

# AI-Powered Speedcubing: Machine Learning Models for Optimized Solution

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## Abstract

This research paper explores the development and implementation of a Rubik's Cube solver, focusing on both algorithmic strategies and robotic execution. The project investigates various methodologies for solving the Rubik's Cube, including classical algorithms, deep learning techniques, and robotic manipulations. Key algorithms such as Kociemba's algorithm for optimal solving and DeepCubeA, a deep reinforcement learning model, are analyzed for their effectiveness in achieving efficient solutions. Additionally, the paper examines the challenges faced in translating theoretical solutions into practical applications, particularly in robotic implementations that require precise movement and sensory feedback. Results demonstrate that while software-based solvers can achieve high success rates and optimal solutions, physical robotic systems encounter obstacles related to sensor accuracy and environmental variability. This study highlights the interplay between computational efficiency and real-world adaptability in solving complex combinatorial puzzles like the Rubik's Cube, paving the way for future innovations in both algorithm design and robotic dexterity.

## 1. Introduction

The Rubik's Cube, invented in 1974 by Ernő Rubik, is a three-dimensional combination puzzle that has captivated millions around the world. With its intricate design and vast configuration space—approximately 43 quintillion possible states—the Rubik's Cube presents a significant challenge for both human solvers and computational algorithms. Over the years, it has become a benchmark for testing algorithmic efficiency, artificial intelligence, and robotic dexterity.

Solving the Rubik's Cube efficiently requires advanced algorithms that can navigate its complex state space. Theoretical studies have established "God's Number," which refers to the minimum number of moves required to solve the cube from any scrambled position; this number is known to be 20 for the standard 3x3 cube. Various algorithms have been developed to approach this problem, including Kociemba's algorithm, which optimally solves the cube in fewer moves than traditional methods.

In recent years, advancements in artificial intelligence (AI) and machine learning have led to innovative approaches for solving the Rubik's Cube. Deep reinforcement learning (DRL) techniques, such as DeepCubeA, have demonstrated remarkable success in training models that can solve the cube efficiently without human intervention. These AI-driven solvers not only achieve high accuracy but also adapt to various configurations with minimal prior knowledge.

Moreover, the integration of robotics into Rubik's Cube solving has introduced new challenges and opportunities. Robotic systems designed to manipulate physical cubes must address issues such as precise movement control, sensor accuracy, and environmental variability. Projects like OpenAI's robotic hand showcase the potential of combining AI with physical manipulation to achieve real-world solutions.

This paper aims to explore the intersection of algorithmic innovation and robotic implementation in Rubik's Cube solving. By analyzing different methodologies and their respective successes and challenges, we seek to provide insights into how these advancements can be applied to other complex combinatorial problems and enhance our understanding of both computational theory and practical robotics. Through this exploration, we aim to highlight the ongoing relevance of the Rubik's Cube as a platform for research and development in algorithm design and robotics.

## 2. Related Work

Recent advancements in Rubik's Cube solving leverage computational algorithms, deep reinforcement learning (DRL), and robotic systems. Below is a synthesis of key methodologies and their contributions to the field.

### 2.1 Algorithmic Foundations

The Rubik's Cube's vast state space ( $\approx 43$  quintillion configurations) and NP-hard complexity for generalized variants have driven theoretical research. MIT studies established God's Number (the minimum moves required to solve any cube state) as 20 for the  $3 \times 3 \times 3$  cube, with upper bounds of  $\Theta(n^2/\log n)$  for  $n \times n \times n$  cubes; solving  $n \times n \times 1$  puzzles was proven NP-hard when ignoring cubie positions, highlighting the computational challenges of cube-solving algorithms.

### 2.2 AI and Reinforcement Learning

UC Irvine researchers pioneered DeepCubeA, a DRL algorithm that solves the Rubik's Cube in under a second with 100% accuracy across all test configurations. Trained on 10 billion simulations using NVIDIA GPUs and TensorFlow, DeepCubeA identifies optimal paths ( $\leq 30$  moves) 60.3% of the time without human guidance. The algorithm combines Monte Carlo Tree Search (MCTS) with policy-value networks, extending its capabilities to puzzles like Lights Out and Sokoban.

Building on this, Autodidactic Iteration (a self-learning DRL framework) was developed to solve cubes without prior domain knowledge, achieving median solve lengths comparable to human

strategies. These innovations underscore DRL's potential in combinatorial optimization tasks with sparse rewards.

### 2.3 Robotic Implementations

OpenAI's robotic hand represents a breakthrough in physical cube manipulation. Using Automatic Domain Randomization (ADR), the system trains entirely in simulation, adapting to real-world perturbations like friction and object deformations. The neural networks achieve a 60% success rate under maximal scrambling (26 moves) and demonstrate emergent meta-learning, adjusting strategies in response to disruptions. Challenges include balancing cube-solving with real-time adaptation, particularly during initial manipulations.

MIT's FPGA-based robot employs RGB sensors and stepper motors to execute Kociemba's algorithm, though real-world deployment faces limitations such as lighting-dependent sensor accuracy.

### 3. Comparative Analysis

Approach	Key Features	Success Rate	Limitations
DeepCubeA <sup>1 3 4 6</sup>	DRL with MCTS; trained on 10B simulations	100%	Simulation-only; no physical control
OpenAI ADR <sup>2</sup>	Robotic hand trained via ADR; meta-learning	60% (max scramble)	High computational cost
MIT FPGA Robot <sup>5</sup>	Sensor-based Kociemba solver	Partial	Sensor reliability in dynamic environments

### 4. Proposed Methodologies

This section outlines the methodologies employed in the development of Rubik's Cube solvers, focusing on algorithmic approaches, deep reinforcement learning techniques, and robotic implementations. Each methodology is designed to address specific challenges associated with solving the Rubik's Cube efficiently and effectively.

#### 4.1 Algorithmic Approaches

One of the foundational methodologies for solving the Rubik's Cube involves algorithmic strategies that leverage mathematical principles and heuristics. Key algorithms include:

- **Kociemba's Algorithm:** This two-phase algorithm is widely recognized for its efficiency in finding optimal solutions. The first phase reduces the cube to a specific state, while the

second phase solves it from that state. Kociemba's algorithm can solve any configuration in 20 moves or fewer, making it an essential tool for both theoretical analysis and practical applications.

- **Thistlethwaite's Algorithm:** This method divides the solving process into four phases, progressively reducing the cube's complexity until it reaches a solved state. While effective, it typically requires more moves than Kociemba's algorithm but provides valuable insights into the structure of cube configurations.

These algorithms serve as a basis for developing software-based solvers that can quickly compute solutions for various cube states.

## 4.2 Deep Reinforcement Learning (DRL)

Recent advancements in artificial intelligence have led to the application of deep reinforcement learning techniques for solving the Rubik's Cube. The proposed DRL methodology includes:

- **DeepCubeA:** This DRL model utilizes a combination of convolutional neural networks (CNNs) and Monte Carlo Tree Search (MCTS) to learn optimal strategies for solving the cube. Trained on billions of simulations, DeepCubeA can solve configurations in under one second with high accuracy. The model learns to evaluate potential moves and their outcomes, refining its strategy through self-play.
- **Self-Play Training:** The model engages in self-play to explore various configurations and develop effective solving strategies without human intervention. This approach allows for continuous improvement and adaptation to new challenges.

By employing DRL, these methodologies aim to achieve near-optimal solutions while minimizing computational resources.

## 4.3 Robotic Implementations

Integrating robotic systems into Rubik's Cube solving presents unique challenges and opportunities. The proposed robotic methodology involves:

- **Automatic Domain Randomization (ADR):** This technique trains robotic hands in simulated environments with randomized conditions, enabling them to adapt to real-world scenarios. By exposing the robot to various perturbations during training, it learns to manipulate the cube effectively despite environmental variability.
- **Sensor Integration:** Robotic systems utilize RGB cameras and advanced sensors to detect cube states accurately. These sensors provide feedback on cube orientation and position, allowing for precise movement execution by stepper motors.

- **Control Algorithms:** Implementing control algorithms that translate cube states into actionable movements is crucial for successful manipulation. These algorithms must account for real-time adjustments based on sensor data to ensure accurate execution of solving sequences.

Through these methodologies, robotic systems aim to bridge the gap between theoretical solutions and practical execution, enhancing their ability to solve the Rubik's Cube efficiently in dynamic environments.

The proposed methodologies encompass a comprehensive approach to Rubik's Cube solving through algorithmic strategies, deep reinforcement learning, and robotic implementations. By leveraging these techniques, researchers aim to develop efficient solvers that not only excel in simulation but also demonstrate adaptability and precision in real-world applications. Future work will focus on refining these methodologies further and exploring their applicability to other complex combinatorial problems.

## 5. Result

The effectiveness of the proposed methodologies for solving the Rubik's Cube is evaluated through various metrics, including success rates, solving times, and the efficiency of both algorithmic and robotic implementations. This section presents the results obtained from different approaches, highlighting their strengths and limitations.

The study on solving the Rubik's Cube using its local graph structure highlights the efficacy of weighted convolutional distance heuristics applied with the A\* search algorithm. Key results include:

**Average Solution Length:** The solver achieves shorter solution lengths as the number of convolution layers increases.

**Average Time Taken:** The time required to compute solutions decreases with more convolution layers due to improved heuristic precision.

**Memory Efficiency:** By focusing on local graph structures rather than the entire state space, memory usage is significantly reduced, enabling solutions for cubes scrambled up to 12 times.

Below is a graphical representation showing the relationship between convolution layers and average solution length:

Convolution Layers	Average Solution Length (Moves)
1	25
2	22
3	20

## 6. Discussion

The results obtained from various methodologies for solving the Rubik's Cube reveal significant insights into the effectiveness and challenges of both algorithmic and robotic approaches. This section discusses the implications of these findings, the interplay between theoretical advancements and practical applications, and future directions for research.

### 6.1 Algorithmic Efficiency

The success of Kociemba's algorithm and DeepCubeA highlights the power of algorithmic optimization in solving complex combinatorial problems. Kociemba's algorithm, with its ability to consistently solve any configuration in 20 moves or fewer, sets a benchmark for efficiency in cube-solving algorithms. The results indicate that as computational power increases, these algorithms can be further refined to minimize solving times and enhance accuracy.

DeepCubeA's integration of deep reinforcement learning has demonstrated a paradigm shift in how AI can approach problem-solving. The model's ability to learn optimal strategies through self-play without prior knowledge showcases the potential of DRL in various applications beyond just Rubik's Cube solving. The high success rate and rapid solving times achieved by DeepCubeA suggest that similar methodologies could be applied to other complex puzzles or optimization problems in fields such as logistics, robotics, and game theory.

### 6.2 Robotic Challenges

While robotic implementations like OpenAI's robotic hand show promise, they also highlight several challenges that need addressing. The 60% success rate achieved under maximal scramble conditions indicates that while the system is capable, it struggles with real-world variability such as lighting conditions and physical perturbations. Sensor accuracy remains a critical factor; variations in environmental conditions can significantly impact performance.

The integration of Automatic Domain Randomization (ADR) has proven beneficial in training the robotic system to adapt to real-world scenarios. However, further research is needed to enhance the robustness of sensor systems and improve the hand's dexterity during manipulation

tasks. Future work should focus on refining these systems to achieve higher success rates and faster solving times across diverse conditions.

### 6.3 Bridging Theory and Practice

The results underscore the importance of bridging theoretical advancements with practical applications. While algorithms like Kociemba's provide optimal solutions in theory, translating these solutions into physical actions requires careful consideration of mechanical constraints and real-time feedback mechanisms.

Robotic systems must not only implement effective algorithms but also adapt to unpredictable factors in their environment. This interplay between algorithmic design and robotic execution is crucial for developing systems that can solve complex problems reliably in real-world situations.

### 6.4 Future Directions

Future research should aim to enhance the capabilities of both algorithmic solvers and robotic implementations. Potential directions include:

- **Hybrid Approaches:** Combining DRL with traditional algorithms may yield more efficient solvers that leverage the strengths of both methodologies.
- **Improved Sensor Technologies:** Developing more reliable sensors capable of functioning under varying environmental conditions will enhance robotic performance.
- **Real-Time Adaptation:** Implementing advanced machine learning techniques that allow robots to adapt their strategies dynamically based on real-time feedback could improve their success rates.
- **Expanding Applications:** Exploring the application of these methodologies to other complex puzzles or optimization problems could lead to broader advancements in AI and robotic .

## 7. Conclusion

This research paper has explored the methodologies and advancements in solving the Rubik's Cube, focusing on algorithmic strategies, deep reinforcement learning, and robotic implementations. The findings demonstrate that both theoretical algorithms and practical applications have made significant strides in efficiency and effectiveness.

The analysis of algorithmic approaches, particularly Kociemba's algorithm and DeepCubeA, reveals their ability to solve the Rubik's Cube with high accuracy and speed. Kociemba's algorithm establishes a benchmark for optimal solutions, consistently achieving results within 20 moves. Meanwhile, DeepCubeA showcases the power of deep reinforcement learning, achieving a 100% success rate in simulations and demonstrating rapid problem-solving capabilities without prior human guidance.

On the robotic front, implementations such as OpenAI's robotic hand highlight the potential for integrating AI with physical manipulation. While these systems show promise, they also face challenges related to sensor accuracy and environmental variability. The use of Automatic Domain Randomization has proven beneficial in training robots to adapt to real-world conditions, yet further improvements are necessary to enhance their reliability and performance.

Overall, this study underscores the importance of bridging theoretical advancements with practical applications. The interplay between algorithmic design and robotic execution is crucial for developing systems capable of solving complex problems in real-world environments. Future research should focus on refining these methodologies, improving sensor technologies, and exploring hybrid approaches that combine the strengths of various techniques.

In conclusion, the Rubik's Cube remains a valuable platform for testing and advancing computational algorithms and robotic dexterity. The insights gained from this exploration not only contribute to the field of combinatorial problem-solving but also pave the way for innovations in artificial intelligence and robotics that can be applied across diverse domains.

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