

# Dynamic Wireless Power Transfer System for Electric Vehicles to Simplify Ground Facilities, Real-time Power Control and Efficiency Maximization

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**Abstract:-** Wireless Power Transfer (WPT) is the process where electrical energy is transferred from a power source to an electrical load across an air gap using induction coils. These coils produce an electromagnetic field which sends energy from a charging base station (transmitter) to a coil on a portable device (receiver) with complete galvanic isolation. The receiver coil takes power from electromagnetic field and converts it into electrical power.

This focuses on dynamic wireless power transfer for electric vehicles and proposes a vehicle-side control method for real-time power control and efficiency maximization. The proposed control strategy and controller design are presented based on a real-time estimation of the mutual inductance between a transmitter and a receiver. Simulations and experiments demonstrate that the proposed method can achieve the maximum efficiency and the desired power simultaneously.

## 1. INTRODUCTION

The transfer of energy from a source to a receiver has traditionally necessitated the use of a physical connection. Indeed, electrical grids and the power outlets span nearly the entire globe and deliver power to billions of people worldwide. Recently, there has been much interest into the area of wireless power transfer (WPT) that is the transmission of power without the need for physical connection. Research into WPT, however is nothing new as experiments in the field took place as far back as Nikola Tesla in the early 20th century.

Wireless power transfer (WPT) is one of the hottest research topics in transportation applications. In particular, a dynamic wireless power transfer (DWPT) system for electric vehicles (EVs) has gathered attention to extend the cruising distance of EVs and to reduce the size of the energy storage system. Its ground facilities are mainly composed of power source, high-frequency inverters, transmitters, and so on. As they are applied to rugged roadways over long distances, power control and efficiency maximization of wireless charging are desirable to be achieved on the vehicle side without signal communication. Although previous research has proposed simultaneous control methods of power control and efficiency maximization on the vehicle side, they have not been

applied to the DWPT system. For maximizing the transmitting efficiency in the DWPT system, the mutual inductance between a transmitter and a receiver has to be estimated from the vehicle side. In this paper, an estimation method considering the vehicle-side control is proposed and applied to the simultaneous power and efficiency control. The effectiveness of the proposed method is verified by simulations and experiments.

## 2. WIRELESS POWER TRANSFER VIA MAGNETIC RESONANCE COUPLING

### 2.1 Circuit analysis:

The transmitter and the receiver coils are shown in Fig. 2.1. They are compensated by resonance capacitors for WPT via magnetic resonance coupling, which can achieve a highly efficient mid-range transmission and robustness to misalignment. In this paper, a series-series (SS) compensated circuit topology is used and its circuit diagram is shown in Fig. 2.2. The transmitter and the receiver are characterized by the inductances  $L_1$ ,  $L_2$ , the series-resonance capacitances  $C_1$ ,  $C_2$ , and the internal resistances  $R_1$ ,  $R_2$ , respectively.  $L_m$  is the mutual inductance between the transmitter and the receiver.

These parameters are expressed in Table 2.1. If power source angular frequency is designed as follows:

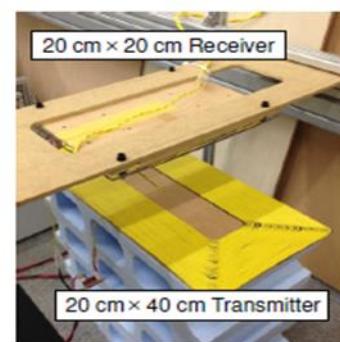


Fig 2.1: Coil

Table 2.1 : Parameters of the coil

	Transmitter	Receiver
Resistance $R_1, R_2$	1.95Ω	1.6Ω
Inductance $L_1, L_2$	417.1μH	210μH
Capacitance $C_1, C_2$	6030pF	12110pF
Resonant frequency $f_1, f_2$	100.4kHz	99.7kHz
Coil gap	100mm	
Mutual Inductance $L_m$	36.3μH (no misalignment)	
Coupling coefficient $k$	0.122 (no misalignment)	

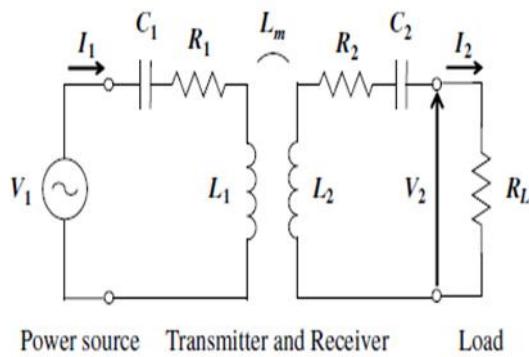
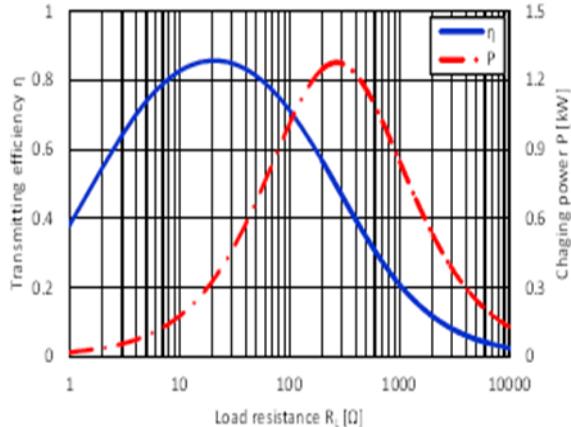


Fig. 2.3: Equivalent circuit of WPT system

Fig. 2.4:  $R_L$  v/s  $\eta$  and  $P$ 

$$\omega_0 = \frac{1}{\sqrt{L_1 C_1}} = \frac{1}{\sqrt{L_2 C_2}} \quad \text{--- (2.1)}$$

The transmitting efficiency  $\eta$  and the transmitting power  $P$  can be obtained as follows:

$$\eta = \frac{(\omega_0 L_m)^2 R_L}{R_2 + R_L \{R_1 R_2 + R_1 R_L + (\omega_0 L_m)^2\}} \quad \text{--- (2.2)}$$

$$P = \frac{(\omega_0 L_m)^2 R_L}{\{R_1 R_2 + R_1 R_L + (\omega_0 L_m)^2\}^2} V_1^2 \quad \text{--- (2.3)}$$

Where  $V_1$  is the RMS value of the primary voltage and  $R_L$  is the load resistance. When  $V_1$  equals to 100V,  $\eta$  and  $P$  are expressed in Fig 2.3. In order to maximize the transmitting efficiency  $\eta$ ,  $R_L$  has to be given as follows:

$$R_{L\eta\max} = \sqrt{R_2 \frac{(\omega_0 L_m)^2}{R_1} + R_2} \quad \text{--- (2.4)}$$

Then, the transmitting power  $P$  is determined by  $R_{\eta\max}$ . As a result, the desired power cannot be achieved only using  $R_L$  optimization when the transmitting efficiency  $\eta$  is maximized.

## 2.2 System configuration:

In order to achieve the maximum efficiency and the desired power simultaneously, the vehicle is equipped with two power converters, i.e. Half Active Rectifier (HAR) and the DC-DC converter. The circuit diagram of the DWPT system is shown in Fig. 2.4. The ground facility consists of voltage source  $V_S$  and an inverter, which generates a square wave voltage with resonance angular frequency  $\omega_0$ . The transmitting power  $P$  is rectified by the HAR and the charging power  $P_L$  is controlled by the DC-DC converter. These control strategies and controller design methods are described below.

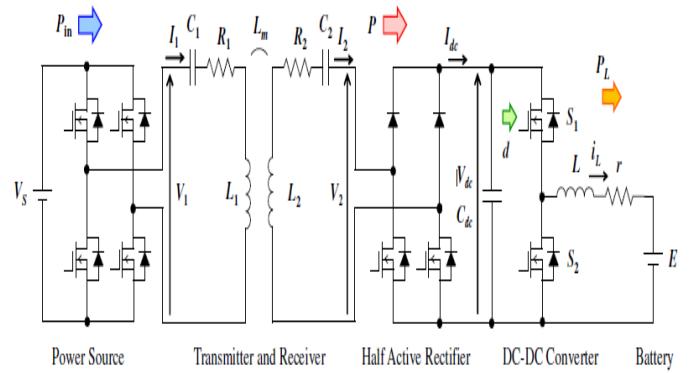


Fig. 2.5: Circuit diagram of the DWPT system.

## 3. Efficiency Maximization by Half Active Rectifier

### 3.1 DC link voltage control:

The HAR regulates the DC link voltage  $V_{dc}$  for efficiency maximization.  $V_{dc}$  control is achieved using two operation modes of HAR, which are shown in Fig. 3.1. When the lower arm MOSFETs are off-state, HAR is operated as the rectification mode. If the MOSFETs are turned on, HAR becomes the short mode and the receiver is shorted. Assuming the transmitting power  $P$  is larger than the load power  $P_L$ ,  $V_{dc}$  is increased during the rectification mode. On the other hand,  $V_{dc}$  is decreased during the short mode because  $P$  is cut-off and  $P_L$  is supplied by the DC link capacitor. Therefore, the waveform of  $V_{dc}$  can be depicted in Fig.3.2.

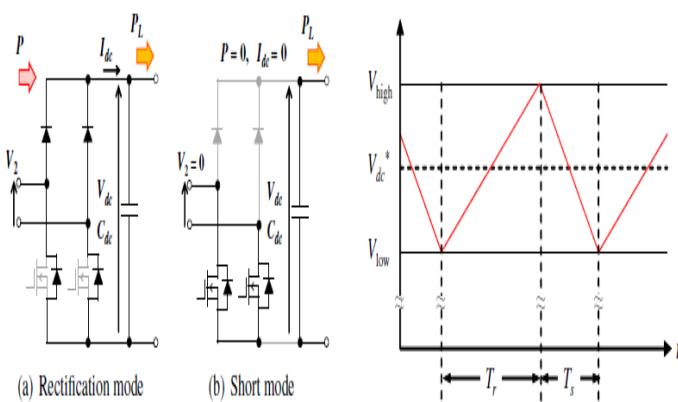


Fig 3.1: Operation modes of Half Active Rectifier.  
Fig 3.2: Waveform of the DC link voltage

If the upper bound  $V_{high}$  and the lower bound  $V_{low}$  are defined as follows:

$$V_{high} = V_{dc}^* + \Delta V \quad \text{--- (3.1)}$$

$$V_{low} = V_{dc}^* - \Delta V \quad \text{--- (3.2)}$$

Where  $V_{dc}^*$  the reference value of the DC link voltage and  $\Delta V$  is the hysteresis band,  $V_{dc}$  is kept within the desired range.

### 3.2 Efficiency Maximization:

In order to maximize the transmitting efficiency, the load resistance  $R_L$ , which is expressed in Fig. 2.2 has to satisfy eq. (2.4) during the rectification mode. If  $V_{dc}^*$  is given as follows:

$$V_{dc\eta\max} = \sqrt{\frac{R_2}{R_1}} \frac{\omega_0 L_m}{\sqrt{R_1 R_2 + (\omega_0 L_m)^2 + \sqrt{R_1 R_2}}} V_s \quad \text{--- (3.3)}$$

$R_L$  is equated to  $R_{L\eta\max}$  and the transmitting efficiency  $\eta$  can be maximized. On the other hand, during the short mode, the transmitting power  $P$  is drastically decreased because  $R_L$  is minimized. As a result, losses during the short mode are assumed to be negligible to losses during the rectification mode in this paper. Therefore,  $V_{dc}^*$  is determined only by  $V_{dc\eta\max}$ .

### 3.3 Mutual inductance estimation:

For tracking the maximum efficiency in the DWPT system, the mutual inductance  $L_m$  has to be estimated to obtain  $V_{dc\eta\max}$  only using the vehicle-side information. From the circuit equations of the DWPT system, the estimation equation of  $L_m$  can be given as follows.

$$L_m = \frac{V_1 + \sqrt{V_1^2 - 4R_1 I_2 (V_2 + R_2 I_2)}}{2I_2 \omega_0} \quad \text{--- (3.4)}$$

Although eq. (3.4) has two solutions, the solution with a positive sign is used in this paper. Assuming the RMS primary voltage  $V_1$  is constant and given to simplify ground facilities,  $L_m$  can be estimated from the vehicle side. The RMS secondary voltage  $V_2$  and the RMS secondary current  $I_2$  are calculated from the DC link voltage  $V_{dc}$  and the rectified DC current  $I_{dc}$  using Fourier series expansions.

In order to reduce the estimation error due to the sensor noise, recursive least square (RLS) filter is applied. From

eq. (3.4), output  $y[i]$  and regressor  $\varphi[i]$  are determined as follows:

$$y[i] = V_1 + \sqrt{V_1^2 - 4R_1 I_2[i](V_2[i] + R_2 I_2[i])} \quad \text{--- (3.5)}$$

$$\varphi[i] = 2I_2[i]w_0 \quad \text{--- (3.6)}$$

RLS filter is used to estimate  $L_m$  statistically by updating  $L_m[i]$ ,  $y[i]$  and  $\varphi[i]$  with following equations.

$$L_m[i] = L_m[i-1] + \frac{\varphi[i]P[i-1]}{\lambda + \varphi[i]^2 P[i-1]} \epsilon[i]$$

$$\epsilon[i] = y[i] - \varphi[i]L_m[i-1]$$

$$P[i] = \frac{1}{\lambda} \{ P[i-1] - \frac{\varphi[i]^2 P[i-1]^2}{\lambda + \varphi[i]^2 P[i-1]} \} \quad \text{--- (3.7)}$$

Where  $\lambda$  is forgetting factor. The initial values are given as  $L_m[0] = 0$  and  $P[0] = 1$ . In order to use the effective values for the estimation, the RLS filter updates  $L_m[i]$ ,  $y[i]$  and  $\varphi[i]$  only during the rectification mode of the HAR. If the HAR is operated as the short mode,  $I_{dc}$  equals to 0 and the estimated value becomes incorrect. Therefore, the RLS filter has to be improved according to the operation mode of the HAR.

## 4. POWER CONTROL BY THE DC-DC CONVERTER

### 4.1 Modeling of the DC-DC converter:

The DC-DC converter controls the load current  $i_L$  for battery charging. Assuming the DC link voltage  $V_{dc}$  is controlled to  $V_{dc\eta\max}$  by the HAR, the circuit diagram of the DC-DC converter can be expressed in Fig. 4.1 (a).  $E$  is the battery voltage,  $L$  is the inductance of the reactor coil and  $r$  is the internal resistance of the reactor coil and the battery. In this paper, the DC-DC converter model is obtained by the state space averaging method. Assuming the DC-DC converter is operated in the continuous conduction mode, its circuit diagram in each switching modes is expressed in Fig. 4.1 (b) and (c).

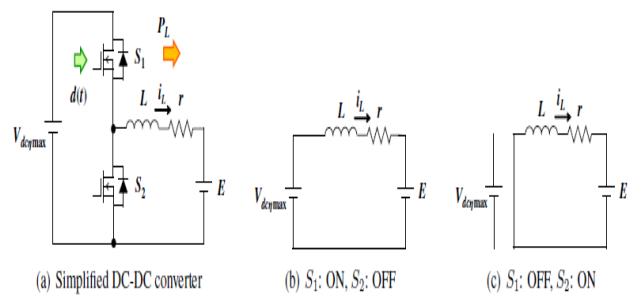


Figure 4.1: Circuit diagram of the DC-DC converter.

From the circuit equation, the state equation of Fig. 4.1 (b) is given as follows:

$$\frac{d}{dt} i_L(t) = -\frac{r}{L} i_L(t) + \frac{1}{L} E + \frac{1}{L} V_{dc\eta\max} \quad \text{--- (4.1)}$$

Also, the state equation of Fig. 4.1 (c) is described as follows:

$$\frac{d}{dt} i_L(t) = -\frac{r}{L} i_L(t) + \frac{1}{L} E \quad \text{--- (4.2)}$$

When  $d(t)$  is defined as the duty cycle of the upper arm MOSFET  $S_1$ , the state space model of the DC-DC converter is obtained as follows:

$$\frac{d}{dt} i_L(t) = -\frac{r}{L} i_L(t) + \frac{1}{L} E + \frac{V_{dc\eta\max}}{L} dt \quad \dots (4.3)$$

In order to apply the linear control theory to the controller design, this model is linearized around an equilibrium point. When  $i_L$  and  $D$  are defined as the equilibrium point,  $i_L(t)$  and  $d(t)$  are expressed as follows:

$$i_L(t) = i_L + \Delta i_L(t) \quad \dots (4.4)$$

$$d(t) = D + \Delta d(t) \quad \dots (4.5)$$

where  $\Delta i_L(t)$  and  $\Delta d(t)$  are the microscopic fluctuations around the equilibrium point.

By substituting eq. (4.4) and eq. (4.5) in eq. (4.3), the linearized DC-DC converter model is given as follows:

$$\frac{d}{dt} i_L(t) = -\frac{r}{L} \Delta i_L(t) + \frac{V_{dc\eta\max}}{L} \Delta d(t) \quad \dots (4.6)$$

Therefore, the transfer function from  $\Delta d(s)$  to  $\Delta i_L(s)$  is obtained as follows:

$$\Delta P_i(s) = \frac{\Delta i_L(s)}{\Delta d(s)} = \frac{V_{dc\eta\max}}{Ls + r} \quad \dots (4.7)$$

#### 4.2 Controller design:

Fig.4.2 shows the block diagram of the proposed control. The feed-forward controller is the same as the equilibrium point calculation, which is given by the constraint of the DC-DC converter. From  $V_{dc\eta\max}$ , which is calculated from  $L_m$ , and the reference value of the load current  $i_L^*$ , the equilibrium point is obtained as follows:

$$i_L = i_L^* \quad \dots (4.8)$$

$$D = \frac{E + r i_L}{V_{dc\eta\max}} \quad \dots (4.9)$$

The feedback controller is designed by the pole placement method. As  $\Delta P_i(s)$  is the first-order system, we apply a PI controller  $C_{Pi}(s)$ , which is expressed as follows:

$$C_{Pi}(s) = \frac{sK_P + K_I}{s} \quad \dots (4.10)$$

If closed loop poles are given by a multiple root  $\omega_d$ , the gains are obtained as follows:

$$K_P = \frac{2L_{wd} - r}{V_{dc\eta\max}} \quad \dots (4.11)$$

$$K_I = \frac{L_{wd}^2}{V_{dc\eta\max}} \quad \dots (4.12)$$

Here,  $V_{dc\eta\max}$  and the gains are calculated by assuming the nominal value of  $L_m$  is 30Mh

## 5. SIMULATION AND EXPERIMENT

### 5.1 Experimental setup:

The experimental setup is shown in Fig. 5.1. The system configuration is the same as Table 5.1. The receiver is driven by the motor to simulate motion of the vehicle. The inverter is operated only while the receiver is above the transmitter to prevent huge power losses. Simulation and experimental conditions are expressed in Table 5.1. The forgetting factor  $\lambda$  of the RLS filter was set to 0.95 and the estimated mutual inductance  $L_m$  was updated only during the rectification mode of the HAR. The reference value of the DC link voltage  $V_{dc\eta\max}$  was calculated from  $L_m$  and the reference value of the load current  $i_L^*$  was set to 1.0 A.

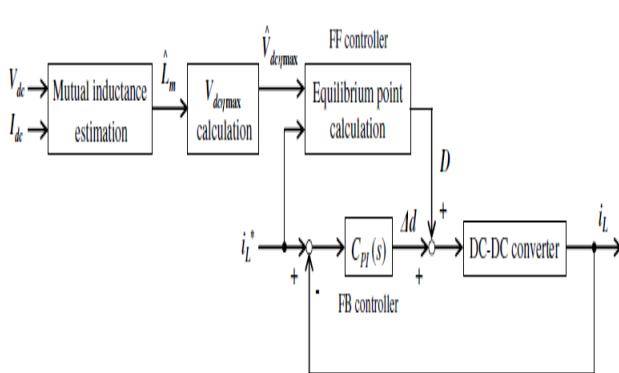
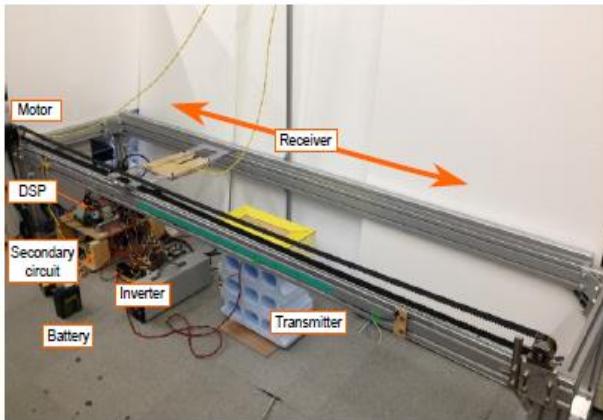
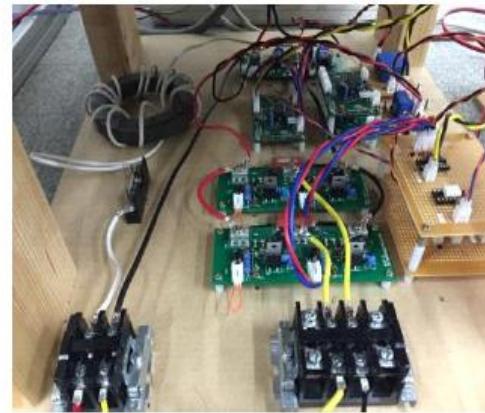


Fig. 4.2: Block diagram of the proposed control.



(a) Whole picture of the DWPT system.



(b) Half Active Rectifier and the DC-DC converter.

Fig. 5.1: Experimental setup.

Parameter	Value	Parameter	Value
Power Source Voltage $V_s$	18V	Battery voltage E	6V
Operating Frequency $f_0$	100kHz	Reactor resistance r	$0.3\Omega$
Hysteresis band $\Delta V$	0.5V	Reactor Inductance L	$1000\mu\text{H}$
Carrier frequency $f_c$	20kHz	DC Link capacitance $C_{dc}$	$200\text{pF}$

Table 5.1: Simulation and experimental conditions.

### 5.2 Simulation:

In the simulations, the change in  $L_m$  was simulated by a sine wave. Its minimum and maximum values were set to  $20\mu\text{H}$  and  $40\mu\text{H}$ .

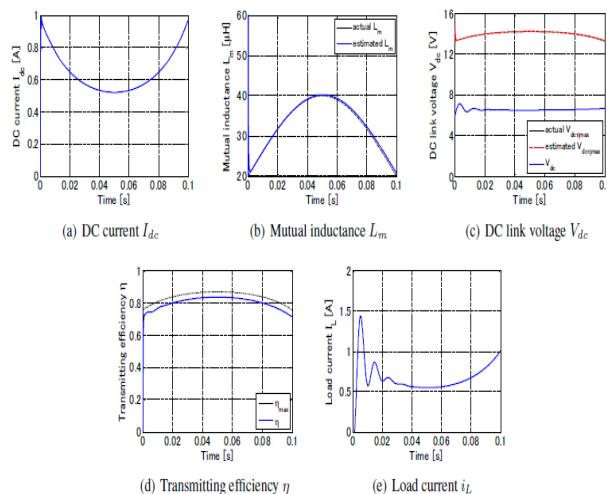


Fig. 5.2: Simulation results without the proposed control

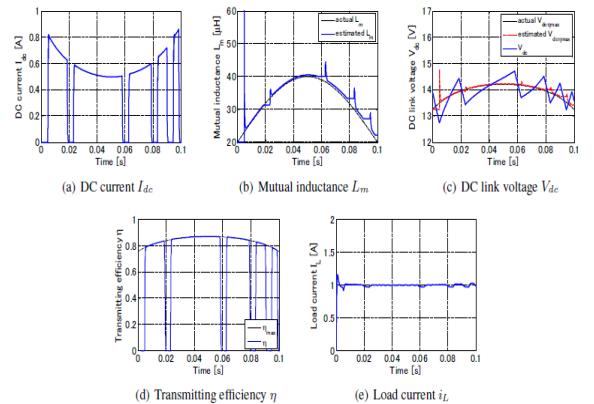


Fig. 5.3: Simulation results with the proposed control.

Fig.5.2 shows the simulation results without the proposed control. In this simulation, the HAR was operated as only the rectification mode and the duty cycle d of the DC-DC converter was equated to 0.95. From Fig.5.2 (b),  $L_m$  is closely matched with the actual  $L_m$ . However, the transmitting efficiency  $\eta$  is decreased from the maximum efficiency because the DC link voltage  $V_{dc}$  cannot be regulated to  $V_{dc\eta\max}$ . Furthermore, the load current  $i_L$  cannot be controlled to  $i_L^*$ . Fig. 5.3 shows the simulation results with the proposed control. The closed loop poles of the proposed control were placed at  $-2000$  rad/s. Although  $L_m$  was estimated only during the rectification mode of the HAR,  $L_m$  accords with the actual  $L_m$  as shown in Fig.5.3 (b). From Fig.5.3 (c) and (d),  $V_{dc}$  is regulated around  $V_{dc\eta\max}$  and  $\eta$  is maximized during the rectification mode. In addition, Fig.5.3 (e) indicates that the load current control can be achieved.

### 5.3 Experiment:

In the experiments, the receiver was driven at 10 km/h and  $L_m$  was compared to the actual  $L_m$ , which was measured by an LCR meter (NF Corp., ZM2371). The DC to DC efficiency  $\eta_{dc}$  includes not only the transmitting efficiency but also the converter efficiency because it was measured by the DC voltages and currents on each side. Therefore, improvement of system efficiency is verified in the experiments. Fig.5.4 shows the experimental results

without the proposed control. The HAR and the DC-DC converter were operated at the same condition as the simulation without control. From Fig.5.4 (b),  $L_m$  and the actual  $L_m$  are closely matched. Although  $L_m$  has a short-time delay,  $V_{dc\eta\max}$  is near by the actual  $V_{dc\eta\max}$  as shown Fig.5.4(c). However, the transmitting efficiency cannot be maximized because  $V_{dc}$  is not regulated to  $V_{dc\eta\max}$ . Furthermore, Fig. 5.4 (e) indicates that  $i_L$  cannot be controlled unless the proposed control is applied. In the case of with control, the DC-DC converter started power control when  $V_{dc}$  reached  $V_{dc\eta\max}$ . The closed loop poles of the proposed control were placed at -1000 rad/s. Fig. 5.5 shows the experimental results with the proposed control. Although the error of  $L_m$  is larger than without control,  $V_{dc}$  can be controlled around  $V_{dc\eta\max}$  as shown in Fig. 5.5 (c). From Fig. 5.5 (d),  $\eta_{dc}$  during the rectification mode of the HAR is increased compared to without control. In addition, Fig. 5.5 (e) shows that  $i_L$  can be controlled to  $i_L^*$ . If the closed loop poles of the proposed control are optimized, it is possible to suppress the current ripple due to the fluctuation of  $V_{dc}$ .

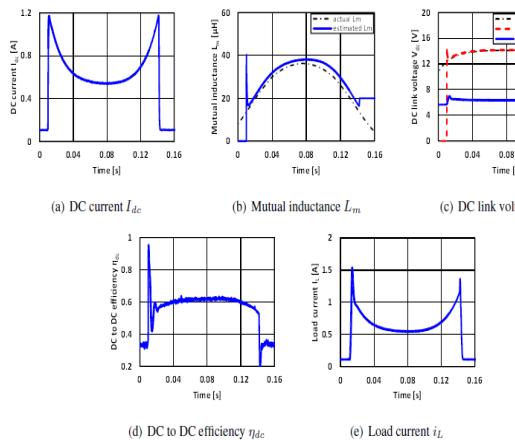


Fig. 5.4: Experimental results without the proposed control

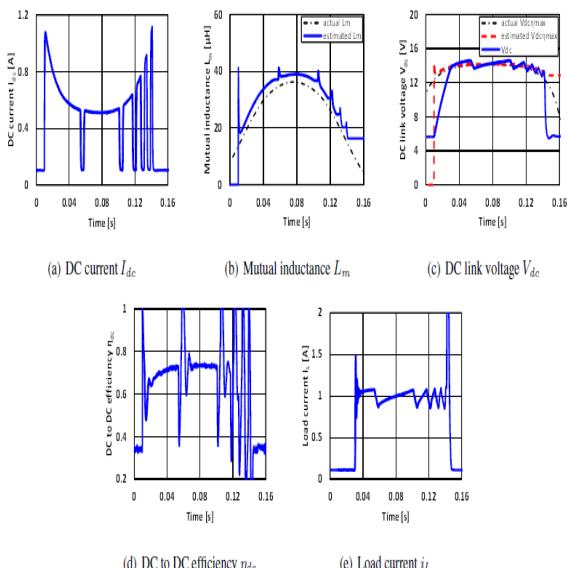


Figure 5.5: Experimental results with the proposed control

## 6. CONCLUSION

This proposed a simultaneous control method of real-time power control and efficiency maximization based on improved mutual inductance estimation from the vehicle side. Its control strategy and controller design methods were presented. The effectiveness of the proposed method was verified by the simulations and the experiments. Future works are to propose an efficiency maximization method considering losses during the short mode of HAR and to design an optimal controller for the proposed control. Furthermore, the proposed method is implemented to an actual DWPT system using an EV.

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