





$$\begin{aligned}\rho &= \text{Density of air} = 1.225 \text{ kg/m}^3 \text{ at } 25^\circ\text{C} \\ V &= \text{volume of air inside main storage box} = 0.381 * 0.381 * 0.381 \text{ m}^3 \\ &= 0.0553 \text{ m}^3 \\ \therefore m_{air} &= 1.225 * 0.0553 = 0.0677 \text{ kg} \\ C_{(v)air} &= 0.718 \text{ kJ/kg-k} \\ \Delta T &= T_1 - T_2 \\ T_1 &= \text{Temperature inside the main storage box} = 70^\circ\text{C} \\ T_2 &= \text{Lowest atmospheric temperature} = 18^\circ\text{C} \\ \therefore \Delta T &= 70 - 18 = 52^\circ\text{C} \\ \therefore Q_{air} &= 0.0677 * 0.718 * 10^3 * 52 \\ &= 2529.23 \text{ J}\end{aligned}$$

**For Aluminum box**

$$\begin{aligned}Q_{Al} &= m_{Al} C_{Al} \Delta T \\ m_{Al} &= \text{mass of aluminum box} = \rho * V \\ \rho &= \text{Density of aluminum} = 2700 \text{ kg/m}^3\end{aligned}$$

**Calculation of mass of aluminum box:**

**Iteration 1:**

$$\begin{aligned}\text{Assume thickness of aluminum sheet} &= 16 \text{ gauge} \\ &= 1.291 \text{ mm} \\ &= 0.001291 \text{ m} \\ \therefore \text{Volume of aluminum box} &= 0.381 * 0.381 * 0.001291 \\ &= 1.8740 * 10^{-4} \text{ m}^3 \\ \therefore m_{Al} &= 2700 * 1.8740 * 10^{-4} = 0.5 \text{ kg}\end{aligned}$$

This is quite light.

**Iteration 2:**

$$\begin{aligned}\text{Assume thickness of aluminum sheet} &= 14 \text{ gauge} \\ &= 1.628 \text{ mm} \\ &= 0.001628 \text{ m} \\ \therefore \text{Volume of aluminum box} &= 0.381 * 0.381 * 0.001628 \\ &= 2.36 * 10^{-4} \text{ m}^3 \\ \therefore m_{Al} &= 2700 * 2.36 * 10^{-4} = 0.638 \text{ kg}\end{aligned}$$

This is suitable mass for aluminum box.

$$\begin{aligned}C_{Al} &= 0.921 \text{ kJ/kg-k} \\ \Delta T &= T_1 - T_2 \\ T_1 &= \text{Temperature inside the main storage box} = 70^\circ\text{C} \\ T_2 &= \text{Lowest atmospheric temperature} = 18^\circ\text{C} \\ \therefore \Delta T &= 70 - 18 = 52^\circ\text{C} \\ \therefore Q_{Al} &= 0.638 * 0.921 * 10^3 * 52 \\ &= 30561.60 \text{ J}\end{aligned}$$

**Total heat requirement:**

$$\begin{aligned}Q_{total} &= 2529.23 + 30561.60 \\ &= 33090.83 \text{ J} \\ \text{Time up to which we required } Q_{total} \text{ amount of heat} &= 5 \text{ min} \\ &= 300 \text{ sec} \\ \therefore \text{Power required} &= Q_{total} / \text{time} \\ &= 33090.83 / 300 \\ &= 110.30 \text{ watts}\end{aligned}$$

**Input power (source power):**

$$\begin{aligned}P &= V * I \\ V &= \text{Voltage of alternator} = 14.4 \text{ v at full load condition} \\ I &= \text{Current from alternator} = 55 \text{ Amps (maximum capacity)} \\ \therefore P &= 14.4 * 55 \\ &= 792 \text{ watts}\end{aligned}$$

**Dimension calculation of heating coil:**

$$\begin{aligned}\text{Outer diameter of strip on which heating coil is wrapped} \\ &= 35.4 \text{ mm (assume)}\end{aligned}$$

$\therefore$  Perimeter of the strip =  $\pi D$   
 $= 0.1112 \text{ m}$   
 Length of the coil / strip =  $(0.1112) \cdot 0.381 / d$   
 Where,  $d$  = diameter of heating coil  
 We know that,  $P = I^2 \cdot R$   
 $110.3 = 55^2 \cdot R$

$\therefore R = 0.036 \Omega$

We know that,

$$R = \frac{\rho L}{A}$$

$\rho$  = Resistivity of heating coil material

**Iteration 1:**

We take Nichrome as a heating coil material.

$$\rho_{\text{nichrome}} = 1.1 \cdot 10^{-6} \Omega \cdot \text{m}$$

$$\therefore 0.036 = 6 \cdot \left[ \frac{1.1 \cdot 10^{-6}}{\frac{\pi}{4} d^2} \cdot \left( \frac{0.1112 \cdot 0.381}{d} \right) \right]$$

$$\therefore d = 21.46 \text{ mm}$$

This is a very large diameter of heating coil which is not suitable.

**Iteration 2:**

Now, we take Copper as a heating coil material.

$$\rho_{\text{copper}} = 1.72 \cdot 10^{-8} \Omega \cdot \text{m}$$

$$\therefore 0.036 = 6 \cdot \left[ \frac{1.72 \cdot 10^{-8}}{\frac{\pi}{4} d^2} \cdot \left( \frac{0.1112 \cdot 0.381}{d} \right) \right]$$

$$\therefore d = 5.36 \text{ mm}$$

This is quite suitable diameter as compared to nichrome diameter.

$$\therefore d = 5.36 \text{ mm} = 4 \text{ gauge}$$

$$\text{So, length of wire / strip} = (0.1112) \cdot 0.381 / 5.36 \cdot 10^{-3}$$

$$= 7.9 \text{ m}$$

$$L_{\text{total}} = 6 \cdot 7.9 \text{ m} = 47.42 \text{ m}$$

**Temperature generated on the strip:**

$$Q_{\text{required}} = m_{\text{cu}} C_{\text{cu}} \Delta T$$

$$Q_{\text{required}} = 33090.83 \text{ J}$$

$$C_{\text{copper}} = 0.385 \text{ kJ/kg} \cdot ^\circ\text{C}$$

$$m_{\text{copper}} = \text{mass of copper wire} = \rho \cdot V$$

$$\rho = \text{Density of copper wire} = 8960 \text{ kg/m}^3$$

$$V = \text{volume of copper wire} = \frac{\pi}{4} d^2 \cdot l = \frac{\pi}{4} 0.00536^2 \cdot 7.9$$

$$= 1.78 \cdot 10^{-4} \text{ m}^3$$

$$\therefore m_{\text{copper}} = 8960 \cdot 1.78 \cdot 10^{-4} = 1.6 \text{ kg}$$

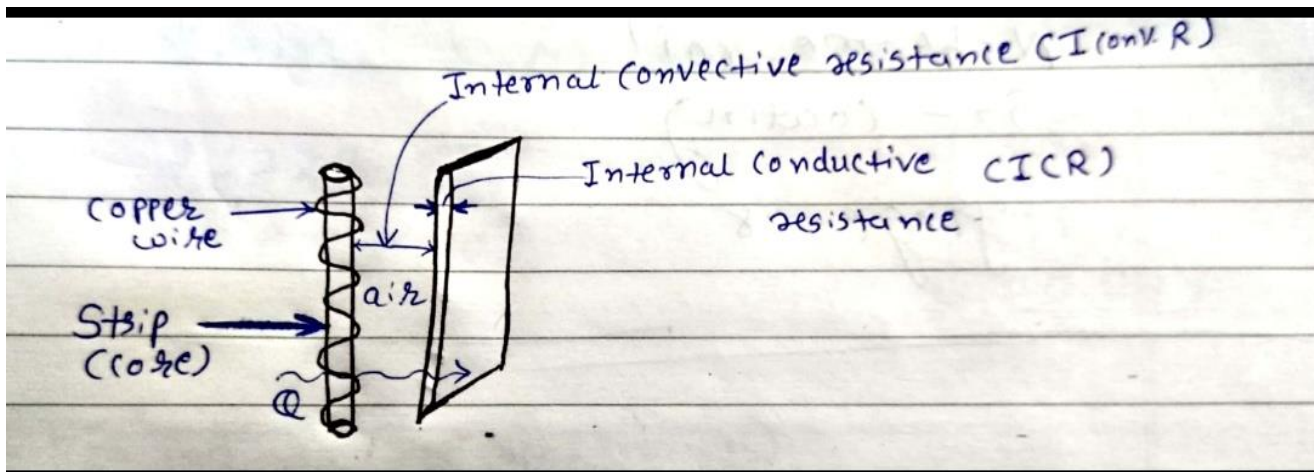
$$\therefore 33090.83 = 1.6 \cdot 385 \cdot (T_1 - 25)$$

$T_1$  = Temperature generated on the strip

$25^\circ\text{C}$  = Surrounding temperature

$$\therefore T_1 = 78.7^\circ\text{C} \approx 80^\circ\text{C}$$

**Heat loss calculations:**



$$\text{Internal convective resistance} = \frac{1}{hA}$$

**Calculation of h (heat transfer coefficient):**

Fan given below is used for proper circulation of hot air inside heating box so that it can be kept warm uniformly leading to increased efficiency of heating box.

**Specification of fan:**

- Length: 40mm
- Width: 40mm
- Thickness: 15mm
- Voltage: 12V
- Current: 0.9Amps
- RPM: 12000
- Air flow: 14 CFM (Cubic feet per minute)



Air Velocity is measurement of the rate of displacement of air or gas at a specific location.

Air velocity (distance traveled per unit of time) is usually expressed in Linear Feet per Minute (LFM). By multiplying air velocity by the cross section area of a duct, you can determine the air volume flowing past a point in the duct per unit of time. Volume flow is usually measured in Cubic Feet per Minute (CFM).

Concept of Air Velocity can be used in air conditioning, heating and ventilating work.

Enter value, select unit and click on calculate. Result will be displayed.

Enter Your Values:

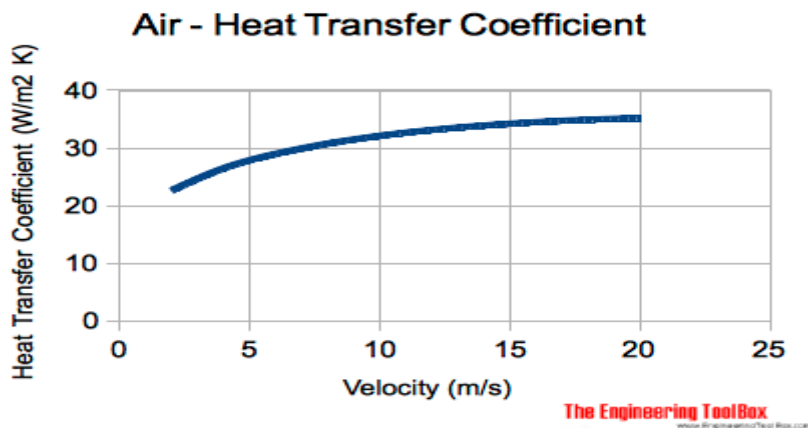
Air Flow:

Rectangle Duct       Circular Duct  
H:  W:   R:

Results:

ft/min (LFM)  
 m/s  
 miles/hr (MPH)  
 ft<sup>3</sup>/min (CFM)  
 m<sup>3</sup>/hr  
 L/s

**Conversion of CFM:** Image given above shows conversion of unit of air flow from CFM to m/s using online convertor [3].  
From above figure,  
14 CFM = 0.05 m/s (air velocity)



### Graph of h vs. air velocity

From graph it is clear that value of h for air = 22 W/m<sup>2</sup>-k

$$\text{Internal convective resistance} = \frac{1}{22 \times (0.381 \times 0.381)} \\ = 0.313 \text{ k/W}$$

$$\text{Internal conductive resistance in aluminium sheet} \\ = \frac{\text{thickness of sheet}}{kA}$$

Thickness of sheet = 0.001628 m

$k = 235 \text{ W/m-k}$

$$\therefore \text{Internal conductive resistance in aluminium sheet} \\ = \frac{0.001628}{235 \times (0.381 \times 0.381)} \\ = 4.77 \times 10^{-5} \text{ k/W (Negligible)}$$

Total resistance = 0.313 k/W

$$\text{Power loss } (\dot{Q}) = \frac{T_1 - T_2}{R_{total}}$$

$$\therefore \dot{Q} = \frac{80 - 70}{0.313 \times 6} \\ = 5.32 \text{ watts}$$

**$\therefore \text{POWER LOSS} = 5.32 \text{ W}$**

### 6.CONCLUSION:

After shortlisting certain materials for heating box and coil, calculations were carried out to finalize the materials for same along with them calculations for temperature generated on strip using this material, for power loss in conduction ,convection and radiation were also done and here is a summary of all the calculations:

Considering extreme conditions of achieving 52 degree celsius temperature difference,under which this system might have to operate, using aluminium box of 14 guage thickness is preferable with heating coil having copper as a material. Resistivity of copper is perfectly suitable for this system as diameter calculated based on it satisfies space criterion of this system. Applying all these specifications, temperature generated on strip comes out to be approximately around 80 degree celsius along with power loss of 5.32 watt which is viable for industry requirements.

### 7. REFERENCES:

1. -PORTABLE WARMER by Charles A. Walton, 19115 Overlook Rd., Los Gatos, Calif. 95030
2. -Food delivery hot bag with electric hot plate by Harold D. Solomon , Wayne R. Greve
3. - <http://www.kylesconverter.com/flow/cubic-feet-per-minute-to-cubic-meters-per-second>