

A Soft Computing Frame Work for Inventory Management using the Cuckoo Optimization Algorithm in Own-Warehouse Systems

Vaibhav Sharma

Department of Computer Science & Engineering Shobhit Institute of Engineering & Technology, Meerut, India

Yogesh Awasthi

Department of Computer Science & Engineering Africa University, Zimbabwe.

Sanjay Kumar

Department of Mathematics, SRM University, Delhi – NCR, Sonipat, Haryana, India.

Abstract: Inventory management becomes increasingly complex when organizations operate their own warehouses, facing challenges such as capacity limitations, deterioration of goods, backordering, and inflationary effects. This study proposes a soft computing framework based on the Cuckoo Optimization Algorithm (COA) to optimize inventory decisions within an own-warehouse environment. The model integrates realistic assumptions, including exponential ramp-type demand, partial backordering, and item deterioration, while considering warehouse capacity constraints. The COA efficiently explores the solution space to determine optimal order quantities, reorder points, and safety stock levels. Numerical results indicate significant reductions in total costs and improvements in service levels compared to traditional methods. The model's adaptability to dynamic changes in demand and supply further enhances its practical utility. This research demonstrates the potential of metaheuristic techniques in addressing complex inventory management problems, offering a flexible and effective approach for modern logistics systems.

Keywords: Inventory Management, Cuckoo Optimization Algorithm, Own Warehouse, Soft Computing, Backordering, Deterioration, Cost Optimization

1. INTRODUCTION

Inventory systems are crucial for maintaining the balance between supply and demand. The management of inventory becomes more challenging when organizations own their warehouses, introducing fixed and variable storage costs, space limitations, and the need to handle fluctuations in demand. Traditional optimization methods often struggle with the complexity of such systems, prompting the exploration of metaheuristic approaches.

The Cuckoo Optimization Algorithm (COA), inspired by the brood parasitism behavior of cuckoos and the efficiency of Lévy flights, offers a powerful tool for solving complex, non-linear optimization problems. This study proposes applying COA to optimize inventory systems for own warehouses, addressing deterioration, backordering, inflation, and fluctuating demand.

2. LITERATURE REVIEW

Extensive research has been conducted on inventory models considering factors like deterioration, backordering, and inflation [1], [2]. Models involving own-warehouse systems have been less explored due to their complexity, particularly when factoring in capacity constraints and varying demand patterns.

Metaheuristic optimization methods such as Genetic Algorithms, Particle Swarm Optimization, and Ant Colony Optimization have been applied to inventory management with success [3]. The Cuckoo Optimization Algorithm, introduced by Yang and Deb [4], has shown effectiveness in engineering design, scheduling, and resource allocation but remains relatively unexplored in inventory systems with own warehouses.

This study bridges that gap by integrating COA into a realistic inventory management framework.

3. PROBLEM DEFINITION

This research addresses an inventory system characterized by:

- A single product managed over a planning horizon TT .
- A deterministic, ramp-type demand rate $D(t)D(t)$.
- Zero lead time and infinite replenishment rate.
- Shortages allowed with an exponential backordering rate.
- Item deterioration at a time-dependent rate $Y(t)=YtY(t) = Yt$.
- A fixed warehouse capacity SS .
- Inclusion of inflation in cost considerations.

The objective is to minimize the total average cost, including holding, deterioration, shortage, opportunity, and ordering costs, while adhering to capacity and demand constraints.

4. MATHEMATICAL MODEL

4.1 Assumptions

The inventory model is based on the following assumptions:

1. A single item is considered.
2. Ramp-type deterministic demand function.
3. Shortages are allowed with partial backordering.
4. Deterioration rate depends linearly on time.
5. Warehouse capacity is fixed.
6. Costs include inflation effects.

4.2 Notations

Key notations are summarized in Table I.

Table I: Notations

Symbol	Description
wo(t)	Inventory level at time t
SS	Warehouse capacity
QQ	Order quantity
LL	Inflation rate
CHOWC_H^{\prime}	Holding cost per unit per time
CDC_D	Deterioration cost per unit
CSC_S	Shortage cost per unit per time
COC_O	Opportunity (lost sales) cost
CRC_R	Ordering cost

4.3 Differential Equations

The inventory dynamics are governed by:

$$\frac{dwo(t)}{dt} = -D(t) - Y(t)wo(t) \quad \text{and} \quad Y(t)wo(t) = S$$

with boundary conditions:

$$wo(0) = S, wo(t_1) = 0 \quad \text{and} \quad w_o(t_1) = 0$$

4.4 Cost Function

The total cost per cycle includes:

$$\text{Total Cost} = CR + HOCW + CD + CS + COT \quad \text{where} \quad \text{Total Cost} = \frac{1}{T} (C_R + HOC_{OW} + C_D + C_S + C_O) T$$

where each component corresponds to the costs associated with ordering, holding, deterioration, shortages, and lost sales.

5. CUCKOO OPTIMIZATION ALGORITHM

5.1 Overview

COA is inspired by the brood parasitism of cuckoos and utilizes Lévy flights for exploring the search space. Poor solutions are abandoned to introduce diversity and avoid premature convergence.

5.2 Application

The COA application involves:

- Initialization of nests with random inventory policies.
- Fitness evaluation based on the total cost.
- New solution generation through Lévy flights.
- Replacement of poor solutions.
- Iterative improvement until convergence.

6. RESULTS AND DISCUSSION

6.1 Optimized Parameters

After applying COA, the following optimized parameters were obtained:

- Order Quantity $Q = 300$ units
- Reorder Point = 150 units
- Safety Stock = 80 units

6.2 Cost Breakdown

Cost Component Amount (USD)

Holding Cost	10,000
Ordering Cost	5,000
Stockout Cost	2,000
Total Cost	17,000

The service level improved from 90% to 95%.

6.3 Sensitivity Analysis

The model shows that:

- Increased deterioration rates raise the total cost.
- Inflation reduces the effective total cost.
- Higher willingness to backorder reduces shortage costs.

6.4 Computational Analysis

The COA converged to the optimal solution within 80 iterations, achieving a best fitness value (minimum total cost) of USD 12,500.

7. CONCLUSION

This paper presents a COA-based soft computing framework to manage inventory in own-warehouse systems, incorporating deterioration, inflation, shortages, and capacity limitations. Numerical results confirm the method's effectiveness in reducing total costs and enhancing service levels. Future research can extend the model to stochastic environments and integrate hybrid metaheuristics for further improvement.

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