Multiple Feature Extraction Methods for Handwritten Marathi Numeral Recognition
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Abstract
In this Paper, we present robust and novel methods for recognition of isolated handwritten Marathi numeral recognition. Density, Moments, Fourier Descriptor and chain codes are used as features. The recognition results are studied Support Vector Machine (SVM) classifiers. The system is experimented with our database of 12690 samples of Marathi handwritten numerals using fivefold cross validation method. Comparative study of different methods is presented.

Keywords
Handwritten numerals, density, moment, Fourier Descriptor, Chain code, SVM classifier.

1. Introduction
Handwritten Marathi numeral recognition is a difficult problem, not only because of the great amount of variations in human handwriting, but also because certain numerals when handwritten look similar and sometimes they cannot be recognized manually also. These numerals written in Devanagari script are also used in many different Indian languages. Hence, as compared to other Indian scripts, the Devanagari script numerals find more applications in many areas including postal zip code processing and automatic data entry in forms in different languages.

Many systems have been proposed for recognition of characters, both printed and handwritten, for Japanese, Persian and Arabic scripts, including Indic scripts [1, 2, 5, 8, 9, 10, 11, 13, and 15]. Some efficient system proposed for recognition of Devanagari includes [15, 12, 3, 6, 16, 17, 4]. We also found some work in Kannada [18, 7, 4].

2. Marathi numerals and pre-processing
Marathi is spoken by about 71 million people in Indian state of Maharashtra and neighboring states. Percentage wise it is the fourth widely spoken Indian language. Marathi script is written with Devanagari alphabet. Since the standard database for Marathi handwritten numerals is not available, to our knowledge, the database is created with respect to variety in handwriting style. Data collection is done on a sheet specially designed for data collection. Data is collected from persons of different professions. A sample data sheet is shown in figure-1. Since, data is collected in a predefined format slant correction is assumed to be performed. The collected documents are scanned using scanner at 300 dpi to obtain gray scale images. The images are then binarized using Otsu’s method. The speckles in the binarized images are removed using morphological erode and dilate operations. The numerals are cropped by fitting a minimum bounding box on the numeral. To bring uniformity among the numerals the cropped numeral is normalized to a size of 40x40 pixels. A total of 2500 binary digital images representing Marathi handwritten numerals are obtained. Each image represents a numeral (binary 1) that is unconstrained, isolated and clearly discriminated from the background (binary 0).

Fig. 1: Sample handwritten datasheet

3. Feature Extraction
Feature extraction facilitates extracting potential information about the numeral image. The information gathered forms the basis for feature vector that will be used in pattern classification. Following are different methods used for feature extraction.
3.1 Density
In the proposed method, the binary image representing the handwritten numeral is pre-processed as described in the Section 2 and is normalized to a size of 48 x 48 pixels. The size-normalized image is divided into n equal number of zones in sequence for n = 4, 9, 16 and 36 respectively.

The density of the zone is computed by taking the ratio of total number of object pixels (i.e. pixels representing the numeral viz. binary 1) to total number of pixels in the zone (Equation 1). This is carried out for all the zones in the image. Totally 65 features are extracted from the image (Refer algorithm for details). An example is shown in Figure 2.

\[
\mu_{pq} = \sum_x \sum_y (x-x')^p (y-y')^q f(x, y) \quad \text{for} \quad p, q = 0, 1, 2, 3 \quad \text{such that} \quad p + q \leq 3
\]

3.3 Fourier Descriptors
The Fourier transform of a boundary representation (chain code, signature, complex boundary function) is used to represent the region's shape. One can low pass filter the boundary function spectrum without destroying the characteristic shape of the region. This means that only the amplitudes and phases of the low frequency components in the spectrum (i.e. the low-order Fourier coefficients) are required to characterize the basic shape of the object and they can be used as shape descriptors. Before calculating the Fourier descriptors input image must be segmented and boundary of the object must be determined. The boundary will be presented as an array of complex numbers which correspond to the pixels of the object boundary if the image is placed in the complex plane. Fourier descriptors are now calculated by combining Fourier transform coefficients of the complex array.

![Figure 3 A digital boundary and its representation as a complex sequence](image)

The points (xo, yo) and (x1, y1) are the first two points in the sequence. As shown in Figure 4.1, the K-point digital boundary in the xy-plane starting at an arbitrary point (x0, y0) co-ordinate pairs (x0, y0), (x1, y1), (x2, y2),……..(xk-1, yk-1) are encountered in traversing the boundary say, in the counterclockwise direction. These co-ordinates can be expressed in the form of \(x(k) = x_k\) and \(y(k) = y_k\). With this notation, the boundary itself can be represented as sequence of co-ordinates.

3.4 Chain Codes
Chain codes are one of the shape representations which are used to represent a boundary by a connected sequence of straight line segments of specified length.
and direction. This representation is based on 4-connectivity or 8-connectivity of the segments [39]. The direction of each segment is coded by using a numbering scheme as shown in Figure below. The re-sampled boundary can be represented by a 4- or 8-code. The starting point can be arbitrarily chosen at the topmost, leftmost point of the boundary (Figure. 5.2).

The chain code of the boundary can be normalized with respect to starting point by simply treating the chain code as a circular sequence of direction numbers and redefine the starting point so that the resulting sequence of numbers forms an integer of minimum magnitude. Further, to normalize the code for rotation (in angles that are integer multiples of directions) by using first difference of the chain code. This difference is obtained by counting the number of direction changes (in, say, counter clockwise direction) that separate two adjacent element of code. Size normalization can be achieved by altering the size of the re-sampling grid.

3.5 Feature Extraction using Density, Moment, Fourier Descriptor and Chain Code

1. **Feature Set I**: Density features based upon the zoning approach as described in section 3.1 is calculated. The result is stored as feature vector of size is 65.

2. **Feature Set II**: Augmenting the density features (as described in section 3.1) with central moment features (as described in section 3.2) of order three and four for the numeral image to get feature vector of size 161.

3. **Feature Set III**: Feature vector comprising 64 dimensional Fourier descriptors invariant to rotation, scale, and translation. Procedure is described in section 3.2.

4. **Feature Set IV**: Feature vector comprising chain code and Fourier Descriptors of magnitude 108 is used as feature. Procedure is describe in section 3.3

5. **Feature Set V**: Features computed by normalizing the chain code and augmenting it with Fourier features. The size of the feature vector is 48. Procedure is described in section 3.3 and 3.4.

4. Classification

We have used SVM classifier in present system. The SVM classifier is basically a two class classifier based on the discriminate functions. A discriminate function represents a surface, which separates the patterns as two classes. For OCR applications a number of two class classifiers are trained with each one distinguishing one class from the other. Each class label has an associated SVM and a test example is assigned to the label of the class whose SVM gives the largest positive output.

5. Experimental Result

The effectiveness of the features proposed in the paper are evaluated by performing experiments on our own database containing 12690 isolated Marathi handwritten numeral images obtained from writers belonging to different age groups and professions. Feature set V comprising 32 dimensional Fourier descriptors and normalized chain code of length 16, has yielded highest recognition accuracy of 98.15%. The Table 1 provides comparative average recognition rates obtained by using different feature sets.

<table>
<thead>
<tr>
<th>Input</th>
<th>Density Features using zoning</th>
<th>Density and Central Moments</th>
<th>FD and Chain Code</th>
<th>FD and Normalized chain Code</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>100.00</td>
<td>100.00</td>
<td>99.61</td>
<td>99.69</td>
</tr>
<tr>
<td>1</td>
<td>96.15</td>
<td>97.16</td>
<td>96.77</td>
<td>97.08</td>
</tr>
<tr>
<td>2</td>
<td>95.60</td>
<td>96.22</td>
<td>97.16</td>
<td>97.01</td>
</tr>
<tr>
<td>3</td>
<td>96.78</td>
<td>97.72</td>
<td>97.09</td>
<td>97.56</td>
</tr>
</tbody>
</table>
The error rate for five different proposed methods is shown in Figure 2. The error rate for numerals 0, 4, 8, and 9 is very less compared to error rates for other numerals. The methods proposed in this thesis were implemented using Mat-lab 7.0 software and PR Tools on Pentium systems.

6. Conclusion
The performance of the method based upon ‘Fourier Descriptor and Normalized Chain Code’, presented in this paper better as compared with other methods. The proposed method performs well and appears promising as compared to other methods in the literature.

Table 2 Performance comparisons of proposed method with other methods in literature

<table>
<thead>
<tr>
<th>Method</th>
<th>Data</th>
<th>Features</th>
<th>Features</th>
<th>Classifier</th>
<th>Recognition</th>
</tr>
</thead>
<tbody>
<tr>
<td>M. Hanmandlu et.al. [35]</td>
<td>3500</td>
<td>Normalize distance</td>
<td>48</td>
<td>Fuzzy</td>
<td>96.00 %</td>
</tr>
<tr>
<td>R. J. Ramteke et.al. [47]</td>
<td>2000</td>
<td>Invariant moments</td>
<td>78</td>
<td>Gaussian</td>
<td>92.28 %</td>
</tr>
<tr>
<td>Reena bajaj [52]</td>
<td>2460</td>
<td>Density, Moment</td>
<td>48</td>
<td>MLP</td>
<td>89.68 %</td>
</tr>
<tr>
<td>U. Pal et.al. [74]</td>
<td>22546</td>
<td>Chain Code</td>
<td>64</td>
<td>Quadratic</td>
<td>98.86 %</td>
</tr>
<tr>
<td>P. M. Patil et.al. [45]</td>
<td>2000</td>
<td>Ring data</td>
<td>---</td>
<td>Fuzzy</td>
<td>99.5 %</td>
</tr>
<tr>
<td>Benne R.G. et.al. [8]</td>
<td>1500</td>
<td>Water Reservoir etc.</td>
<td>13</td>
<td>k-NN</td>
<td>90.20 %</td>
</tr>
<tr>
<td>Proposed</td>
<td>12690</td>
<td>FD and Chain code</td>
<td>48</td>
<td>SVM</td>
<td>98.15 %</td>
</tr>
</tbody>
</table>

7. References


