data-set, in which vertices represent users and edges represent private chat sessions. The edges are labeled with attributes such as timestamps. In accordance with its privacy policy, F-net has removed the user IDs from the graph before giving it to Bob.

Bob, being an inquisitive person, wants to know who these users are. Suppose, somehow, Bob identifies 4 of these users from the graph (the "Seed Construction" and "Seed Recovery" interludes in Section 3.1 illustrate a way to do this). By using a graph (with the user ID tagged) he crawled a month ago from the website of another service provider T-net (the 4 identified persons are also users of T-net), and by carefully measuring structural similarity of

circumvents his employer's attempt to protect its customers' privacy.

We conclude this section with a brief comment on our choice of model. We use the *undirected* graph model to explain the proposed deanonymization attack on social networks. Undirected graphs arise naturally in scenarios where the social relation under investigation is *mutual*, e.g., friend requests must be confirmed on Facebook. *Directed* graphs, however, are more appropriate in other cases, such as fans following a movie star on Twitter. An undirected graph could be seen as a special case of directed graphs, in which the relationship is reciprocal; Mislove et al. confirmed the relationship reciprocity in a large-scale study on the Flickr online photo-sharing service [12]. As explained in Section 3, the algorithms used in the proposed deanonymization attack do not rely on the fact that the used graphs are undirected; they work on directed graphs the same way. The undirected graph model is only a choice for specificity and ease of presentation.

### III. SYSTEM MODEL

#### SEED-AND-GROW: THE ATTACK

This section describes an attack that identifies users from an anonymized social graph. Let an undirected graph  $G_T = \{V_T, E_T\}$  represent the *target* social network after anonymization. We assume that the attacker has an undirected graph  $G_B = \{V_B, E_B\}$  which models his *background knowledge* about the social relationships among a group of people, i.e.,  $V_B$  are labeled with the identities of these people. The motivating scenario demonstrates one way to obtain  $G_B$ .

The attack concerned here is to infer the identities of the vertices  $V_T$  by considering *structural similarity* between the target graph  $G_T$  and the background graph  $G_B$ : Nodes that belong to the same users are assumed to have similar connections in  $G_T$  and  $G_B$ . Although sporadic connections between who would otherwise be strangers may exist in an online social network (and, thus, affect the similarity between  $G_T$  and  $G_B$ ), such links can be removed by, for example, quantifying the strength of these connections [13]; the residual network consists of the stable, strong connections that reflect the users' real-world social relationships, which give rise to the similarity between  $G_T$  and  $G_B$ . Additionally, auxiliary knowledge about the target graph  $G_T$  (such as the source and nature of the graph) may help in choosing a background graph  $G_B$  with similar structures.

Thus, the two graphs  $G_T$  and  $G_B$  are syntactically (the social connections) similar but semantically (the meaning associated with such connections) different. By re-identifying the vertices in  $G_T$  with the help of  $G_B$ , the attacker associates the sensitive semantics with users on the anonymized  $G_T$  and, thus, compromise the privacy of such users. An example of sensitive semantics is the private chat sessions, and their associated timestamps, in the motivating scenario.

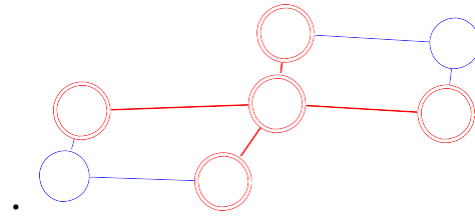


Figure 3.1. An undirected graph  $G_F$  may be symmetric. Vertices in  $G_F = \{v_1, \dots, v_5\}$  are double-circled.

We assume that, *before* the release of  $G_T$ , the attacker obtains (either by creating or stealing) a few accounts and connects them with a few other users (the *initial seeds*) in  $G_T$ . The feasibility of doing this is the basis of the Sybil identity forgery attack studied in numerous previous works [14, 15, 16, 17, 18, 19, 20, 21, 22]. In-deed, experiments (Section 4) show that our algorithm is capable of identifying 10 times of anonymized users from as few as 5 initial seeds. Besides user IDs, the attacker knows nothing about the relationship between the initial seeds and other users in  $G_T$ . Furthermore, unlike previous works, we *do not assume that the attacker has complete control over the connections*: the attack only *knows* them before  $G_T$ 's release. This is more realistic. An example is a confirmation-based social network, in which a connection is established only if the two parties confirm it: the attacker *can decline but not impose* a connection.

In contrast to a pure structure-based vertex matching algorithm [23], Seed-and-Grow is a *two-stage* algorithm.

The *seed* stage plants (by obtaining accounts and establishing relationships) a small specially designed subgraph  $G_F = \{V_F, E_F\} \subseteq G_T$  ( $G_F$  reads as "fingerprint") into  $G_T$  before its release. After the anonymized graph is released, the attacker locates  $G_F$  in  $G_T$ . The neighboring vertices  $V_S$  of  $G_F$  in  $G_T$  are readily identified and serve as the *initial seeds* to be grown.

The *grow* stage is essentially comprised of a structure-based vertex matching, which further identifies vertices adjacent to the initial seeds  $V_S$ . This is a self-reinforcing process, in which the seeds grow larger as more vertices are identified.

#### 3.1 Seed

##### 3.1.1 Feasibility

Successful retrieval of  $G_F$  from  $G_T$  is guaranteed if  $G_F$  exhibits the following structural properties.

- $G_F$  is *uniquely* identifiable, i.e., no subgraph  $H \subseteq G_T$  except  $G_F$  is isomorphic to  $G_F$ . For example, in Figure 2, sub graph  $\{v_1, v_2, v_3\}$  is isomorphic to sub graph

$\{v_1, v_4, v_5\}$  because there is a structure-preserving mapping  $v_1 \xrightarrow{7} v_1, v_2 \xrightarrow{7} v_4, v_3 \xrightarrow{7} v_5$  between them. Therefore, the two sub graphs are structurally indistinguishable once the vertex labels are removed.

if we could locate  $V_F = \{v_1, \dots, v_5\}$  from  $G_T$ ,  $v_2, \dots, v_5$  are indistinguishable once their labels are even

In practice, since the structure of other nodes in the network is unknown to the attacker before its release, the uniquely identifiable property is not realizable. However, as was proved by Backstrom et al. [3], with a large enough size and randomly generated edges under the Erdos-Renyi model [24],  $G_F$  will be uniquely identifiable with high probability.

Although a randomly generated graph  $G_F$  is very likely to be uniquely identifiable in  $G_T$ , it may violate the asymmetric structural property. However, because the goal of seed is to identify the initial seed  $V_S$  rather than the fingerprint  $G_F$ , the asymmetric requirement for  $G_F$  can be relaxed. For  $u \in V_S$ , let  $V_F(u)$  be the vertices in  $V_F$  which connect with  $u$  ( $|V_F(u)| \geq 1$  by the definition of  $V_S$ ). For each pair of vertices, say  $u$  and  $v$ , in  $V_S$ , as long as  $V_F(u)$  and  $V_F(v)$  are distinguishable in  $G_F$  (e.g.,  $|V_F(u)| \neq |V_F(v)|$  or the degree sequences are different; more precisely, no automorphism of  $G_F$  exists which maps  $V_F(u)$  to  $V_F(v)$ ), and once  $G_F$  is recovered from  $G_T$ ,  $V_S$  can be identified uniquely. In Figure 2, since  $V_F(6) = \{v_2, v_3\}$  and  $V_F(7) = \{v_4, v_5\}$  are not distinguishable, vertices  $v_6$  and  $v_7$  cannot be identified through  $G_F$ .

Based on these observations, we propose the following method of constructing and recovering  $G_F$ .

### 3.1.2 Construction

The construction of  $G_F$  starts with a *star* structure. The motivation for the star structure will become clear in Section 3.1.3. We call the vertex at the center of the star the *head* of  $G_F$  and denote it by  $v_h$ .  $v_h$  connects and *only* connects to every other vertex in  $G_F$ .

The vertices in  $V_F - \{v_h\}$  are connected with some other vertices of the initial seeds  $V_S$  in  $G_T$ . To ensure the distinguish ability of two seeds  $u$  and  $v$  once the fingerprint  $G_F$  is recovered, the attacker can decline those connection requests (from other vertices in  $G_T$ ) which render  $V_F(u) = V_F(v)$ . Note that the attacker is not assumed to have full control over the connections: an attacker does not have to impose a connection as long as he can decline it.

- $G_F$  is *asymmetric*, i.e.,  $G_F$  does not have any non-

trivial automorphism. For example, in Figure 2, sub-graph  $\{v_1, v_2, \dots, v_5\}$  has an automorphism  $v_1 \xrightarrow{7} v_1, v_2 \xrightarrow{7} v_3, v_3 \xrightarrow{7} v_4, v_4 \xrightarrow{7} v_5, v_5 \xrightarrow{7} v_2$ . Therefore, After setting up the initial star structure, the attacker establishes other *internal* connections within the finger-print graph  $G_F$ . Two principles dictate this process:

- 1) No automorphism of  $G_F$  should map  $V_F(u)$  to  $V_F(v)$  for two distinct initial seeds  $u$  and  $v$ .
- 2) The constructed  $G_F$  should leave no distinctive structural pattern for anyone besides the attacker, but should yet be recoverable.

Principle 1 follows from the discussion in Section 3.1.1: a pair of initial seeds  $u$  and  $v$  could be unambiguously identified only if no automorphism of  $G_F$  maps  $V_F(u)$  to  $V_F(v)$ . Principle 2 apparently presents a dilemma:  $G_F$  should mingle with the rest of the target graph  $G_T$ , yet be distinctive. In the following discussion, we first

justify this principle, and then resolve the dilemma by reconciling the two competing requirements.

The motivation for having  $G_F$  mingle with the rest of the target graph  $G_T$  is to avoid leaving distinctive structural patterns for defenders. Otherwise, a straight-forward defense against the proposed attack would be to locate the fingerprint graph  $G_F$  by pattern-matching and to remove it prior to the publication of  $G_T$ . An implication is that the construction of  $G_F$  should be stochastic rather than deterministic.

Yet, stochastic construction alone is not enough for  $G_F$  to blend into  $G_T$ . Numerous studies [25, 26, 27, 28, 29, 30, 31] indicate the existence of distinctive structural properties of online social networks as opposed to arbitrary random graphs. In particular, online social graphs consist of a well-connected backbone linking numerous small communities [25]. Within each community, vertices show a local, transitive, triangle-closing connection pattern [29]. The construction of  $G_F$  should reflect these properties to blend into  $G_T$ .

The cost for the attacker to set up the fingerprint graph  $G_F$  is dominated by the number and variety of connections between  $V_F$  and the initial seeds  $V_S$ . To minimize the cost, the construction of  $G_F$  mimics a local community in  $G_T$  [25]: after establishing the star structure centering at the head vertex  $v_h$ , each pair of vertices in  $V_F - \{v_h\}$  connects with a probability of  $t$ . The probability  $t$  reflects the *transitivity* of a community in  $G_T$ , which is the likelihood that, in the same community, two vertices sharing a common neighbor ( $v_h$  in  $G_F$ ) will connect to each other. In reality, the attacker almost



always knows some auxiliary information about the target graph  $G_T$ , which may include the community transitivity and a reasonable size for a community: The construction of  $G_F$  should be adjusted to such information for  $G_T$  to blend into  $G_T$ .

After connecting pairs of non-head vertices in  $V_F$  with a probability of the community transitivity  $t$ , the attacker collects the *internal degree*  $DF(v)$ , which is number of vertices in  $V_F$  that  $v$  connects to, for every  $v \in V_F - \{v_h\}$  into an *ordered* sequence  $SD$ .

Now, for every  $v \in V_S$ ,  $v$  has a corresponding subsequence  $SD(v)$  of  $SD$  according to its connectivity with  $V_F$ . For example, in Figure 2,  $v_6$  connects to  $v_2$  and  $v_3$  from  $G_F$ ; since  $DF(v_2) = DF(v_3) = 1$ ,  $SD(v_6) = h1, 1i$ . As long as  $SD(u) \neq SD(v)$  for  $u$  and  $v$  from  $V_S$ , no automorphism of  $G_F$  will map  $V_F(u)$  to  $V_F(v)$ . Therefore, the attacker guarantees unambiguous recovery of  $V_S$  by ensuring that the randomly connected  $G_F$  satisfies this condition. If not, the attacker will simply redo the random connection among  $V_F - \{v_h\}$  until it does (which it eventually will, since we assume that  $V_F(u) \neq V_F(v)$  for any pair  $u$  and  $v$  from  $V_S$ ). Algorithm 1 summarizes the procedure. [Seed construction.] Bob had created 7 accounts  $v_h$  and  $v_1, \dots, v_6$ , i.e.,  $V_F$ . He first connected  $v_h$  with  $v_1, \dots, v_6$ . After a while, he noticed that users

$v_7$  to  $v_{10}$  are connected with  $v_1, \dots, v_6$ , i.e.,  $V_S = \{v_7, \dots, v_{10}\}$ .

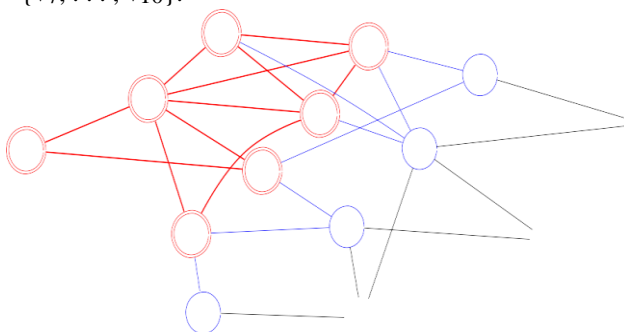


Fig. 3.2 The task of the seed stage is to identify the initial seed by recovering the fingerprint graph  $G_F$ .

Then, he randomly connected  $v_1, \dots, v_6$  with the community transitivity  $t$  and got the resulting graph  $G_F$ , as shown in Figure 3. The ordered internal

degree sequence  $SD = h2, 2, 2, 3, 3, 4i$ . Bob found out that  $SD(v_7) = h2i$ ,  $SD(v_8) = h2, 2i$ ,  $SD(v_9) = h3, 3, 4i$ , and  $SD(v_{10}) = h2, 3i$ . Since they are mutually distinct, Bob was sure that he could

identify  $v_7$  to  $v_{10}$  once  $V_F$  was recovered from the published anonymized graph.

### 3.2 Grow

The initial seeds  $V_S$  provide a firm ground for further identification in the anonymized graph  $G_T$ . Background knowledge  $G_B$  comes into play at this stage.

We have a partial mapping between  $G_T$  and  $G_B$ , i.e., the initial seeds  $V_S$  in  $G_T$  map to corresponding vertices in  $G_B$ . Two examples of partial graph mappings are the Twitter and Flickr datasets [2] and the Netflix and IMDB datasets [32]. The straightforward idea of testing all possible mappings for the rest of the vertices has an exponential complexity, which is unacceptable even for a medium-sized network. Besides, the overlapping

Figure 3.3 shows a small example.  $v_7$  to  $v_{10}$  have already been identified in the seed stage (recall Figure 3). The task is to identify other vertices in the target graph  $G_T$ .

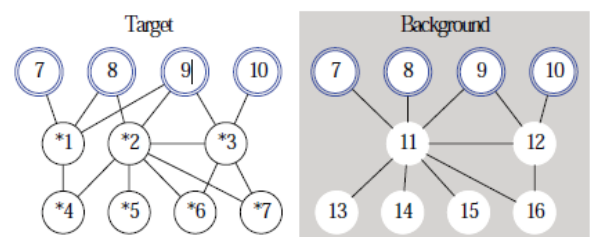


Figure 3.3 The task of the grow stage is to identify the unmapped vertices starting from the seed.

based on the attacker's existing knowledge of the users' social relations. We identify and relax implicit assumptions for unambiguous seed identification taken by previous works, eliminate arbitrary parameters in grow algorithm, and demonstrate the superior performance over previous works in terms of identification effectiveness and accuracy by simulations on real-world-collected social-network datasets between  $G_T$  and  $G_B$  may be *partial*, so a *full* mapping is neither possible nor necessarily desirable. Therefore, the grow algorithm adopts a progressive and self-reinforcing strategy, starting with the initial seeds and extending the mapping to other vertices for each round

## IV. CONCLUSION

*Seed-and-Grow*, to identify users from an anonymized social graph. Our algorithm exploits the increasing overlapping user-bases among services and is based solely on social graph structure. The algorithm first identifies a seed sub-graph, either planted by an attacker or divulged by collusion of a small group of users, and then grows the seed larger

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